

# Lecture #22

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# Graphs & Networks

- ❖ Subgraphs
- ❖ Graph coloring
- ❖ Activity networks
- ❖ Route problems
- ❖ Network flow
- ❖ Visibility graph problems
- ❖ Covering problems

# Project Management

- ❖ **Service organizations have to take on large, complex projects at some point**
  - ❑ **An airline opening new routes or pulling a jumbo jet out of service for major maintenance – large expenses if tasks are delayed**
  - ❑ **Department store – installing new inventory control system – lost sales and large ordering costs if timetables unmet**
  - ❑ **A hospital modernizing operating rooms**

# Project Management

- ❖ **Elements:**
  - ❑ **Planning**
  - ❑ **Scheduling**
  - ❑ **Control**
- ❖ **Aid to planning – work breakdown structure (WBS), which is a hierarchical tree – tasks required to achieve the objective**
- ❖ **Divides work into manageable components such as tasks, subtasks, and work elements**

# WBS

- 1.0 Move the hospital (Project)
  - 1.1 Move patients (Task)
    - 1.1.1 Arrange for ambulance (Subtask)
      - 1.1.1.1 Prepare patients for move
      - 1.1.1.2 Box patients personnel effects
  - 1.2 Move furniture
    - 1.2.1. Contract with moving company
      - 
      - 
      -

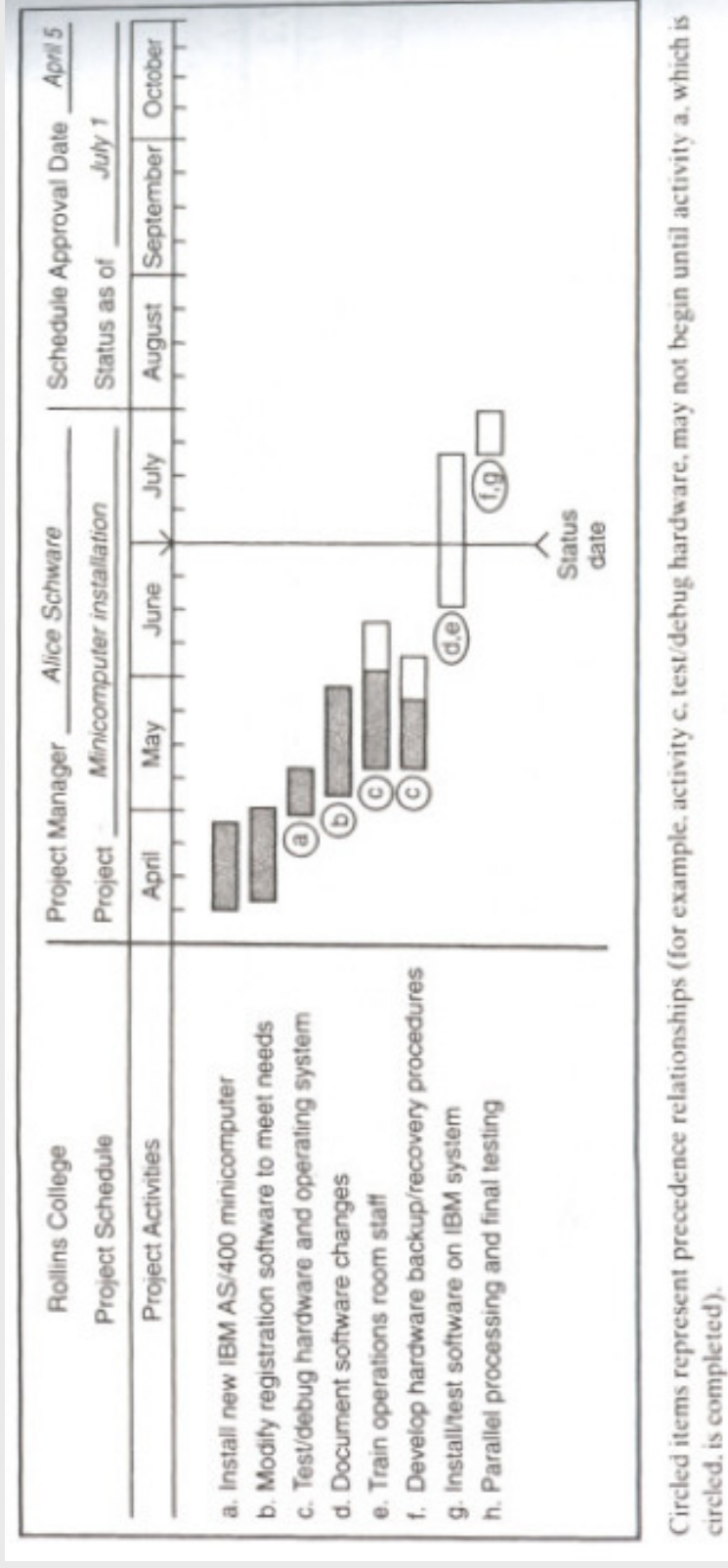
Fitzsimmons 2006

# Project Scheduling

- ❖ Project Scheduling: determine the project activities in the time sequence in which they have to be performed
- ❖ Materials and people needed at each stage of production are computed, and the time each activity will take is also determined

