

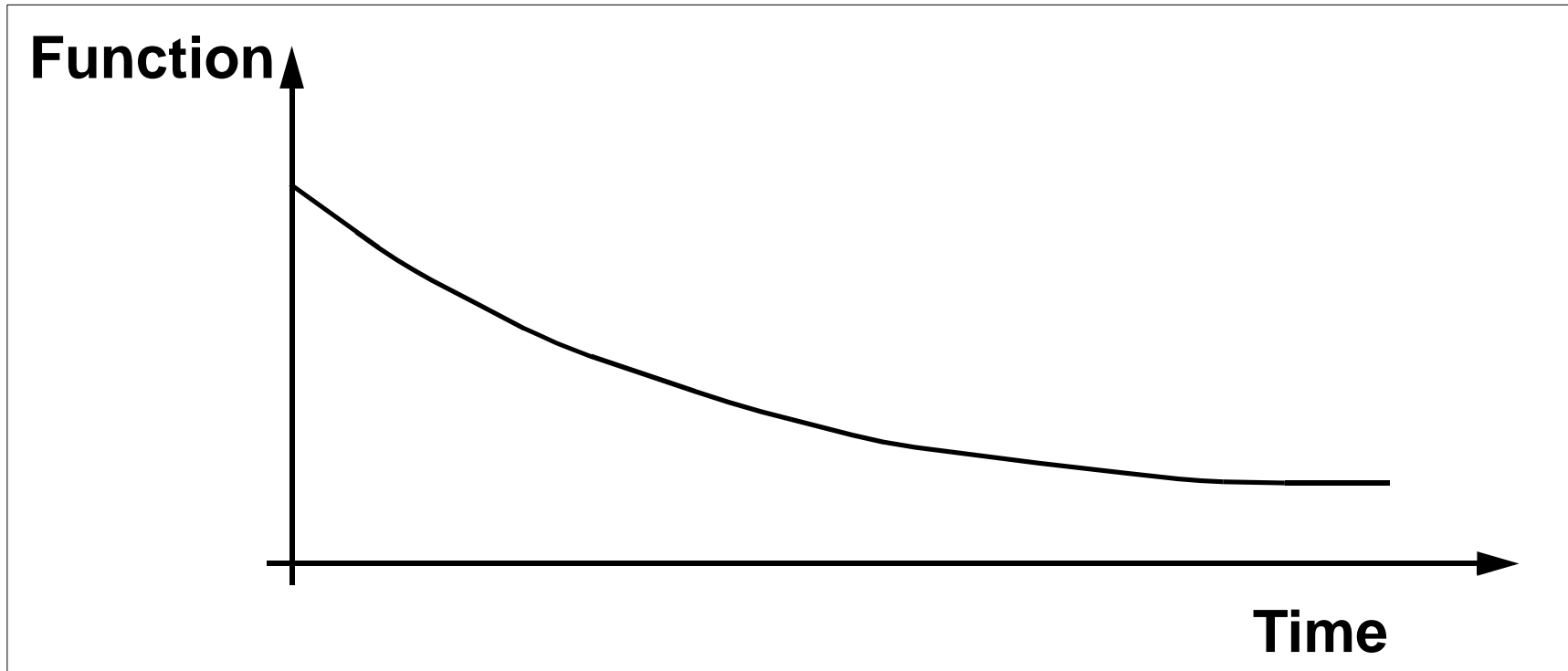
# Lecture #14

## ERDM

**Prof. John W. Sutherland**

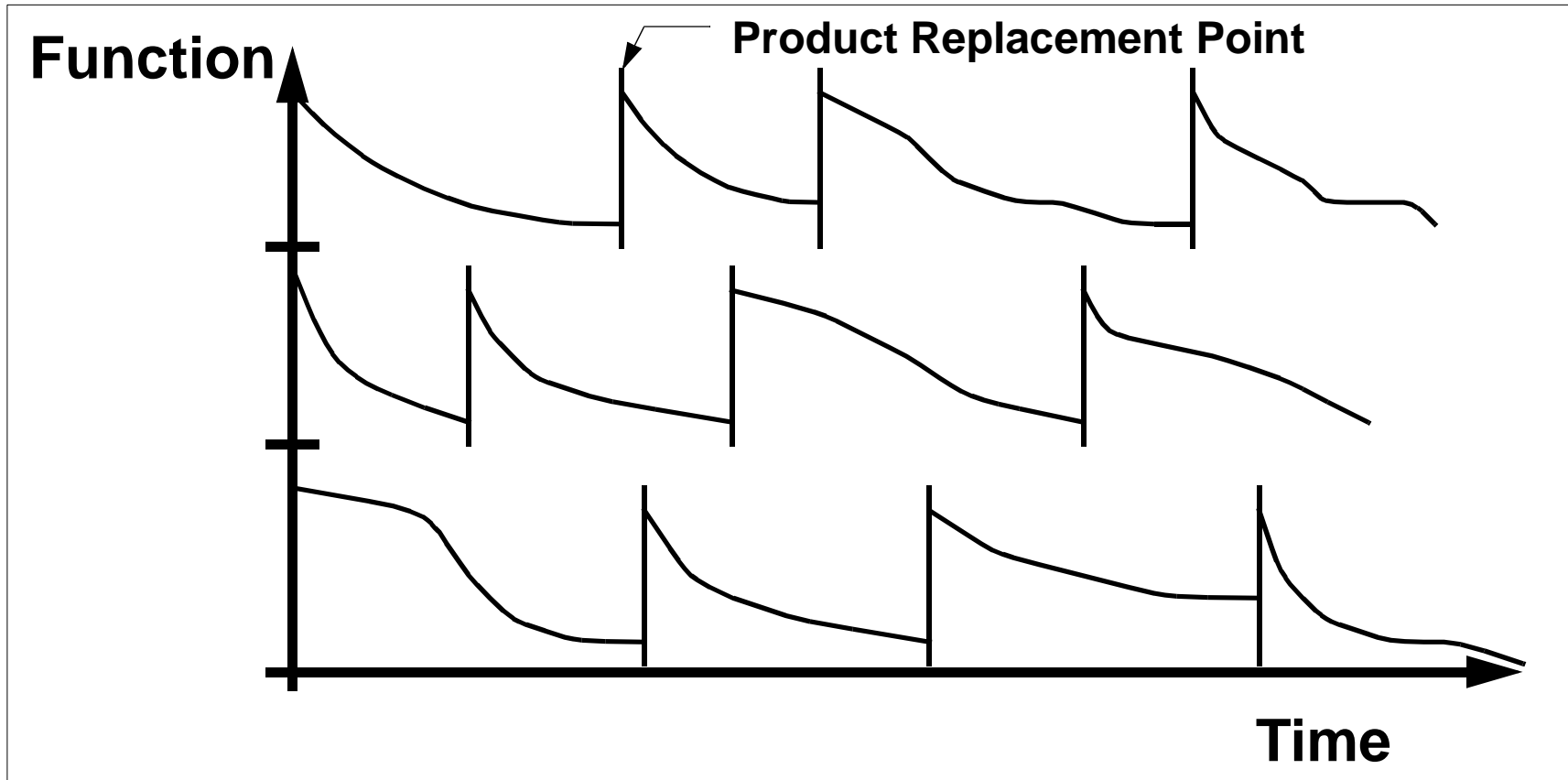
**Feb. 11, 2004**

# Product Function



**We observe that prod. function deteriorates over time.**

# Product Function



**Multiple products - multiple use cycles -- how to handle?**

# Background

In defining the course syllabus, several areas immediately evident:

