

# Lecture #19

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# Quality - Reliability

- ❖ We already discussed some of the service quality dimensions.
- ❖ One of them is Reliability
- ❖ We will revisit Reliability today – how reliability of a product/service can influence the system performance

# Product vs. Service Reliability

## ❖ Product

- ❑ Refers to probability that product will perform intended function for specific period under specified conditions
- Probability that transmission system will not require a repair for 6 years when maintained according to guidelines.
- ❑ Many measures of reliability

# Product vs. Service Reliability

## ❖ Service

- ❑ Ability to perform the service dependably and accurately.
- Organization performs service right the first time and honors its promises.
- ❑ Examples include
  - Accuracy in billing
  - Keeping records correctly
  - Completing service as scheduled

# Reliability Indexes

- ❖ As experience is gained in quantifying reliability, many companies are learning that it is best to create an index that uniquely meets the needs of those who will use the index
  - ❑ Telephone system: Downtime of switching center should be a maximum of 24 hours per 40 years or 0.6 hour/year or 36 min/yr or about 0.1 min/day

# Reliability Goals

- ❖ **Setting overall reliability goals requires agreement on:**
  - ❑ **Reliability as a number**
  - ❑ **The environmental conditions to which the numbers apply**
  - ❑ **A definition of successful product/service performance**

# Reliability Quantification Process

- ❖ **Apportionment (or budgeting)**
  - Process of allocating reliability objectives among various elements that collectively make up a higher-level product/service.
- ❖ **Prediction**
  - The use of prior performance data plus probability theory to calculate the expected failure rates
- ❖ **Analysis**
  - Identification of the strong and weak portions of the design to serve as a basis for improvements, trade-offs, etc.

# Reliability Engineering Disciplines

- ❖ Reliability – time to failure
- ❖ Maintainability – time to repair
- ❖ Availability – relates to use time – includes fix time
- ❖ All three of these areas can be numerically quantified with the use of reliability engineering principles and life data analysis.

# Fundamental Concepts

- ❖ Probability density function (pdf),  $f(t)$ , associated with lifetime or time to failure of a unit that is of interest
- ❖  $F(t)$  denotes the probability that the unit fails before some time  $t$ , i.e. the cumulative distribution function or cdf, can be found by

$$F(t) = P(T \leq t) = \int_0^t f(x) dx$$

# Important Functions

## ❖ Reliability Function (or Survival Function)

- The probability that a unit survives to time  $t$ :

$$R(t) = P(T > t) = 1 - P(T \leq t) = 1 - F(t)$$

- The reliability function is always a decreasing function of time.

