

# Nonlinear Model Predictive Control of a Latent Thermal Energy Storage Device for Electronics Cooling Applications

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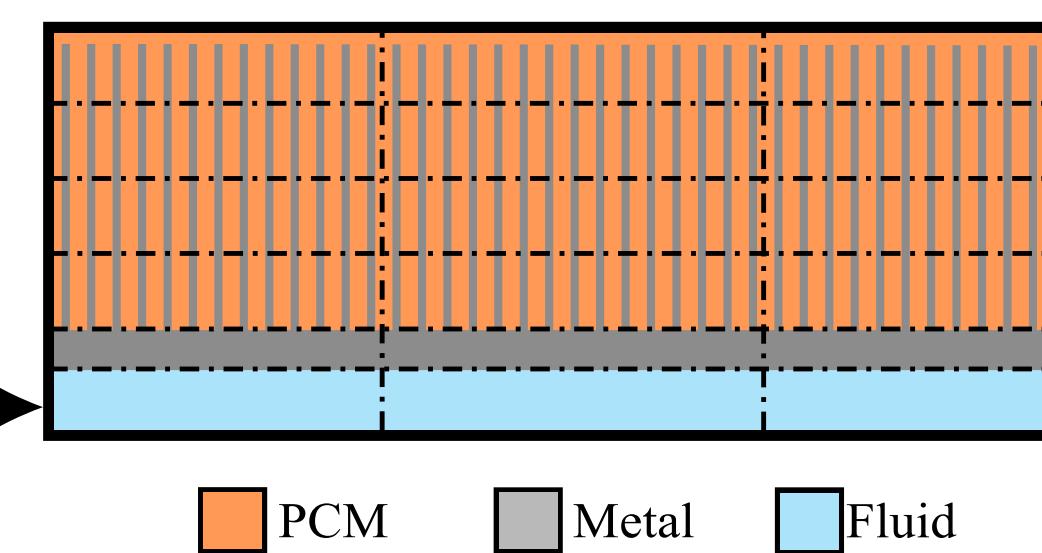
## Motivation

- Thermal management systems (TMSs) integrated with phase-change thermal energy storage (TES) devices, to provide robustness against highly transient heat loads produced by electrical systems, are called hybrid TMSs.
- The TES is designed to provide additional heat rejection via latent heat capacity with a phase change material (PCM) only when needed, so its operation must be actively controlled.
- To fully utilize the benefits of hybrid TMS, a nonlinear finite-horizon model predictive controller (NMPC) may be synthesized..
- To accurately predict TES state of charge (SOC) during transient operation, a fine discretization of the PCM melt front is needed.