- Design
- Manufacturing
- Life Cycle Issues

Several topics important (building blocks) but not covered elsewhere:

- Statistical issues
- Multi-criteria decision-making
- Optimization

# Objective

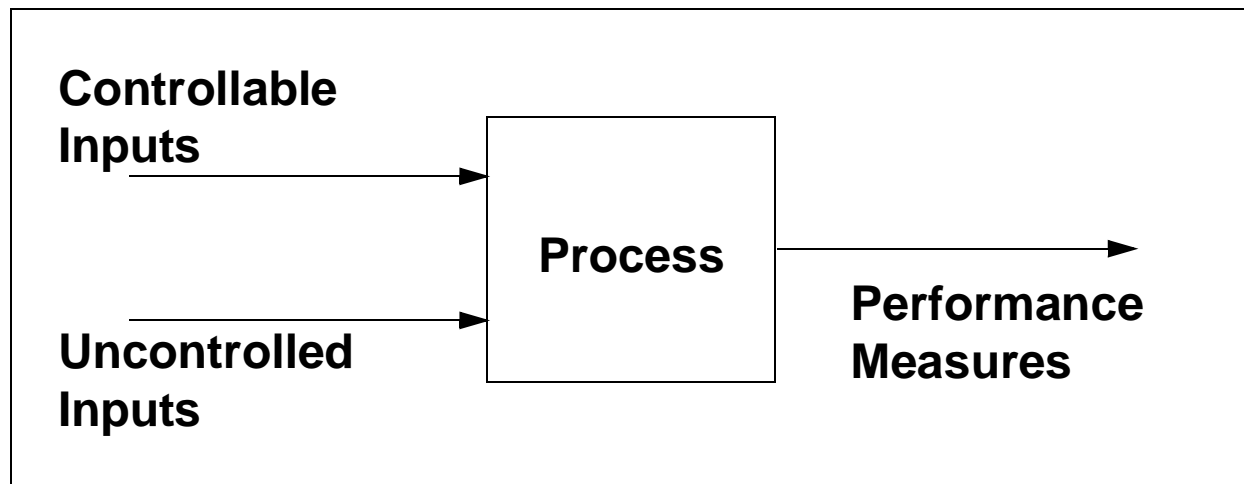
**Introduce basic concepts related to the origin, treatment, and characterization of variation.**

- **Origin and types of variation**
- **Quality (SPC & DOE)**
- **Reliability**

**A future class will tie many of these topics to “the environment”**

# Introduction

- Consider block diagram for a manufacturing process



- Performance measures (outputs) from the process may include: Part dimensions, surface finish, machine power, tool life, shrinkage, etc.

# Introduction (cont.)

**We often evaluate the success of the process by comparing these measures to desired values.**

- **The controllable inputs are variables that we suspect have a strong influence on performance. These include: cutting conditions, tooling, barrel temperature, operator actions, etc.**
- **The uncontrollable inputs are often assumed to have little or no effect on performance. Examples are: vendors, machine maintenance, material inhomogeneities, etc.**

# Degree-of-Control

- **Process inputs: either controllable or uncontrollable.**
- **Distinction is restrictive - most input variables fall somewhere in between. Machine settings (controlled variables) vary from their nominal values and are thus somewhat uncontrollable.**
- **Often variables could be controlled if we wished to.**
- **The amount of control (degree-of-control) we wish to exercise is an economic decision - increased control carries with it an economic price tag.**

# Variation

**The block diagram structure shown previously can be used to describe either process or product performance. Focus, for now, on process behavior.**

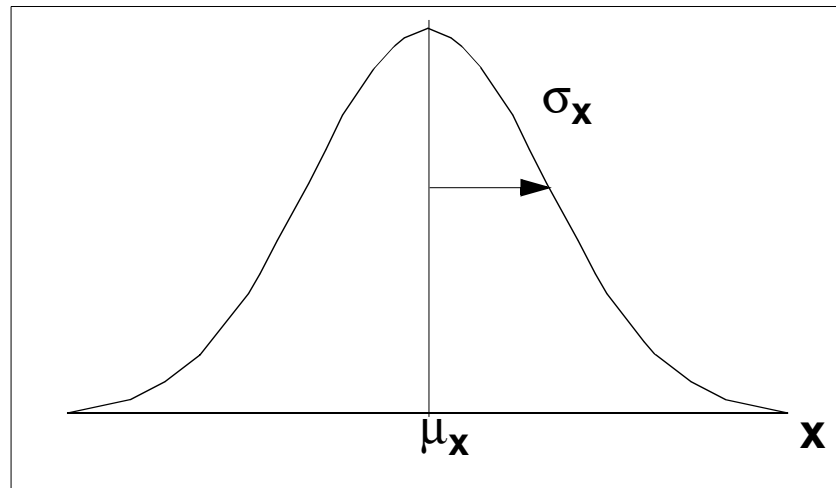
**When variables are not controlled, they change or vary. Variations in process inputs produce variations in the process output.**