□ Gantt charts

# Gantt Chart



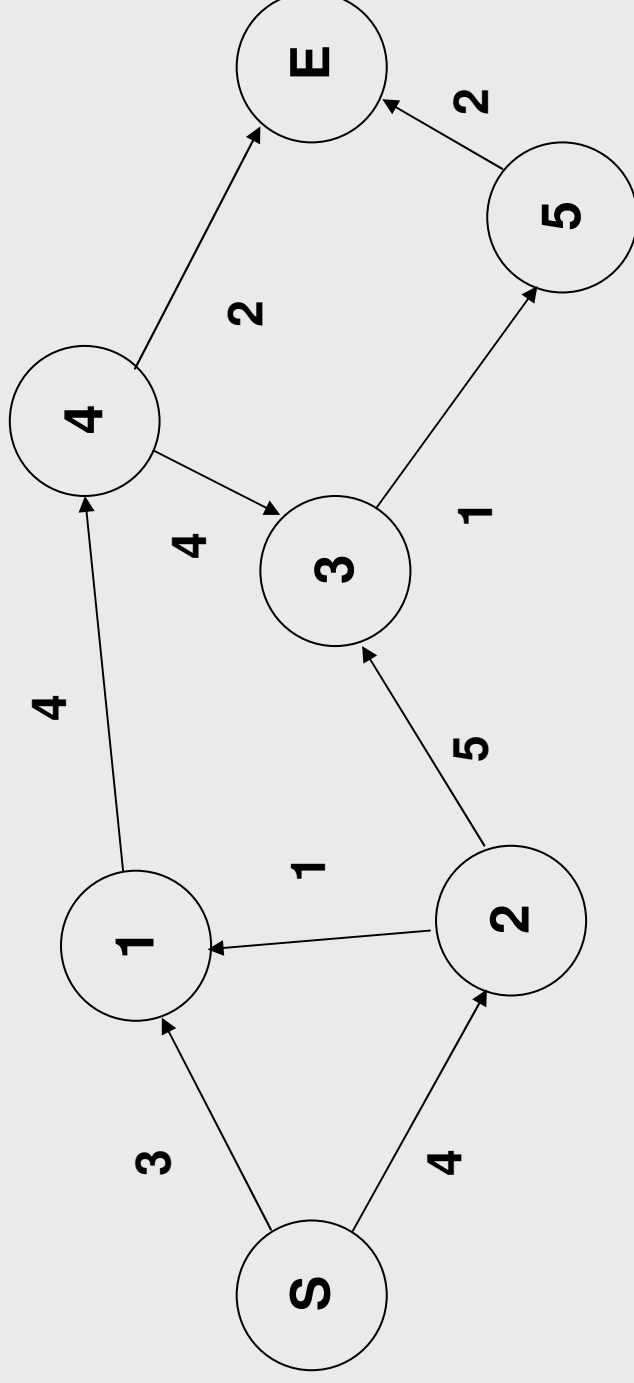
- ❖ Reflects time estimates and can be easily understood
- ❖ Horizontal bars for each activity
- ❖ Letters on left of each bar – activities that precede it

# Project Scheduling

- ❖ Gantt charts not easily updated
- ❖ Don't adequately illustrate interrelationships between activities and resources
- ❖ CPM (Critical Path Method) & PERT (Program Evaluation Review Technique) are two widely used network techniques – they have the ability to consider precedence relationships and interdependency of activities