# Important Functions

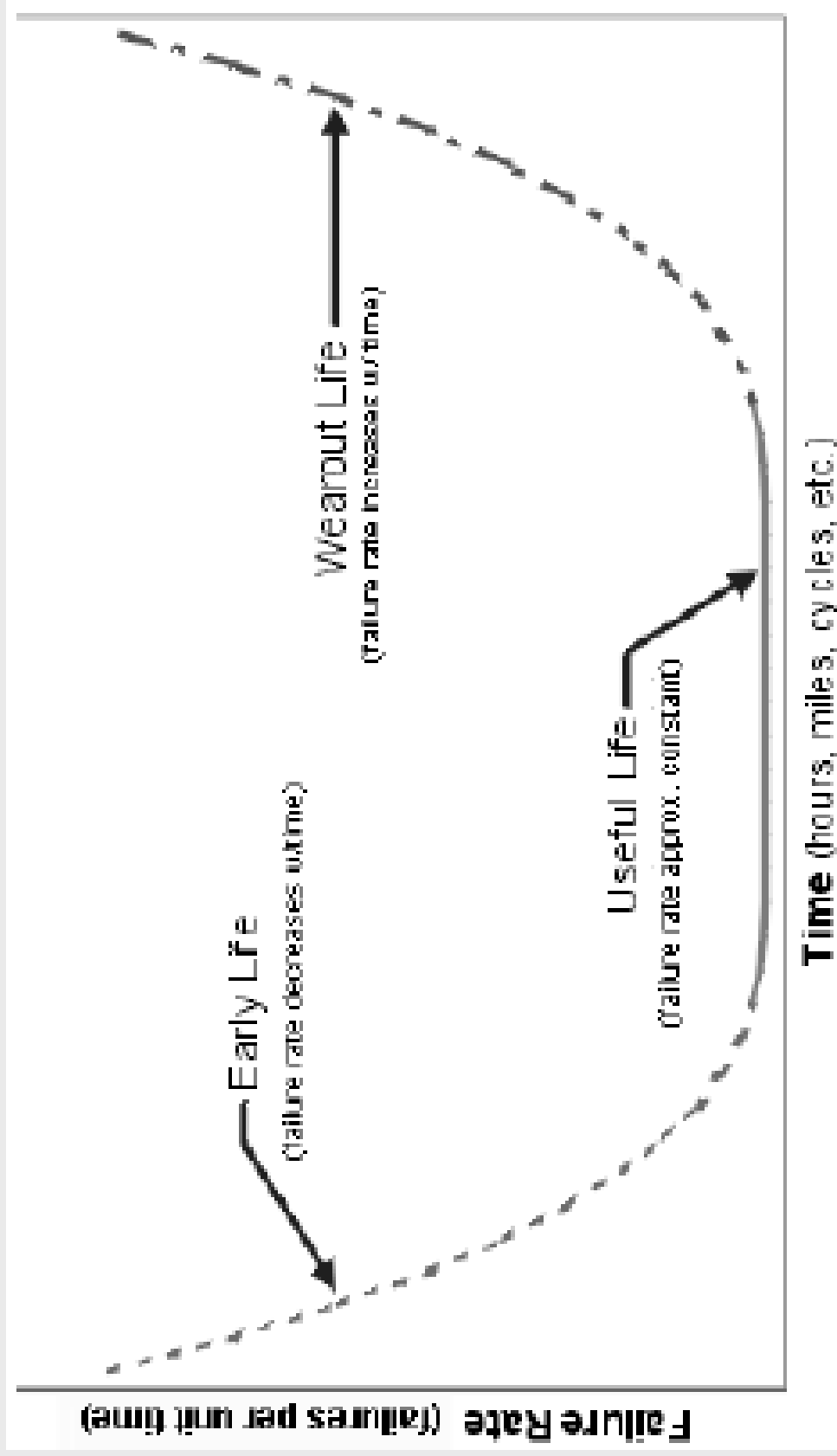
## ❖ Hazard Function

- The rate of failure of units,

$$h(t) = \frac{f(t)}{R(t)}$$

- $h(t)$  is the hazard or instantaneous failure rate function. It indicates the proneness to failure or risk of failure of a unit after time  $t$  has elapsed.

# Important Functions



# Important Functions

- ❖ Mean Time Between Failures (MTBF)

$$MTBF = \int_0^{\infty} tf(t)dt, \text{ or } MTBF = \int_0^{\infty} [1 - F(t)]dt$$

- ❖ Average or expected lifetime of an item.  
Frequently used

$$MTBF = \int_0^{\infty} R(t)dt$$

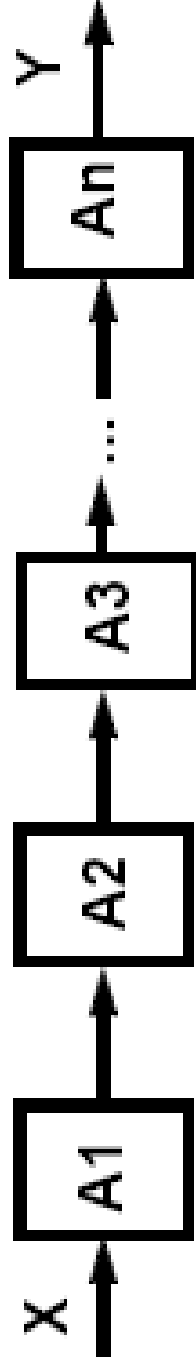
- ❖ Most commonly expressed in terms of  
reliability fcn.

