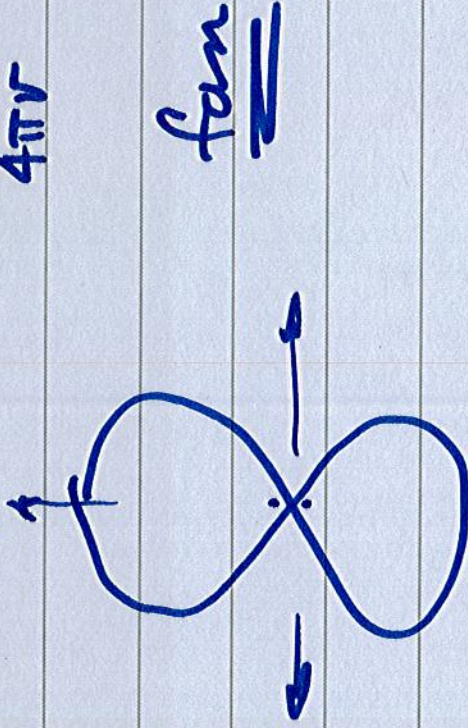


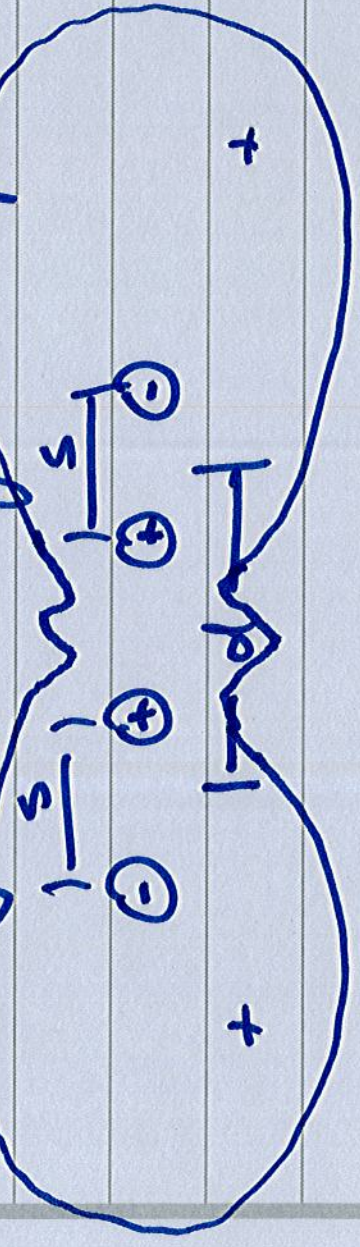
$$\vec{p}(r) = -\frac{1}{4\pi r} \int_{\text{volume}} \rho(\vec{r}') e^{-ikr} d\vec{r}'$$



quadrupole - pt moment - sound radiation from turbulence

- turbulent interaction with a hard surface
- dipole-like

longitudinal quadrupole.



$$ks \ll 1$$

$$kd \ll 1$$

compact sources

- special types of compact sources
 - simple sources
 - monopole - volume efficiency
 - dipole - force
 - quadrupole - moment
 - radiation efficiency
 - drifts

per unit source strength

$$| \text{monopole} | \Rightarrow | \text{dipole} | \Rightarrow | \text{quadrupole} |$$

Multipole Decomposition

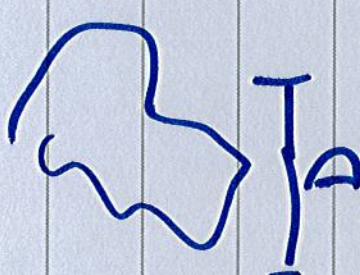
Equivalent source methods (ESM)