# Activity Network

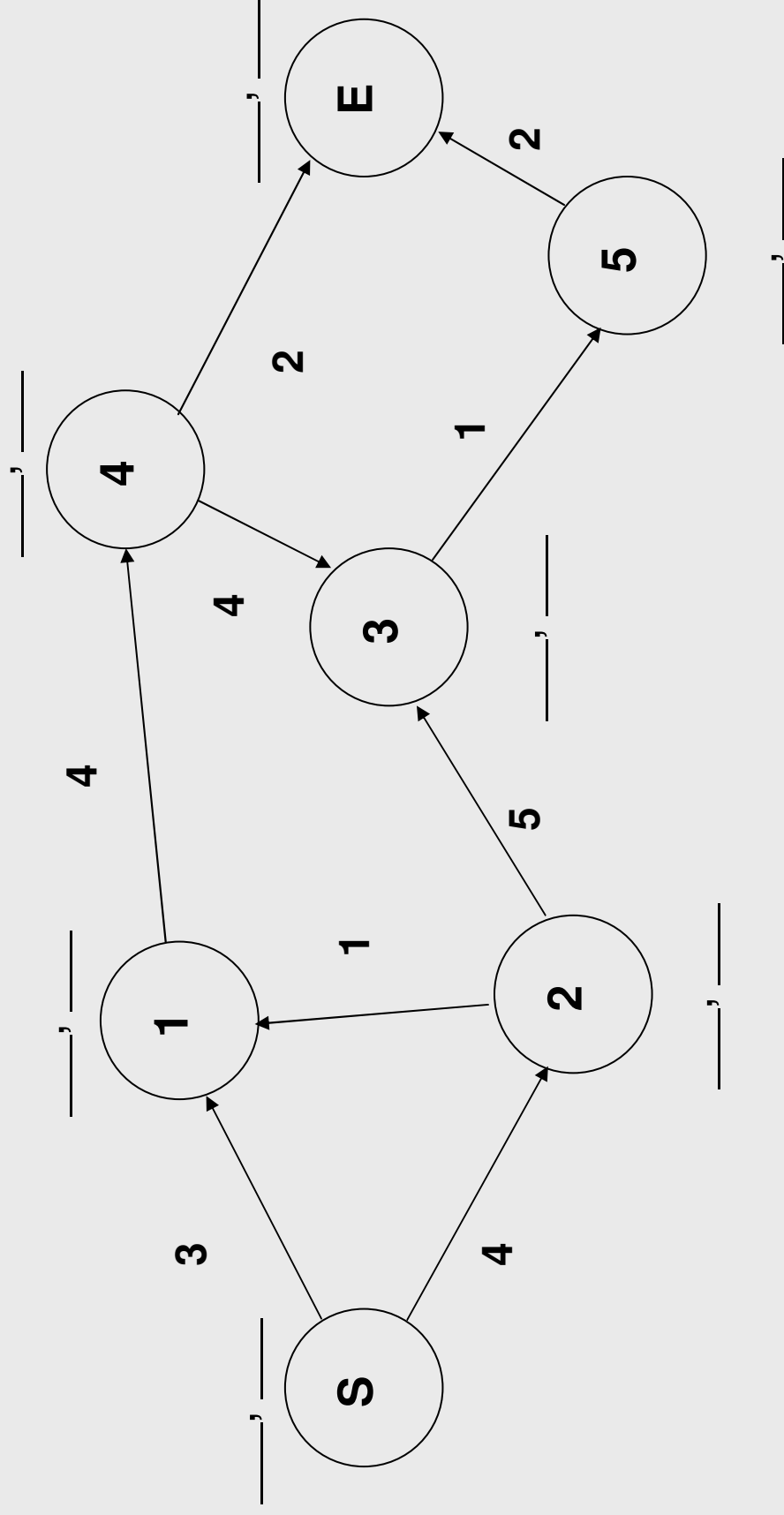
- ❖ Arcs – activities
- ❖ Nodes – events
- ❖ Event – requires completion all events



# Critical Path Method

- ❖ CPM is an approach to determine the start and finish dates for individual activities in a project
- ❖ A result of this method is the identification of a critical path, or chain of crucial activities throughout project

# CPM



# Critical Path Method

| Item              | Symbol | Definition                                                                                           |
|-------------------|--------|------------------------------------------------------------------------------------------------------|
| Activity duration | $t$    | The expected duration of an activity                                                                 |
| Early start       | $ES$   | The earliest time an activity can begin if all previous activities are begun at their earliest times |
| Early finish      | $EF$   | The earliest time an activity can be completed if it is started at its early start time              |
| Late start        | $LS$   | The latest time an activity can begin without delaying the completion of the project                 |
| Late finish       | $LF$   | The latest time an activity can be completed if it is started at its latest start time               |
| Total slack       | $TS$   | The amount of time an activity can be delayed without delaying the completion of the project         |

# Critical Path Method

|                                |                |     |
|--------------------------------|----------------|-----|
| $ES = EF_{\text{predecessor}}$ | $(max)$        | (1) |
| $EF = ES + t$                  |                | (2) |
| $LF = LS_{\text{successor}}$   | $(min)$        | (3) |
| $LS = LF - t$                  |                | (4) |
| $TS = LF - EF$                 |                | (5) |
| or                             | $TS = LS - ES$ | (6) |