# System Reliability

## ❖ Consider components

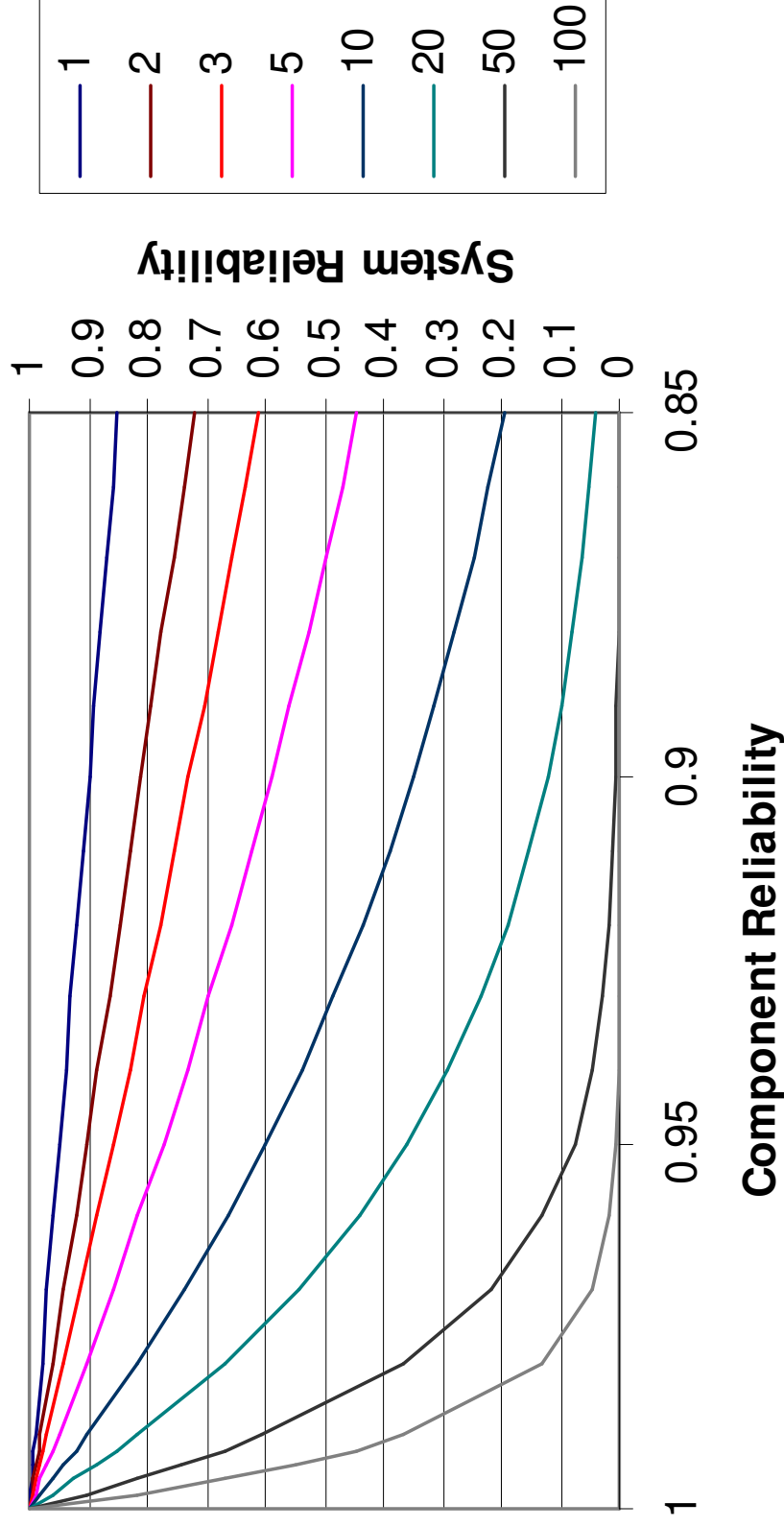
- ❑ In Series
- ❑ In Parallel
- ❑ Combination of Series and Parallel

# Series System

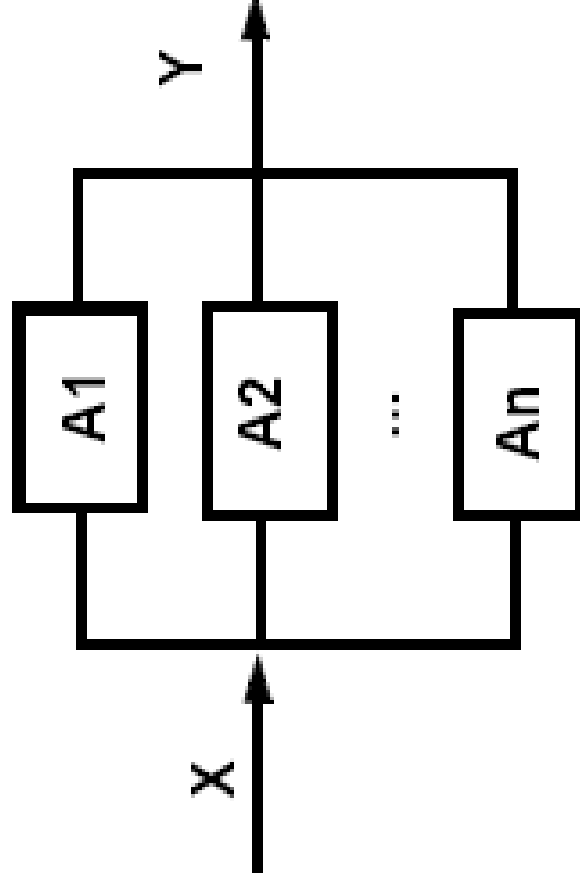


$$R_{system} = \prod_{i=1}^n R_i$$

$R_i$  is probability component  $i$  will survive for design life.