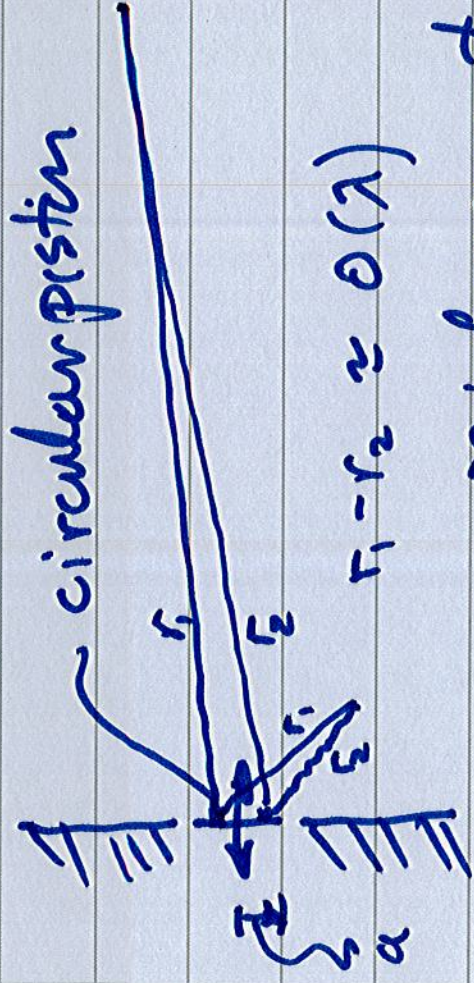
$$\tilde{p}(r) = \sum \text{monopoles} \\ + \sum \text{dipoles} \\ + \sum \text{quadrupoles} \\ + \sum \text{octopoles}$$