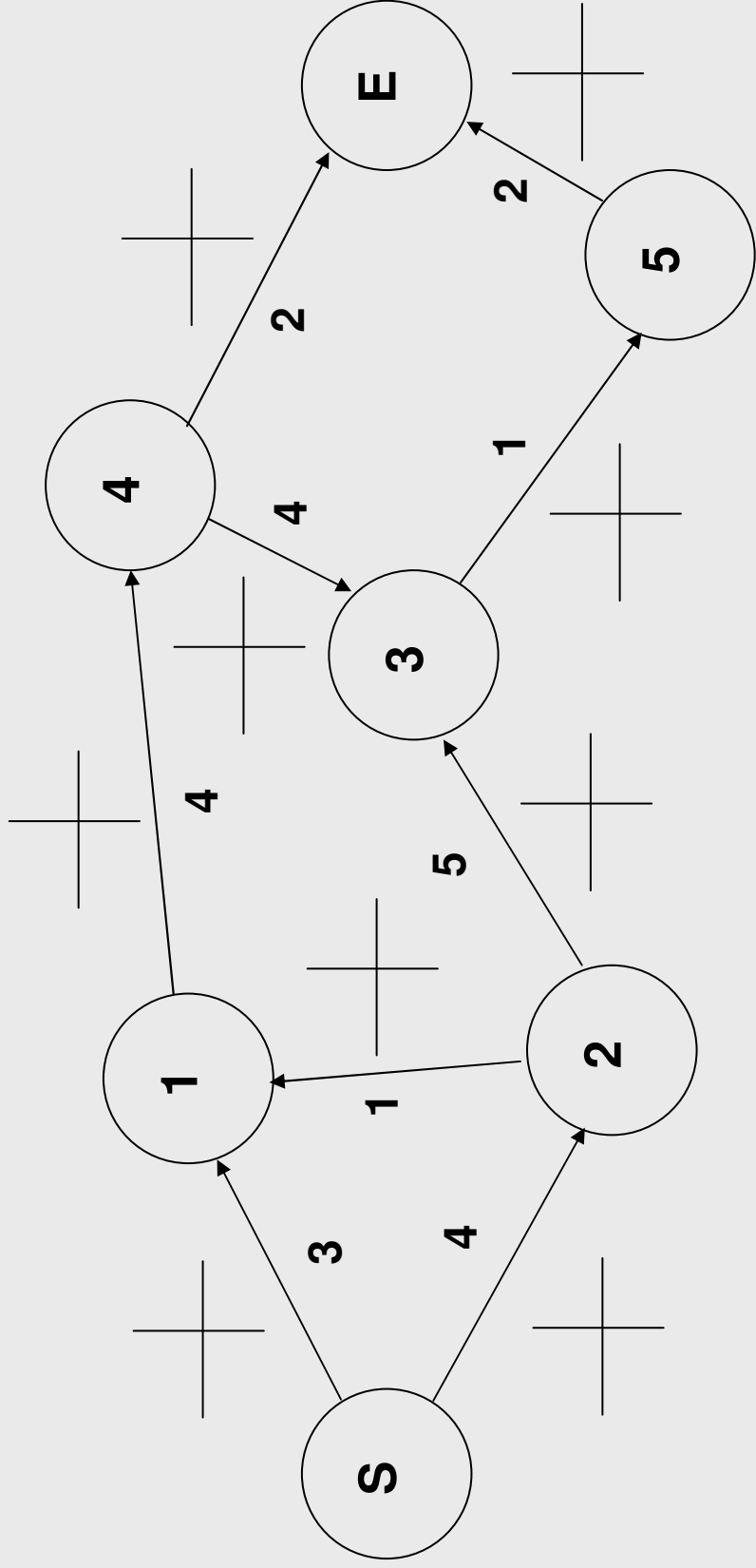
# More on CPM

❖ Associated with each activity is a cross to be filled in with the activity schedule times, which are calculated as follows:

$$TS = LS - ES$$

|    |    |
|----|----|
| ES | EF |
| LS | LF |

# More CPM



# More on Activity Networks

- ❖ In many cases  $t$  values are assumed to be deterministic (i.e., constant)
- ❖ In other cases, expected duration is mean of known probability distributions
- ❖ PERT Approach – Beta Dist.
  - ❑ 3 time estimates
  - ❑ Most likely time ( $M$ ), optimistic time ( $O$ ), and pessimistic time ( $P$ )
  - ❑ For each activity:  $\text{Mean} = (O + 4M + P) / 6$
  - ❑ For each activity:  $\text{Std Dev} = (P - O) / 6$
  - ❑ Add variances along path
  - ❑ End up with Mean and S.D. of Completion Time