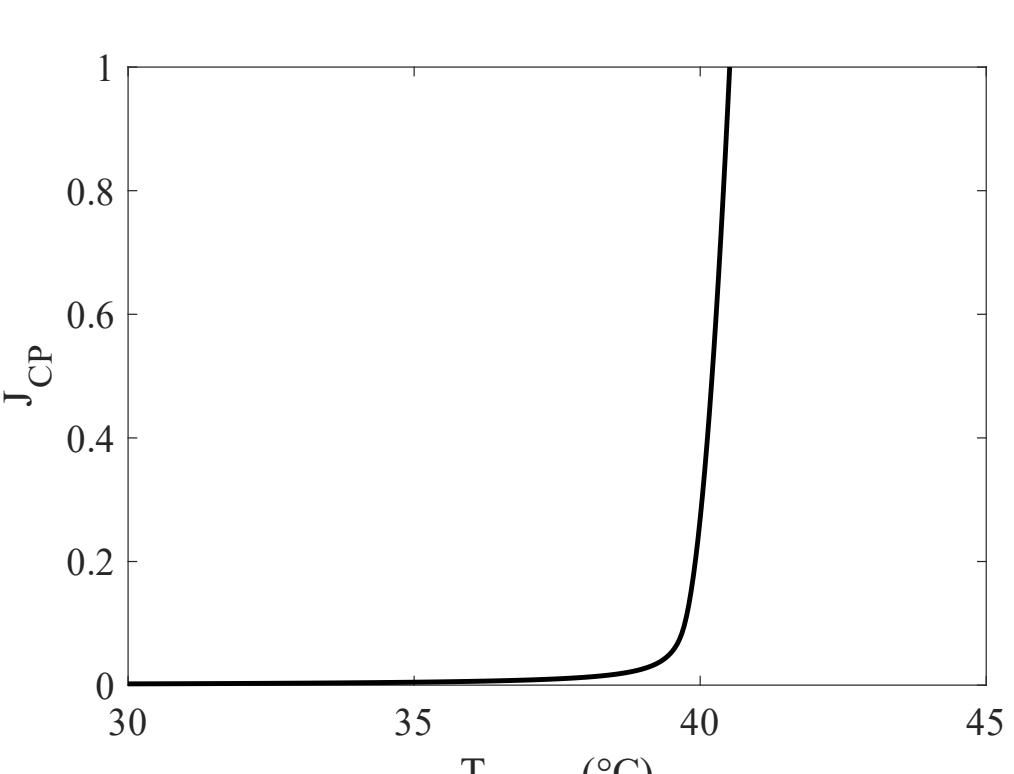
## Approach and Methodology

The single-phase cooling loop considered in this work is shown on the right. The cold plate and heat exchanger solid and liquid masses are each modeled as a lumped parameter system. In addition, the tank is modeled as a single state, assuming total mixing.

Right: The spatial domain of each TES device is discretized to transform the PDE into a system of ODEs. The PCM and fins are tightly packed, such that they can be modeled as a composite.



The hybrid TMS may be modeled as a graph, where the temperature of each control volume corresponds to a node in the associated graph. This allows for flexible and computationally efficient modeling of the hybrid system.