5.4 Sound radiation from extended source

- finite extent $\Delta = O(\lambda)$



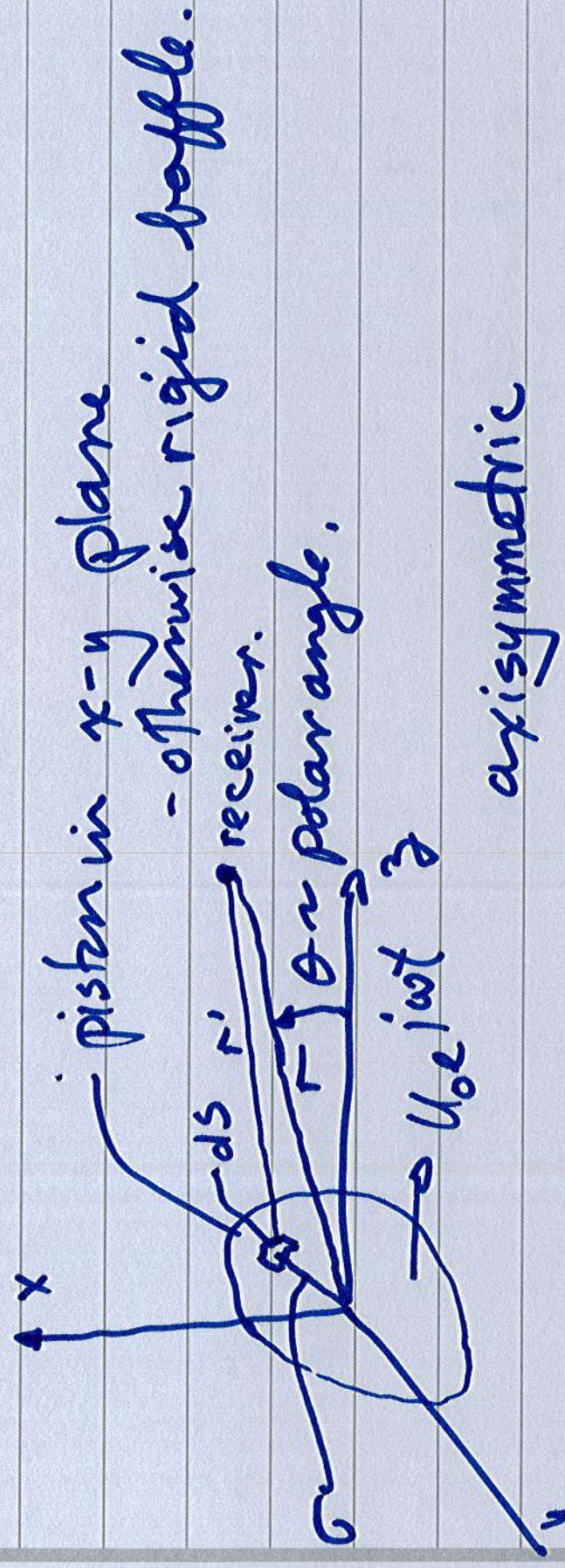
5.4.1 Piston in a Baffle



$a = O(\lambda)$

reinforcement & cancellation is possible.

$r_1 - r_2 \approx O(\lambda)$



$$dQ = U_0 ds$$

contribution from the incremental source
 dS

$$d\vec{p} = j\omega\epsilon_0 k(dQ) \frac{e^{-ikr}}{(2\pi r)}$$

\int monopole on a
 hard surface.

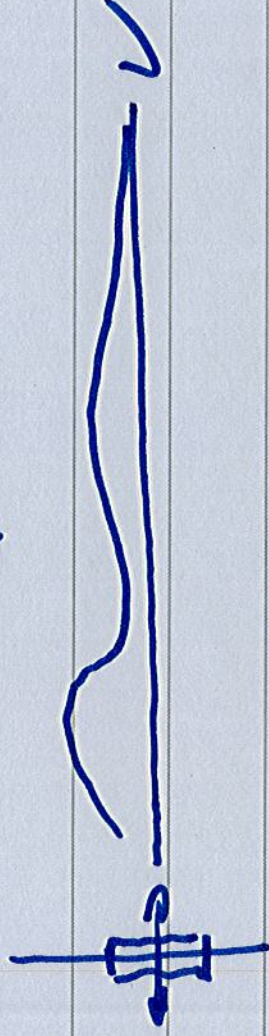
$$dQ = U_0 dS$$

Integrate over the
 surface of the source

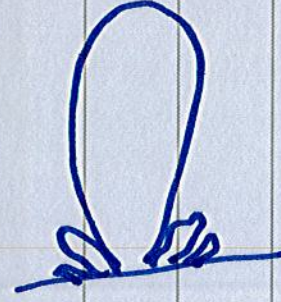
$$\vec{p}(r, \theta) = j \rho_0 c U_0 k \int \frac{e^{-jkr'}}{r'} ds$$