**Thus, uncontrolled process inputs produce manufacturing variation.**

# Manufacturing Variation

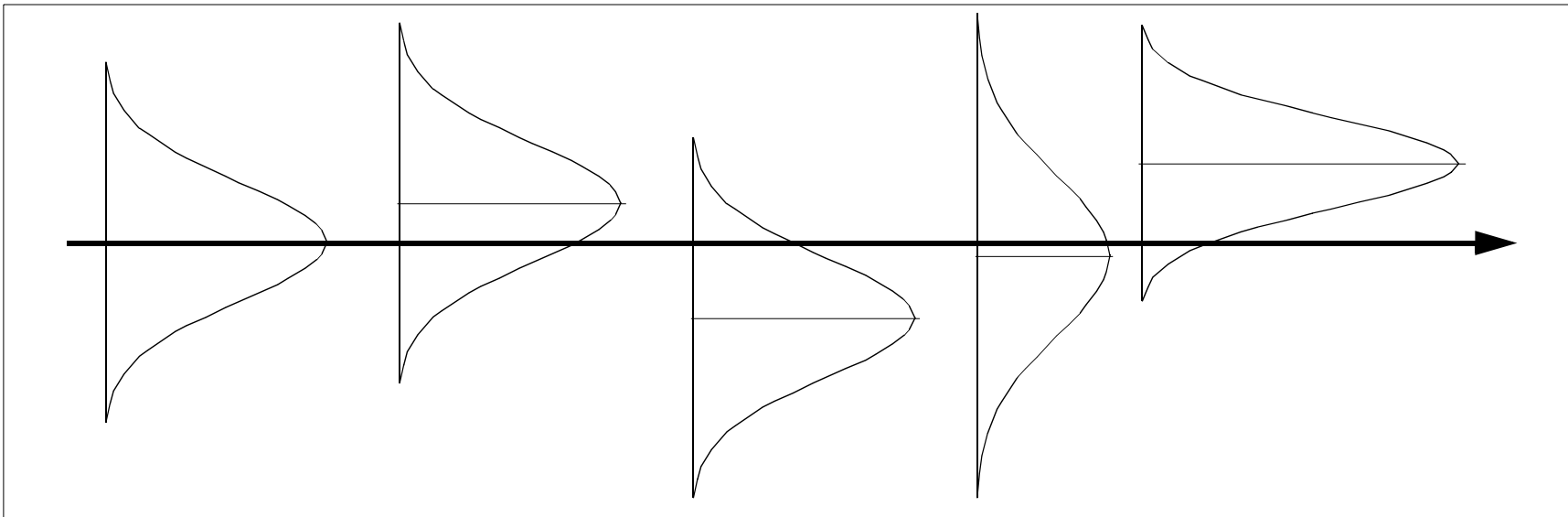
Broken down into two categories:

- **Common causes (Deming):** sources of variation that influence every product. Define the system (system faults). Chronic problems (Juran). Mgmt. responsible