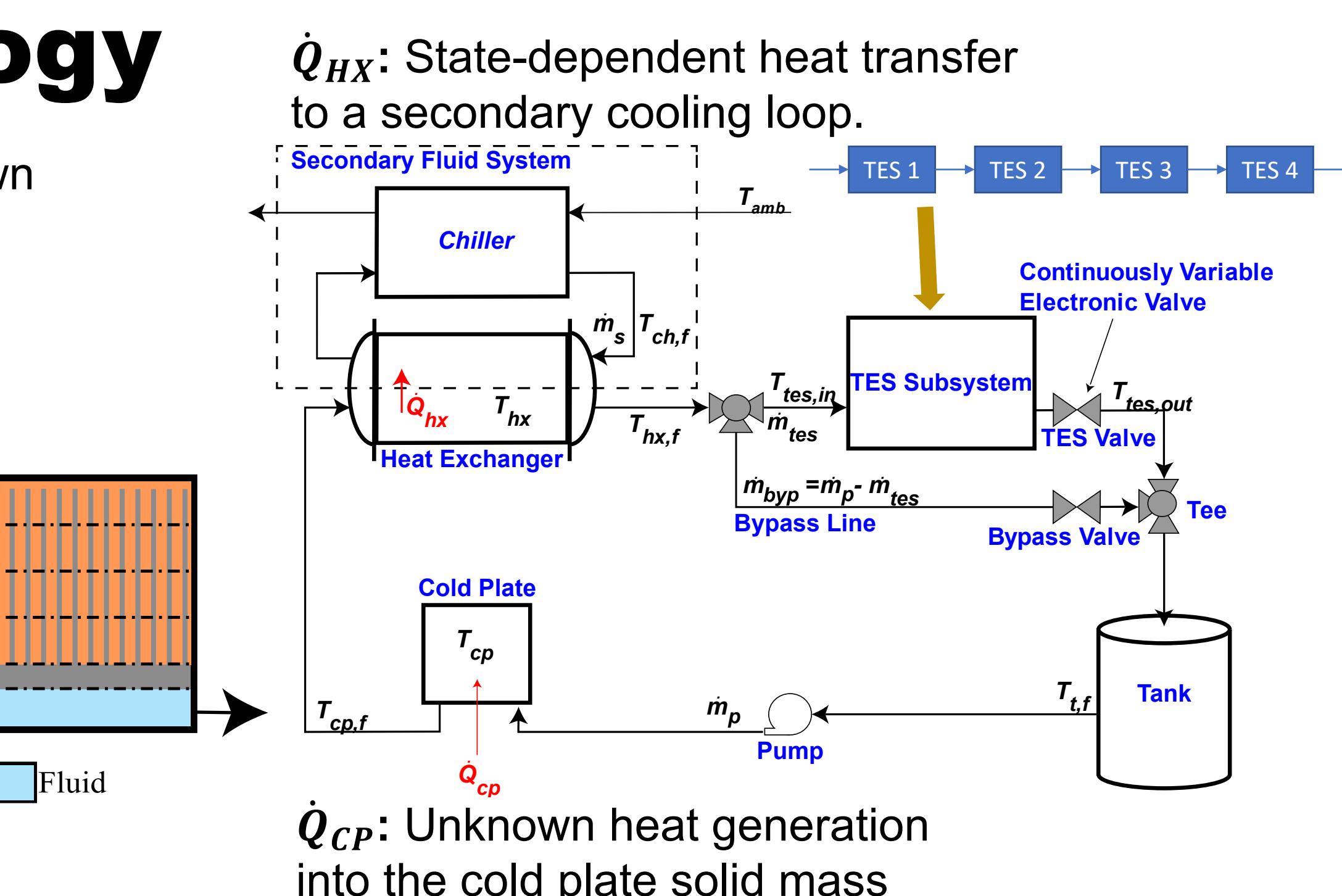
Above: pseudo barrier function

A non-linear model predictive controller (NMPC) is synthesized to control the hybrid TMS.

- Prediction model: 77 states, 2 control actions (primary and TES branch mass flow rates).
- The multi-objective function  $J$  is comprised of 3 objectives.

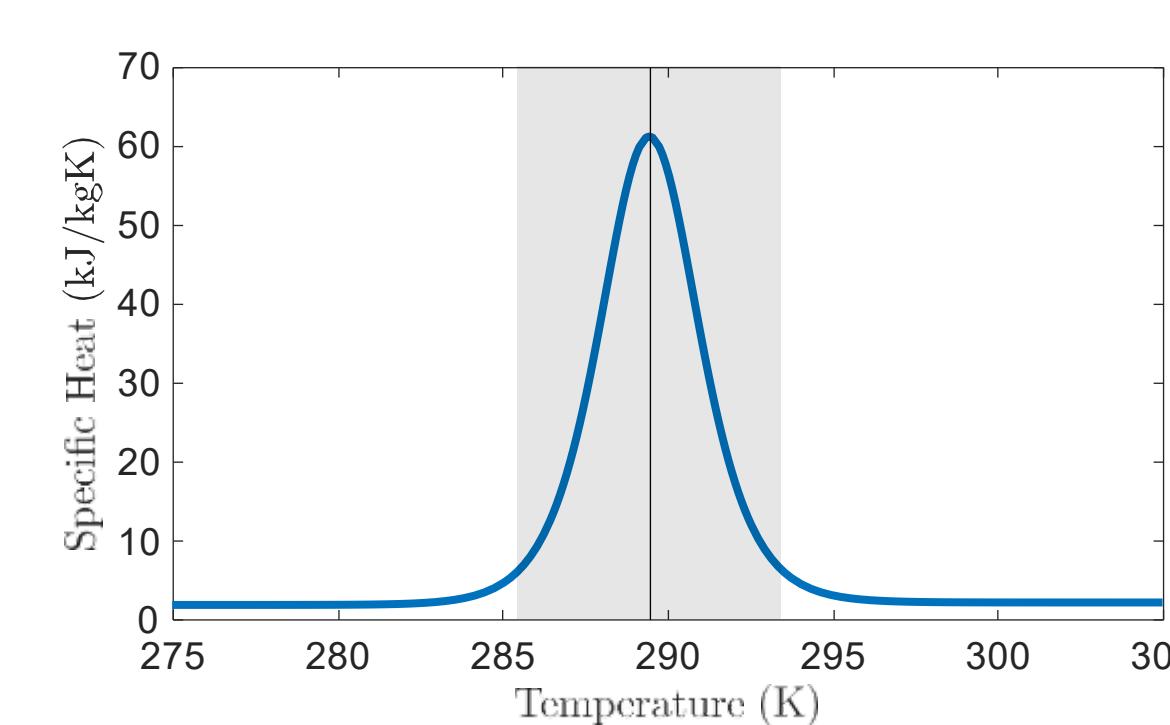
$$J[n] = \sum_{k=n}^{N+n} (J_{CP}[k] + J_{TES}[k] + J_u[k])$$

- $J_{CP}$ : Cold Plate temperature is to be regulated below some threshold  $T_{cp,max}$  if it is possible to do so within the horizon of the NMPC. This is achieved using a pseudo barrier function. While a true barrier function is asymptotic at the threshold, this function is not, allowing the cost function to be defined above the soft constraint.
- $J_{TES}$ : TES device temperature is penalized by a quadratic function to compensate for the limited time horizon.
- $J_u$ : Mass flow rate is penalized to ensure power efficient solutions, and the change in mass flow rate is also penalized to minimize actuator wear.