S_2 total piston area

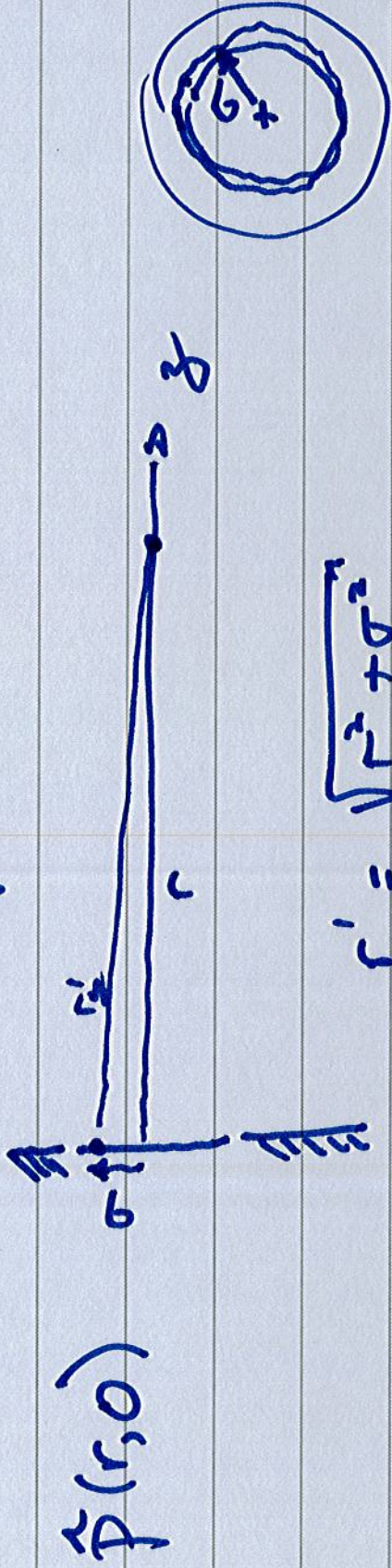
(i) On-axis



(ii) Farfield



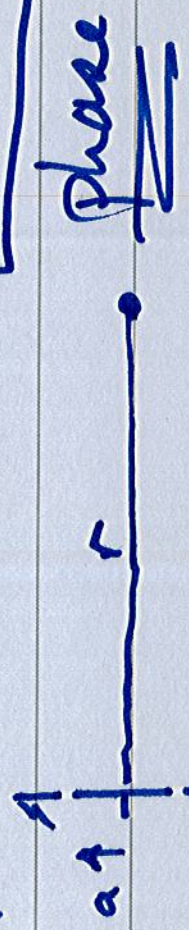
Evaluate The pressure on-axis



$$r' = \sqrt{r^2 + \sigma^2}$$

$$\tilde{P}(r, 0) = j \rho c k U_0 \int_0^\infty \frac{e^{-jk(r^2 + \sigma^2)^{1/2}}}{(r^2 + \sigma^2)^{1/2}} 2\pi \sigma d\sigma$$

$$\vec{p}(r, \theta) = j \rho_0 c U_0 e^{-jkr} e^{-i \frac{kr}{2} [\sqrt{1 + \frac{a^2}{r^2}} - 1]} 2j \sin \left[\frac{kr}{2} [\sqrt{1 + \frac{a^2}{r^2}} - 1] \right]$$



oscillatory function of position

special case

$ka \ll 1$ (compact source)

farfield $\frac{a}{r} \ll 1$

should reduce to a monopole on a hard surface.

farfield

$$\sqrt{1 + \frac{a^2}{r^2}}$$

$$\frac{a}{r} \ll 1$$

$$(1 + x)^{1/2}$$

$$= 1 + \frac{a^2}{2r^2}$$

$$\approx 1 + \frac{x}{2}$$

$$+ \frac{x^2}{3}$$

$$\sin \frac{kr}{2} \left[1 + \frac{1}{2} \frac{a^2}{r^2} - \frac{x}{2} \right]$$

$$\sin \left(\frac{ka}{4} \left(\frac{a}{r} \right) \right)$$

$ka \ll 1$ compar

$\frac{a}{r} \ll 1$ farfield

$$\approx \frac{ka}{4} \left(\frac{a}{r} \right)$$

substitute into

The complete &

take the magnitude

$$Q = \pi a^2 U_0$$

$$|\hat{p}^2(r, 0)| \approx \rho_0 c U_0 \frac{(ka)}{2} \frac{a}{r}$$

$$\approx \rho_0 c k Q \frac{1}{2\pi r}$$

Exactly the same as the monopole on a hard surface.