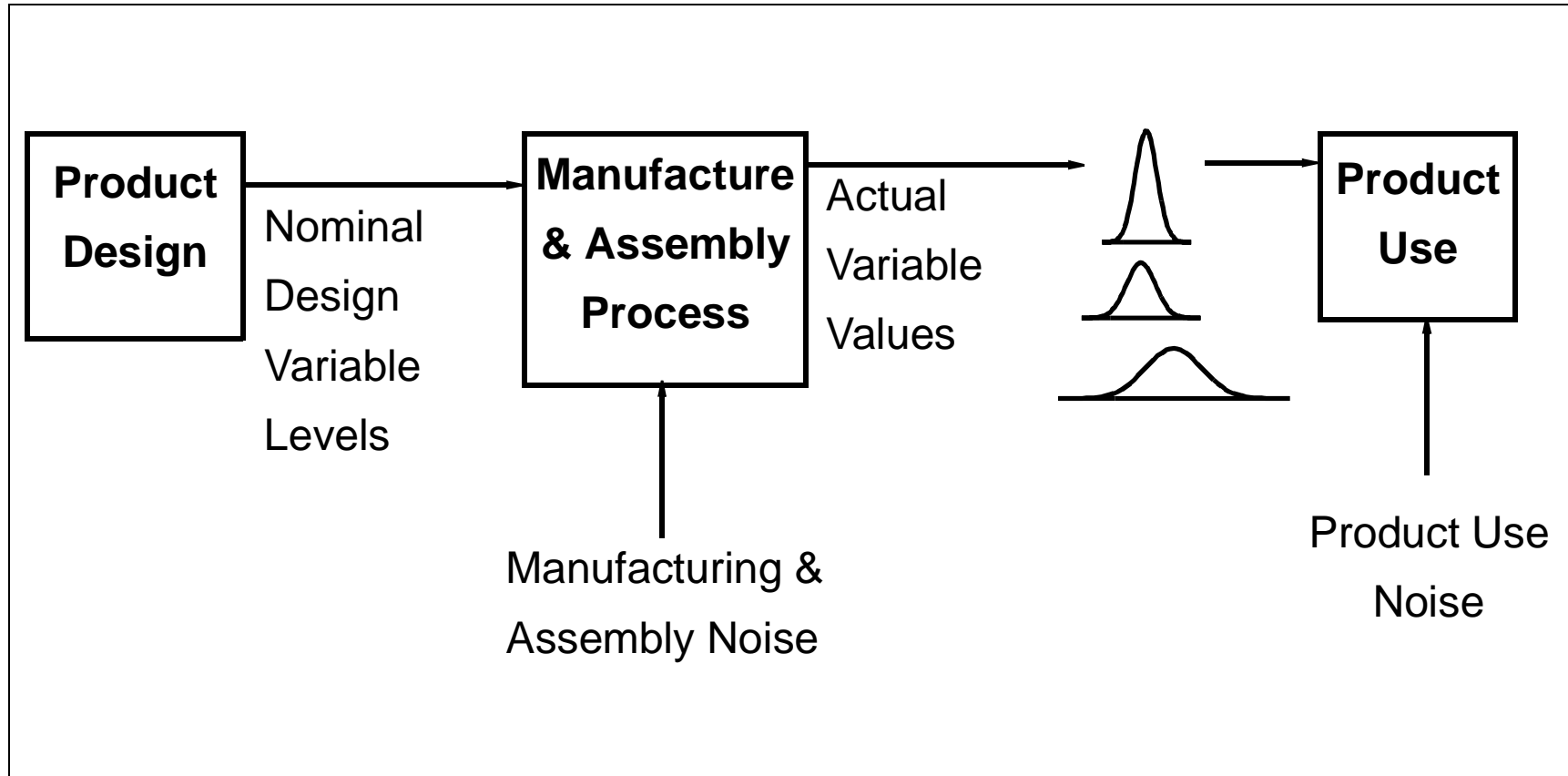


# Manufacturing Variation (cont.)

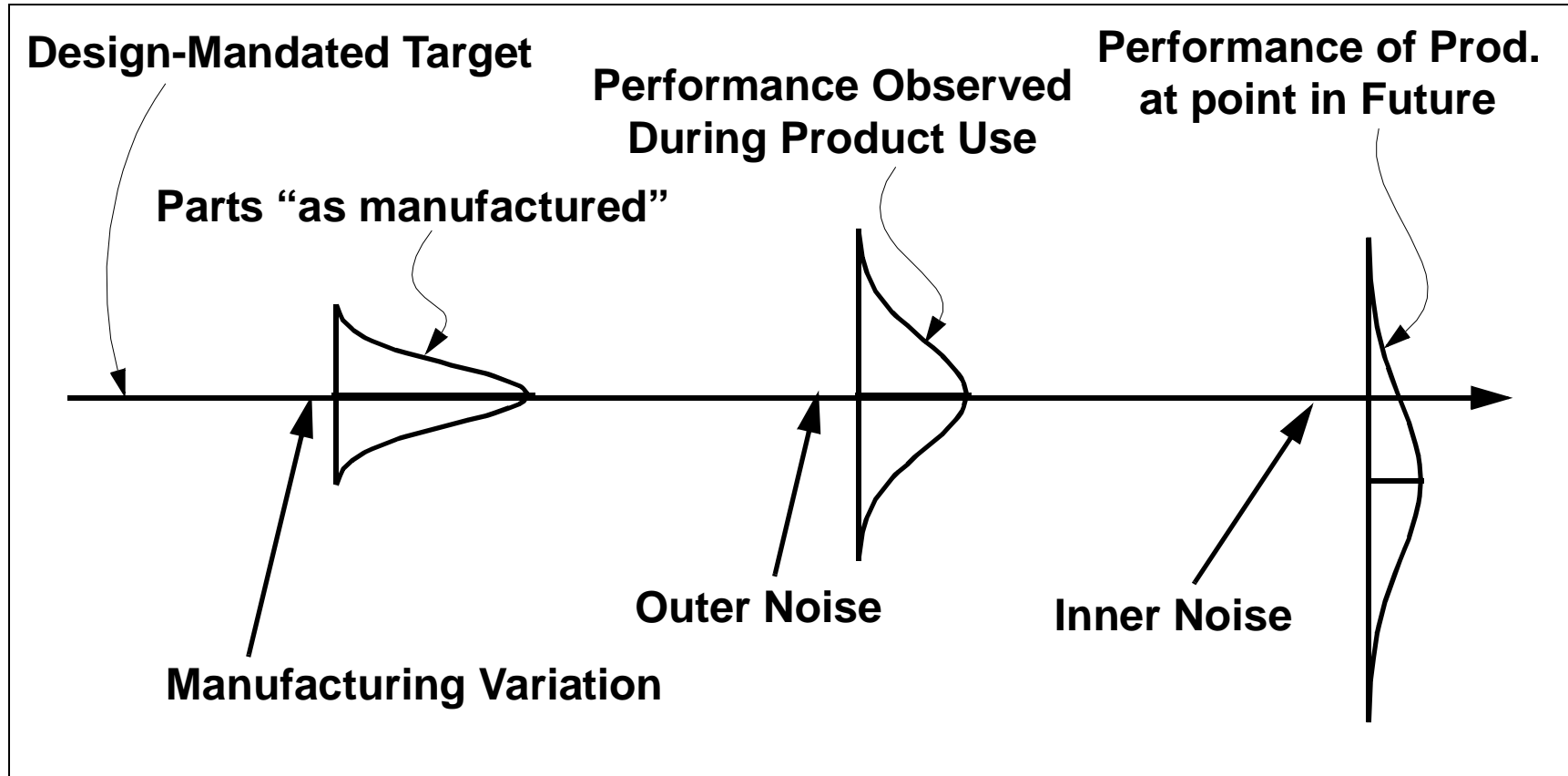
- **Special causes (Deming):** sources of variation that arise unpredictably - influence some of the parts. Also referred to as local faults. Sporadic problems (Juran). Often correctable locally at the process.