$\dot{Q}_{CP}$ : Unknown heat generation into the cold plate solid mass

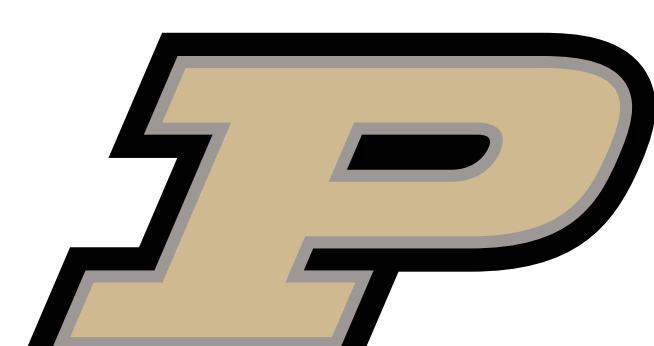
Right: The latent melting zone of the PCM is modeled as a continuous, sharp increase in the specific heat around the melting point of the PCM.



- The system dynamics may be written as in Eq. 1.
$$M(x)\dot{x} = C(x, u, d)x + Bd \quad (1)$$
- To implement the predictive step in the NMPC, the system dynamics are linearized at each point in the finite horizon and integrated using the implicit trapezoidal integration rule.
- Linearization is done by assuming M and C are constant over one step in the NMPC horizon.
- Approximate gradients are obtained for the linearized system to accelerate computation time.

### NMPC parameters

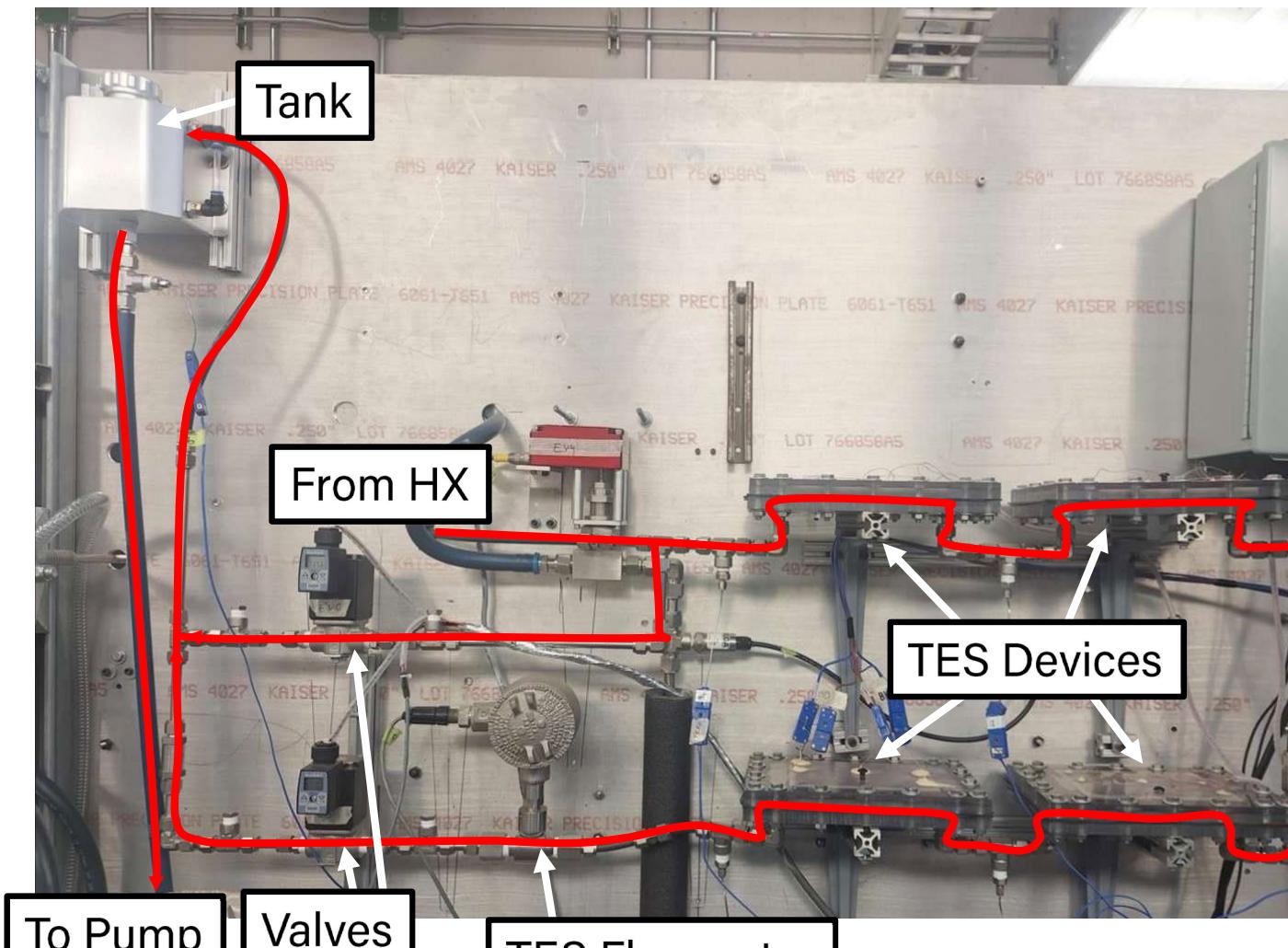
Parameter	Selected Value	Unit	Description
$N$	25	steps	Steps in NMPC Horizon
$\Delta t$	1	s	Control action update rate
$u_{min}$	0.0005	$kg \cdot s^{-1}$	Min allowed flow rate
$u_{max}$	0.1	$kg \cdot s^{-1}$	Max allowed flow rate
$\Delta u_{max}$	0.02	$kg \cdot s^{-1}$	Max allowed change in flow rate
$T_{CP,W,max}$	45	°C	Soft constraint max cold plate temperature
$T_{CH,F}$	8	°C	Chiller inlet temperature