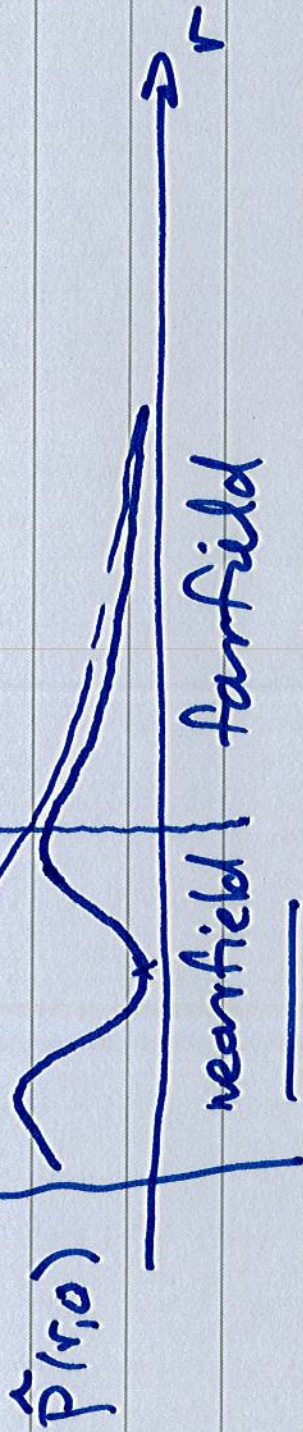
Piston in a baffle
loudspeaker flush
mounted in a wall

if $ka \ll 1$

The L/S can be modeled as a pt. monopole on a hard surface.

complete solution

$\sim 1/r$ dependence



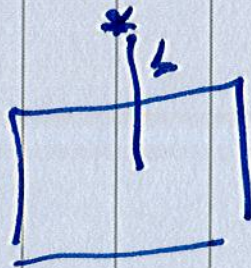
oscillatory |

sound field

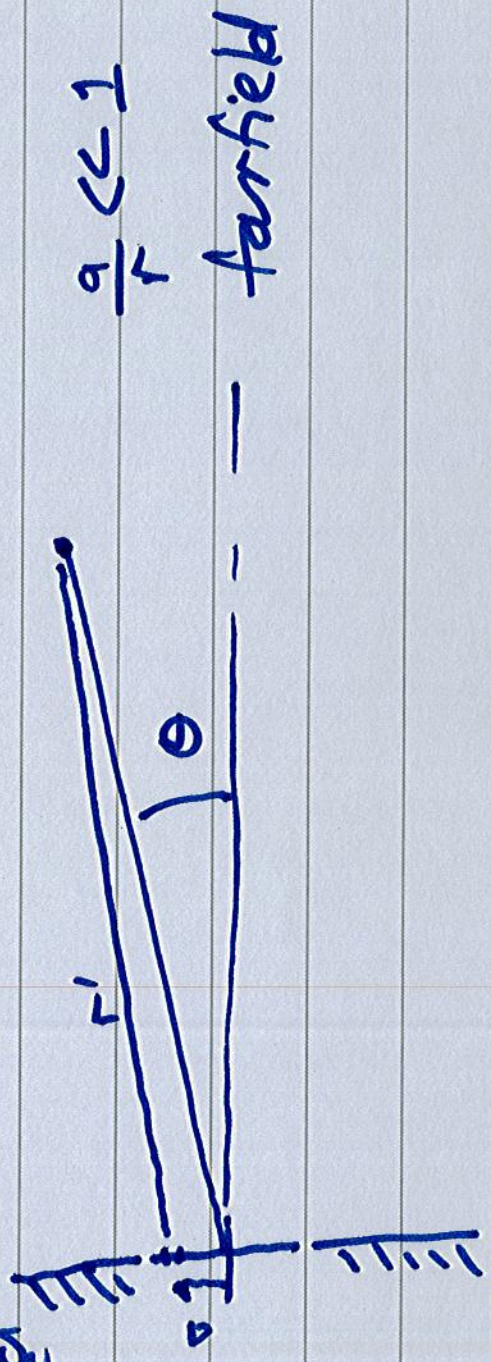
That can both

increase

& decrease



far field



- replace r' by r
- replace r' by $\sqrt{r^2 + a^2}$

$\approx r - a \sin \theta \cos \phi$

$$\tilde{P}(r, \theta) = \underbrace{j \frac{\rho_0 \epsilon}{2} U_0 \left(\frac{a}{r}\right)}_{\text{monopole}} e^{-i \text{tr}} \left[2 \frac{J_1(k a \sin \theta)}{k a \sin \theta} \right]_{\text{Directivity factor}}$$