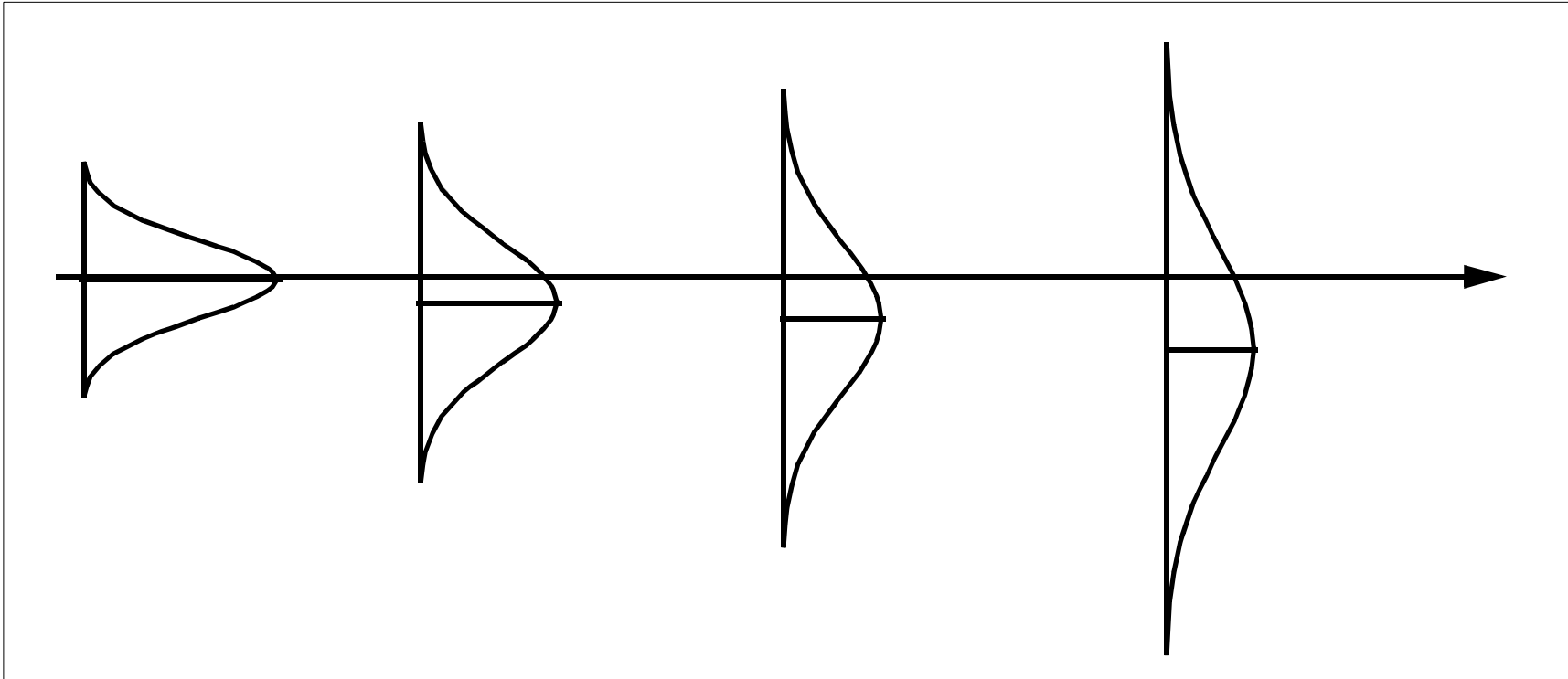
# Product Performance Variation



# Product Performance Variation (cont.)



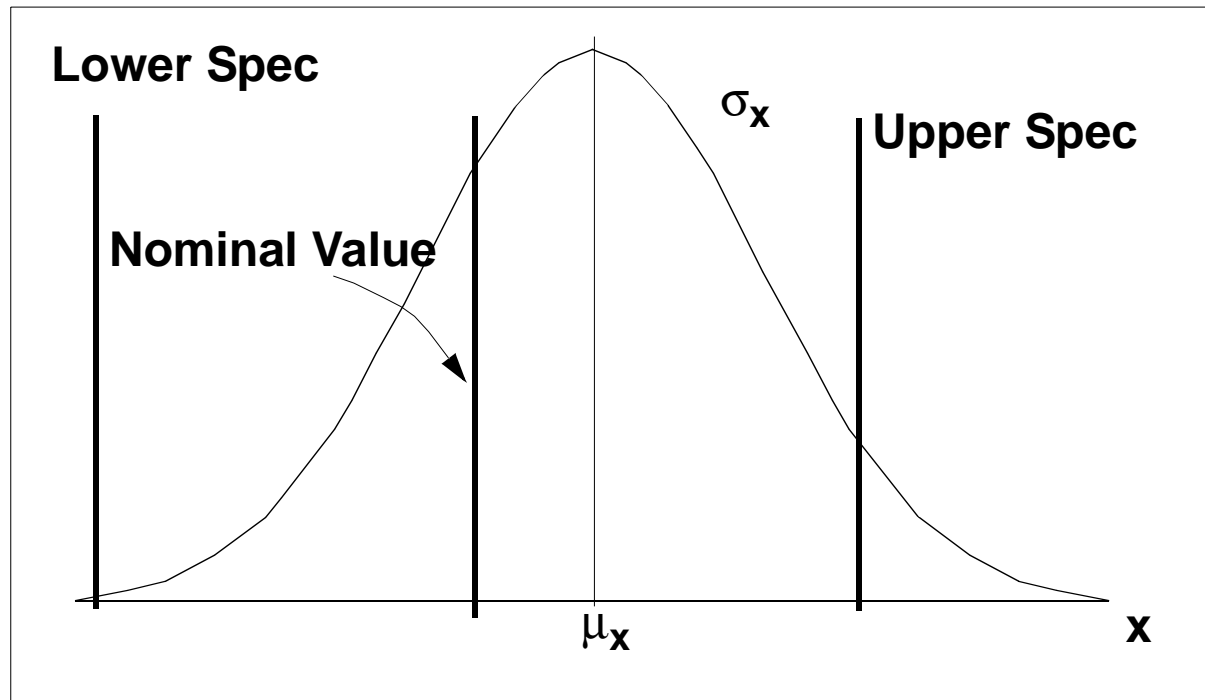
# Effect of Wear and Aging



**Process mean and variability change over time.**

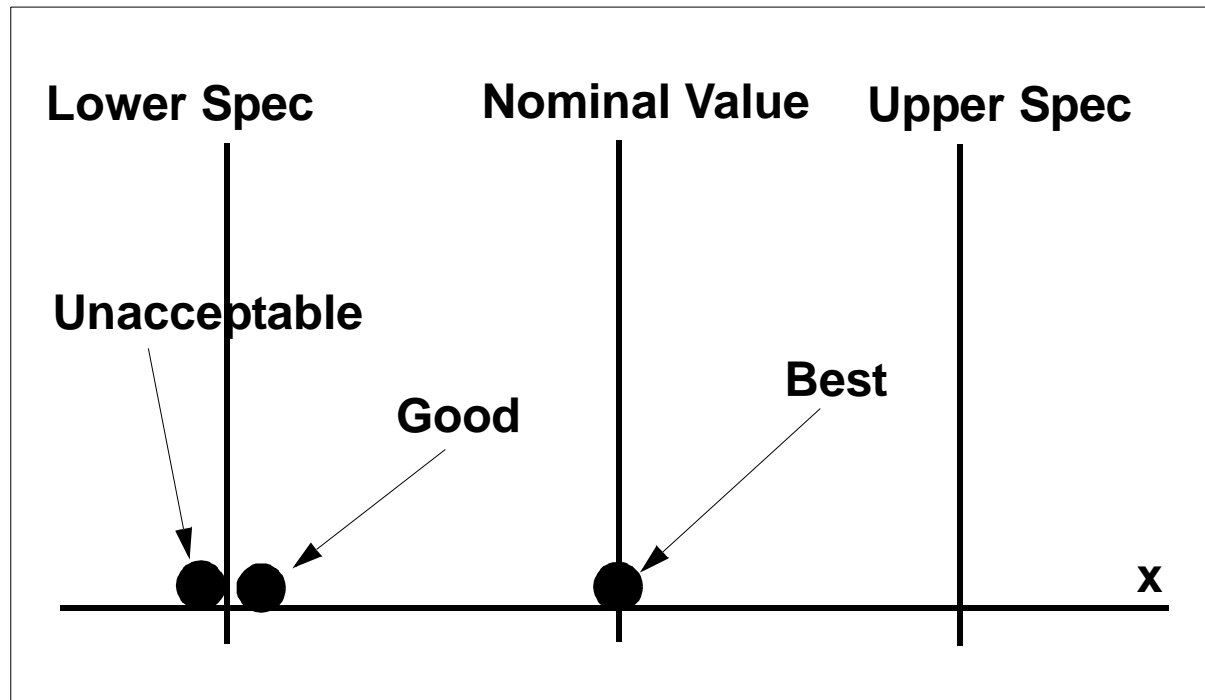
# Quality

Traditionally defined as conformance to engineering specifications.