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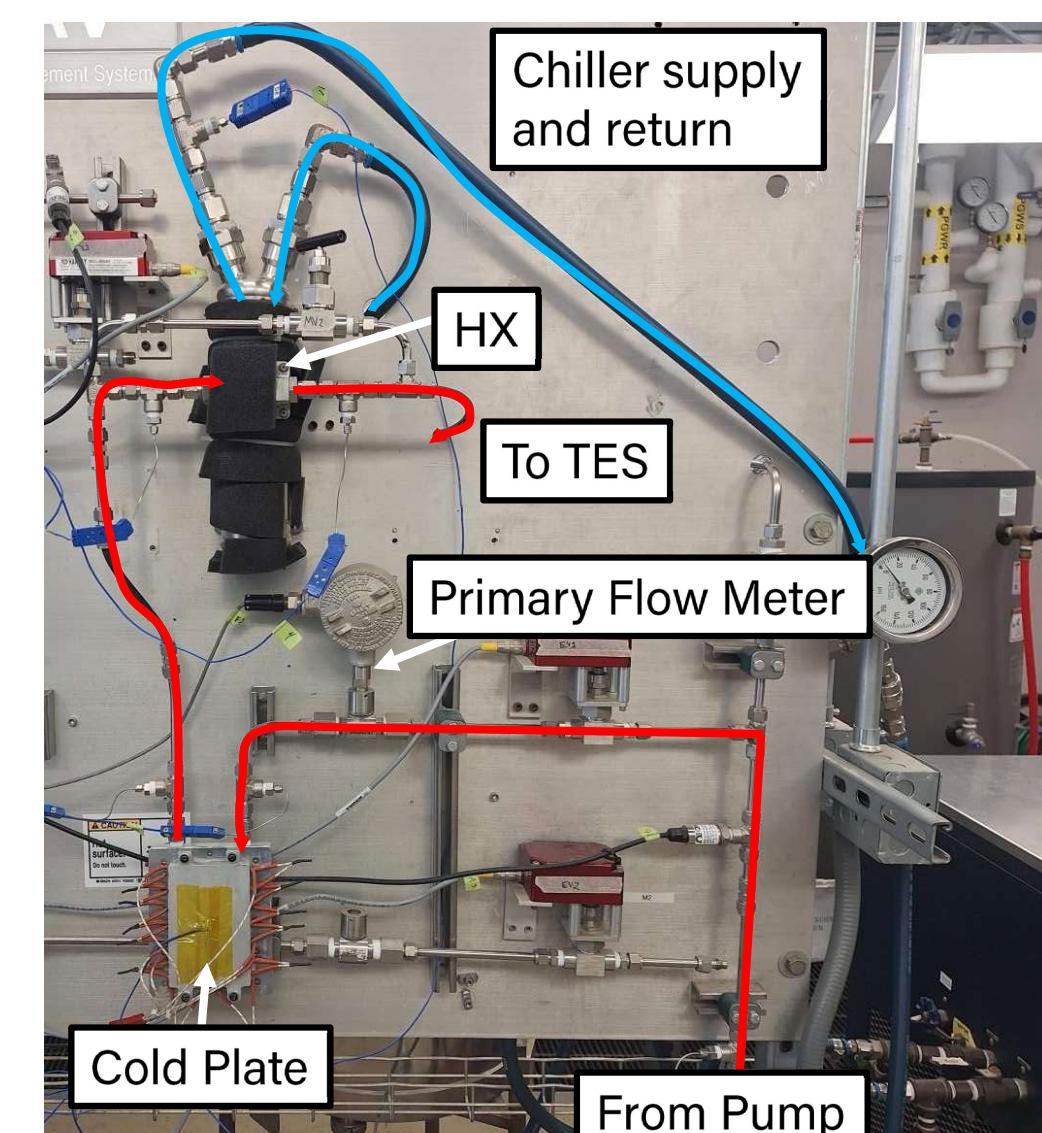
## Experimental System