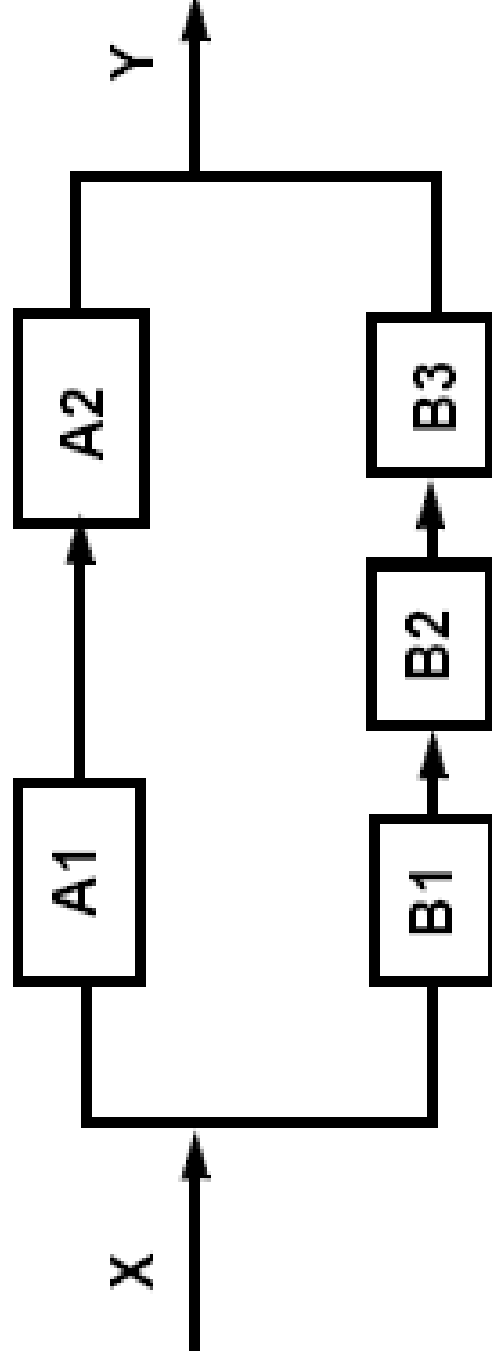
# Parallel System



$$R_{system} = 1 - \prod_{i=1}^n (1 - R_i)$$

# Mixed System

Example:



$$R_{system} = 1 - (1 - R_{A1A2}) \times (1 - R_{B1B2B3})$$

$$R_{A1A2} = R_{A1} \times R_{A2} \quad R_{B1B2B3} = R_{B1} \times R_{B2} \times R_{B3}$$

# System Reliability Example

- ❖ Pyzdek (1994) discusses the design of an ambulance service to handle emergency calls
- ❖ It is developed on a reliability block diagram for the rescue system
  - The reliability of the system is  $(0.998)(0.999) \dots (0.994) = 0.9195$ ; i.e., the system would succeed in its mission about 92 % of the time.