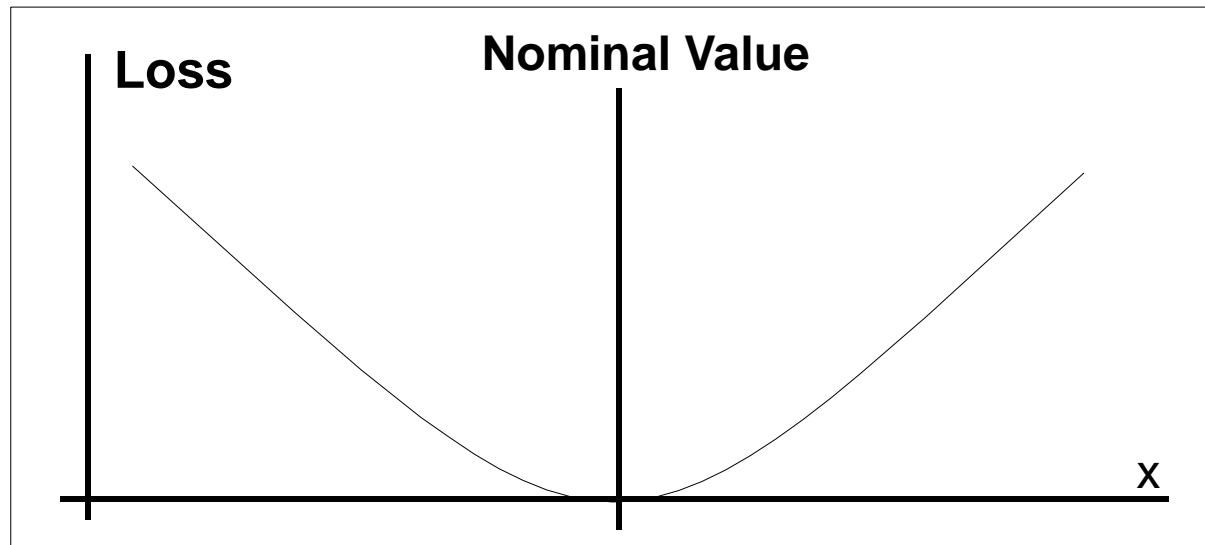
# Quality (cont.)

Traditional definition of quality does not promote notion of never-ending improvement.



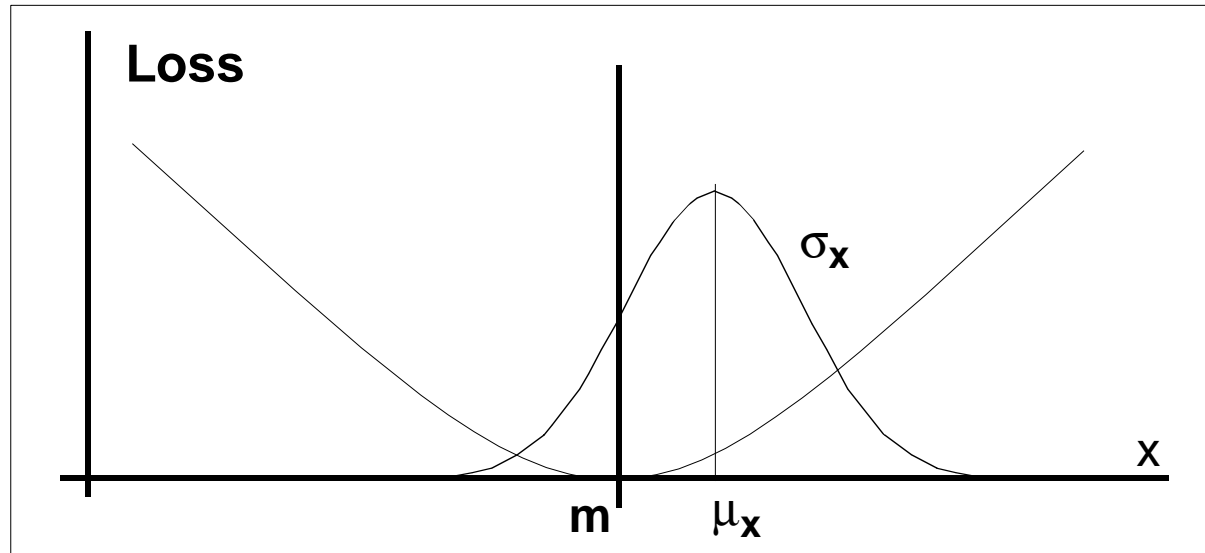
# Loss Function

Taguchi advocates the use of a loss function to characterize quality. Quadratic form:



$$L = k(x - m)^2$$

# Expected Loss



Since the characteristic  $X$  is a random varb., loss is also a random varb. - characterizes “average” loss

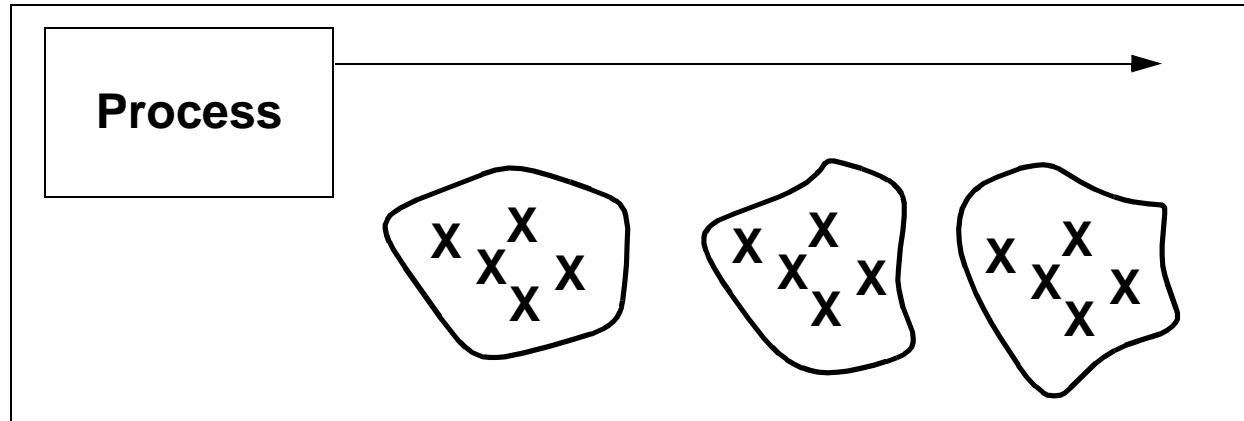
$$E[L(X)] = k \left[ (\mu_x - m)^2 + \sigma_x^2 \right]$$

# SPC and DOE

**Two widely used statistical approaches for improving the process.**

- **SPC - Is process stable (predictable, consistent, “in-control)? i.e., free of special causes. Control charts help us identify whether local faults are present.**
- **DOE - Study how a set of variables influence a performance response of interest. What must be done to move a process to a given target value?**