Left: Front side of hybrid TMS experimental system

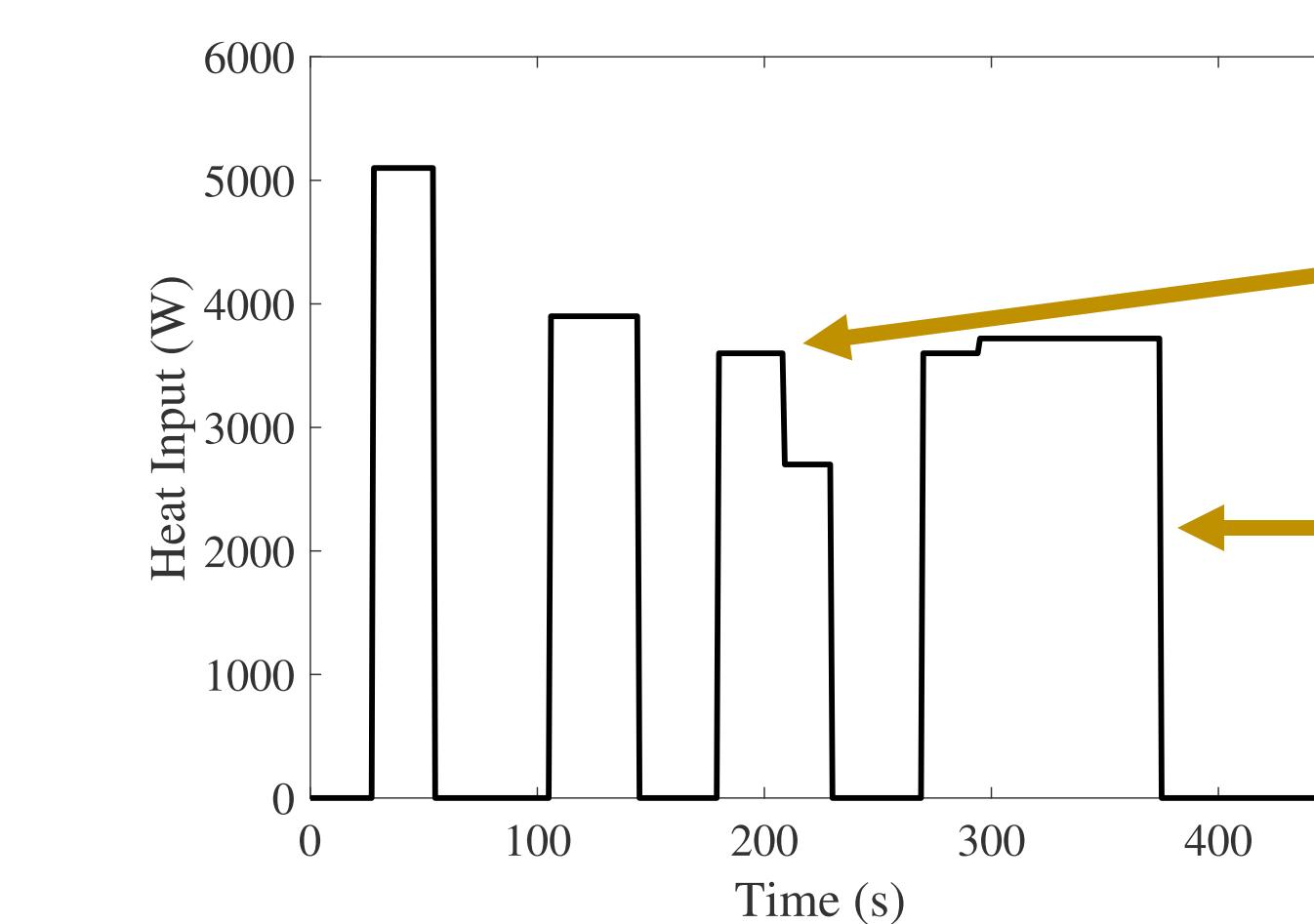
Right: Rear side of hybrid TMS experimental system