# Emergency Rescue System

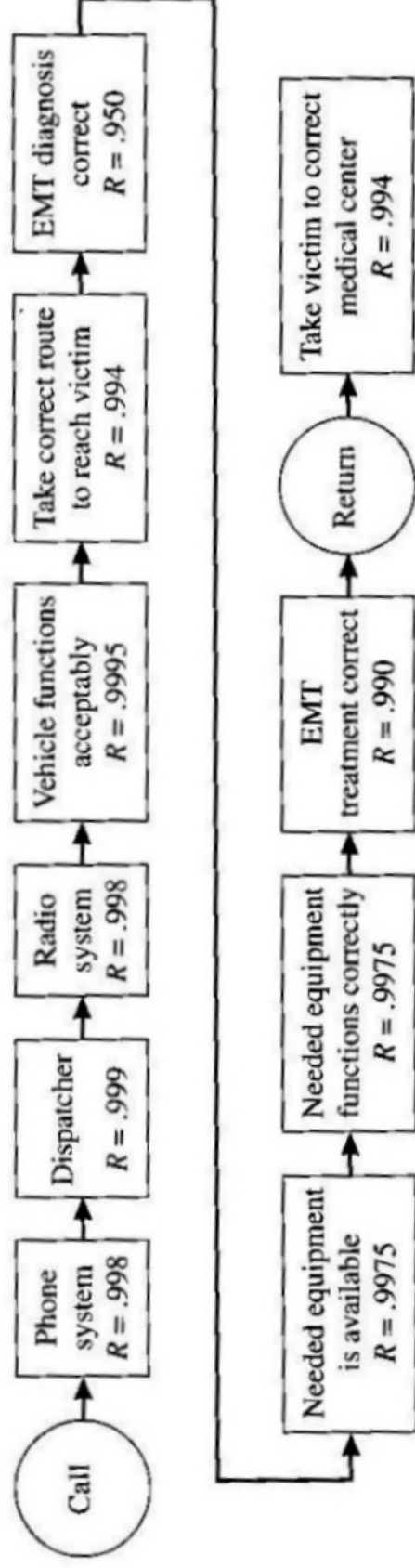


FIGURE 14.4

Reliability block diagram of emergency rescue system. (Reprinted with permission by the ASQ.)

Gryna 2001

# Predicting Reliability during Design

- ❖ **Define the product and function**
  - **The system, subsystems, and units must be precisely defined in terms of their functional configurations and boundaries**
- ❖ **Prepare a reliability block diagram**
  - **For systems in which there are redundancies or other special interrelationships among parts**
- ❖ **Develop the probability model**
  - **A simple model may only add failure rates; or a complex model can account for redundancies and other conditions**

# Predicting Reliability during Design

- ❖ Collect information relevant to part reliability
- ❖ Select parts reliability data
- ❖ Combine all of the above to obtain numerical reliability prediction

# More on Predicting Reliability...

- ❖ Based on the exponential distribution
- ❖ Based on the Weibull distribution
- ❖ As a function of applied stress and strength.

# Failure Modes & Effects Analysis (FMEA)

- ❖ Important tool for predicting and analyzing reliability
- ❖ Evolved at NASA – where interest in preventing failures is extremely high
- ❖ Later popularized by automotive industry.
- ❖ Now routine in many organizations

# Failure Modes and Effects Analysis

- ❖ FMEA is a system for analyzing the design of a product or service system to identify potential failures, then taking steps to counteract or minimize the risk of failure
- ❖ The FMEA process begins by identifying “failure modes”, the ways in which a product, service, or process could fail
- ❖ A project team examines every element, starting from the inputs and working through to the output delivered to the customer

# Failure Modes – truck stop coffee

- ❖ One of the inputs to process is “clean coffee pot.” What could go wrong? Water in the dishwasher is not hot enough, so pot is not cleaned
- ❖ First step in process is to fill the brewing machine with water. What could go wrong? Perhaps water is not the right temperature or too much/little water is added
- ❖ Output from process is hot cup of coffee delivered to the customer. What could go wrong? Coffee could cool before it is served.

# RPN

- ❖ RPN = Risk Priority Number
- ❖ All failures are not the same
- ❖ Being served a cup of coffee that is just hot water is much worse than being served a cup that is just a bit too cool.
- ❖ A key element of FMEA is analyzing three characteristics of failures:
  - ❑ How severe they are
  - ❑ How often they occur
  - ❑ How likely it is that they will be noticed when they occur.

# More on RPN

❖ Typically, the project team scores each failure mode on a scale of 1 to 10 or 1 to 5 in each of the three areas, then calculates a Risk Priority Number:

$$\square \text{RPN} = (\text{Severity}) \times (\text{freq. of occurrence}) \times (\text{likelihood of detection})$$

# FMEA

- ❖ Idea is to focus improvement efforts on the failures that have the biggest impact on customers
- ❖ Highest scoring failure modes are those that happen frequently, are bad when they happen, and/or are difficult to detect.
- ❖ Difficult-to-detect errors – more likely to get through to customers

# More on FMEA

- ❖ Team completes FMEA analysis for highest-scoring failure modes and for the highest severity scores
- ❖ Want to make sure possible disasters are prevented – even if they are unlikely to occur
- ❖ “Completing the analysis” means:
  - ❑ Looking at potential causes for error mode
  - ❑ Identifying ways to detect the problem
  - ❑ Developing recommended actions
  - ❑ Assigning responsibility for monitoring the process and taking action when warranted