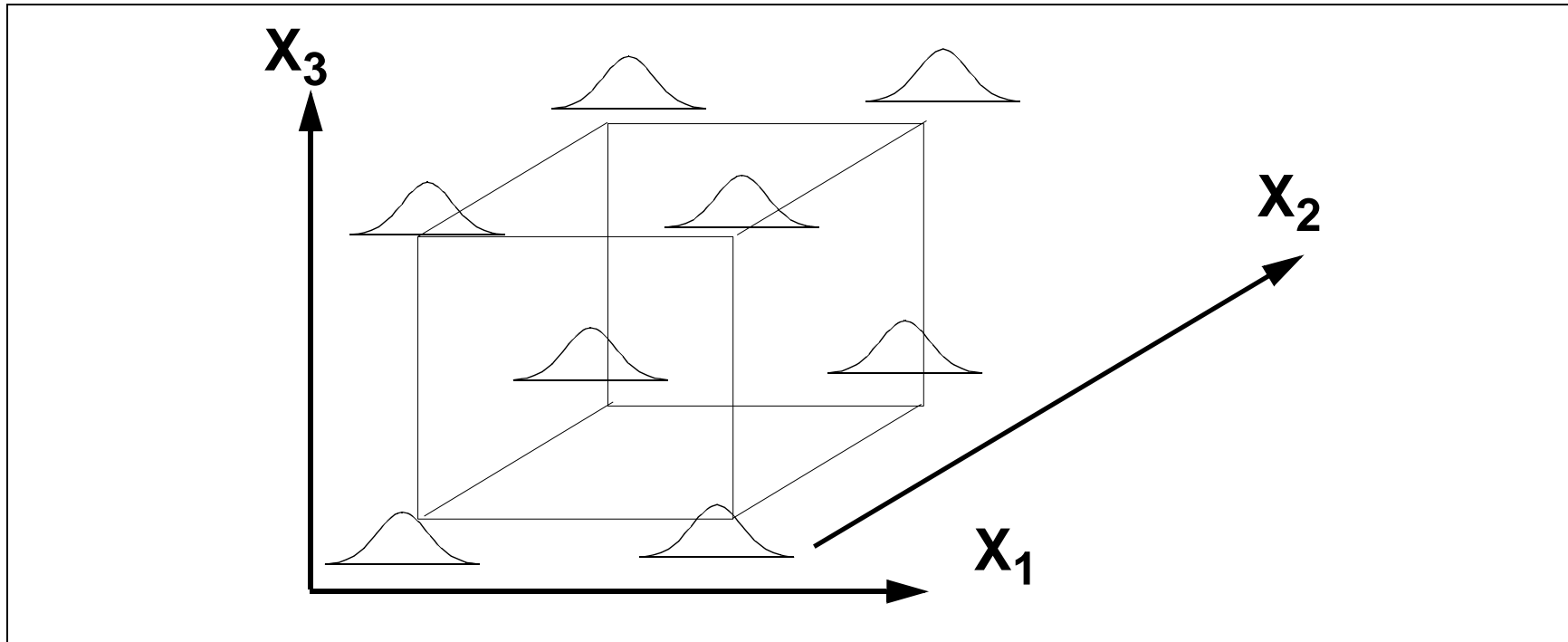
# SPC - Control Charts



**Samples are collected from the process - use this data to characterize process**

**For each sample calculate a sample mean and a sample range - plot values versus time**

# DOE - Designed Experiments

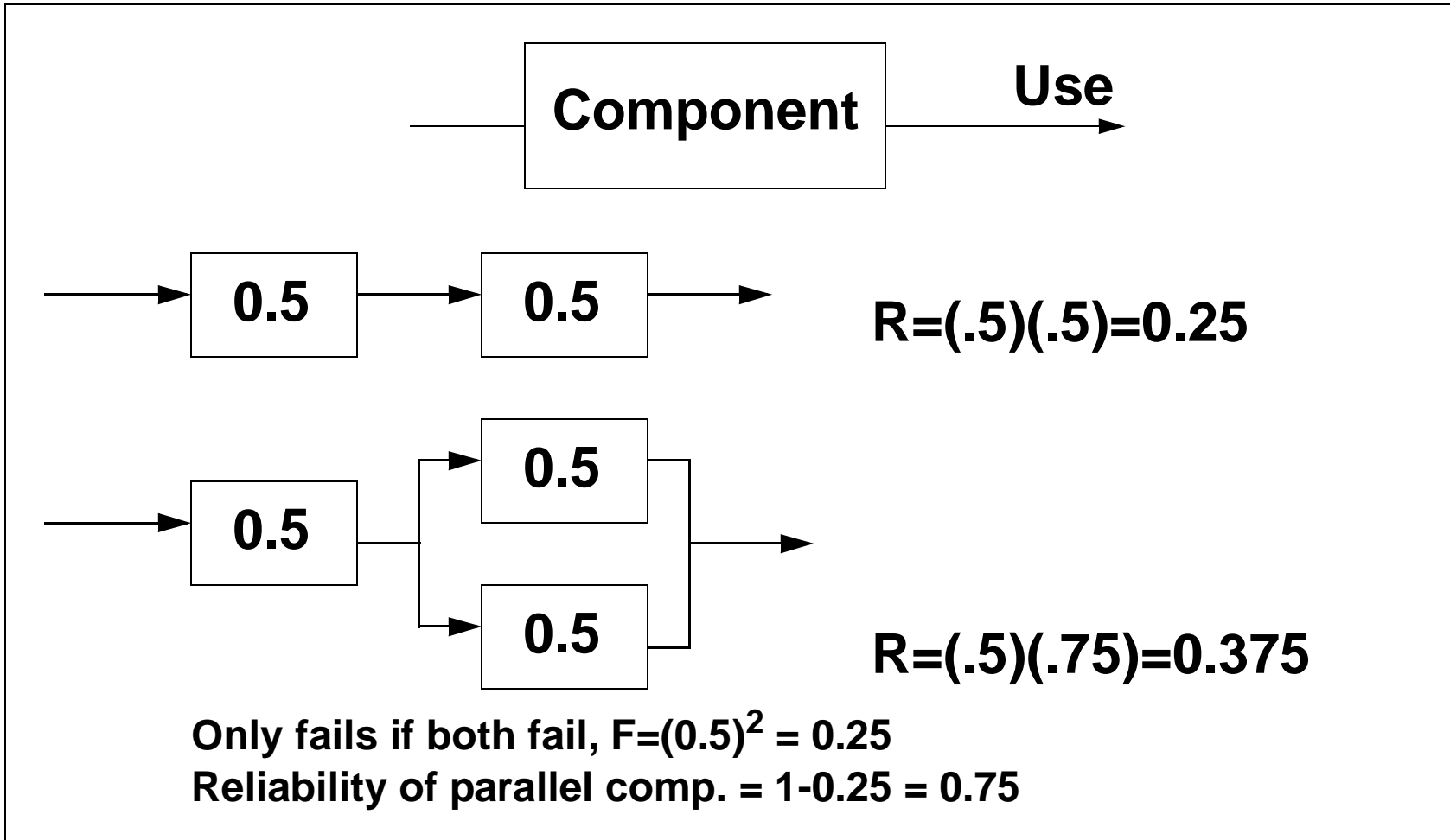


**Calculate the effect that each variable has on the process mean and variability (interactions as well).**

# Modern Quality Principles

- **Never-ending (continuous) improvement**
- **Variation reduction leads to cost reduction and quality improvement (SPC, DOE)**
- **Employ Robust Design principles to reduce effects of manufacturing variation and inner/outer noise.**
- **Improve signal-to-noise ratio by reducing noise rather than increasing signal**

# S/N Example - Reliability



# Failure Distribution

Would like a component to last forever. Reliability is a measure of a component's ability to last over time.

**f(t): time to failure probability density**

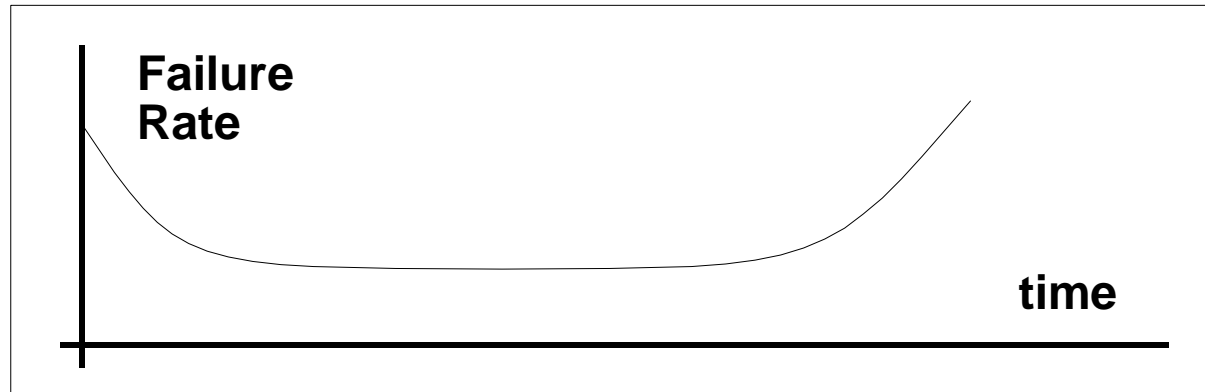
**Prob of a failure between (t and t+Δt): f(t)•Δt**

**Prob. of failure on interval from 0 to t:** 
$$F(t) = \int_0^t f(x) dx$$

**Reliability function,  $R(t) = 1 - F(t)$**

**Failure rate:  $Z(t) = f(t)/R(t)$**

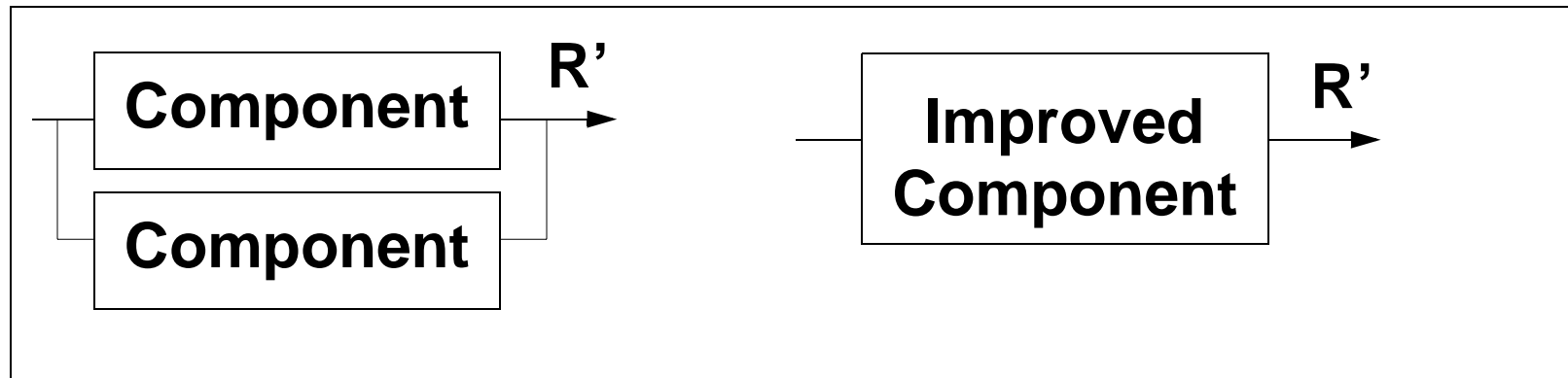
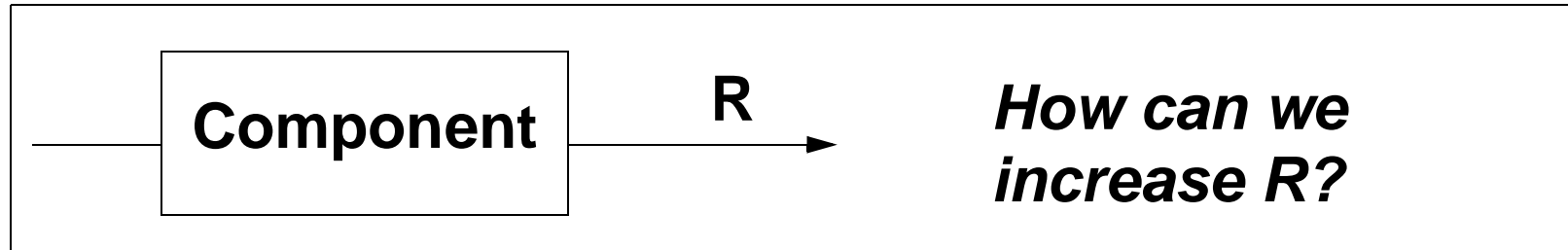
# Failure Rate Curve



Could assume that for useful part of life, failure rate is constant ( $\alpha$ )

Distribution of failure times is exponential:  $f(t) = \alpha e^{-\alpha t}$   
Time between failures exponentially distributed.

# Improving S/N Ratio



Which is preferred?