- The proposed NMPC was implemented on an experimental test system. Type-T thermocouples are used to measure twelve of the total seventy-two states. An observer is used to estimate the remaining states.
- NMPC determines mass flow rate setpoints, and individual lower-level controllers are used to track these setpoints.



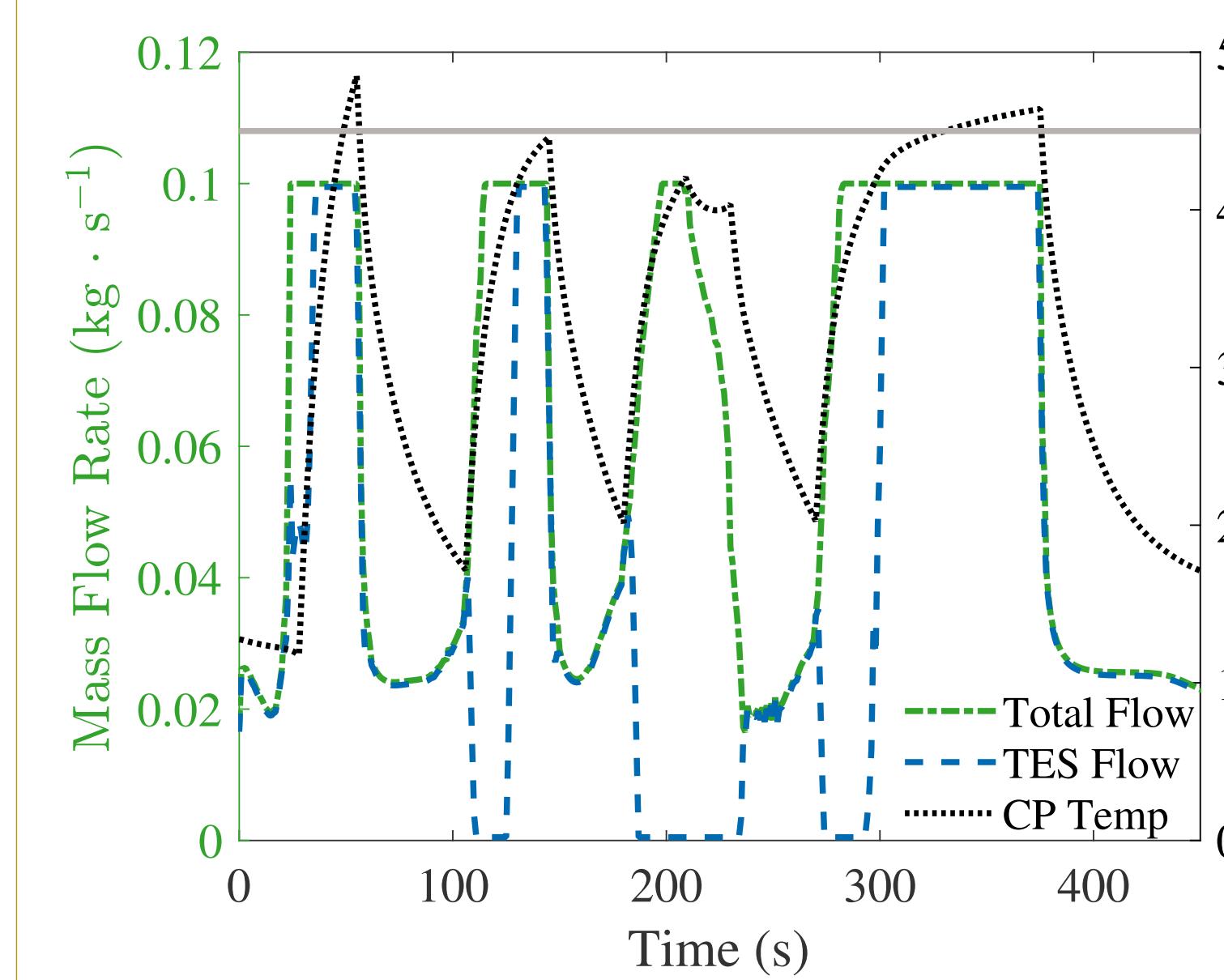
Left: Cold plate disturbance profile

- Decreasing load to demonstrate NMPC solution near soft constraint boundary
- Sustained loading to show significant TES usage.



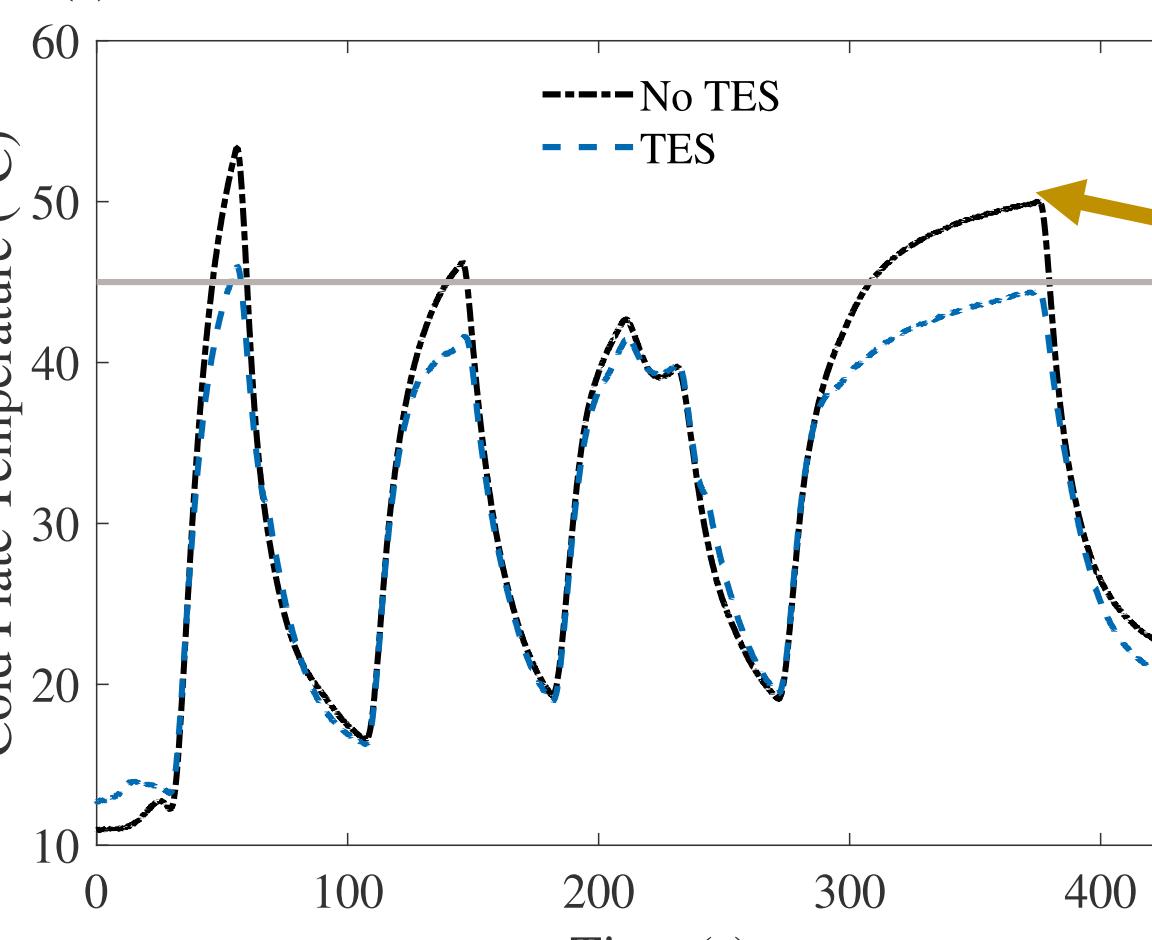
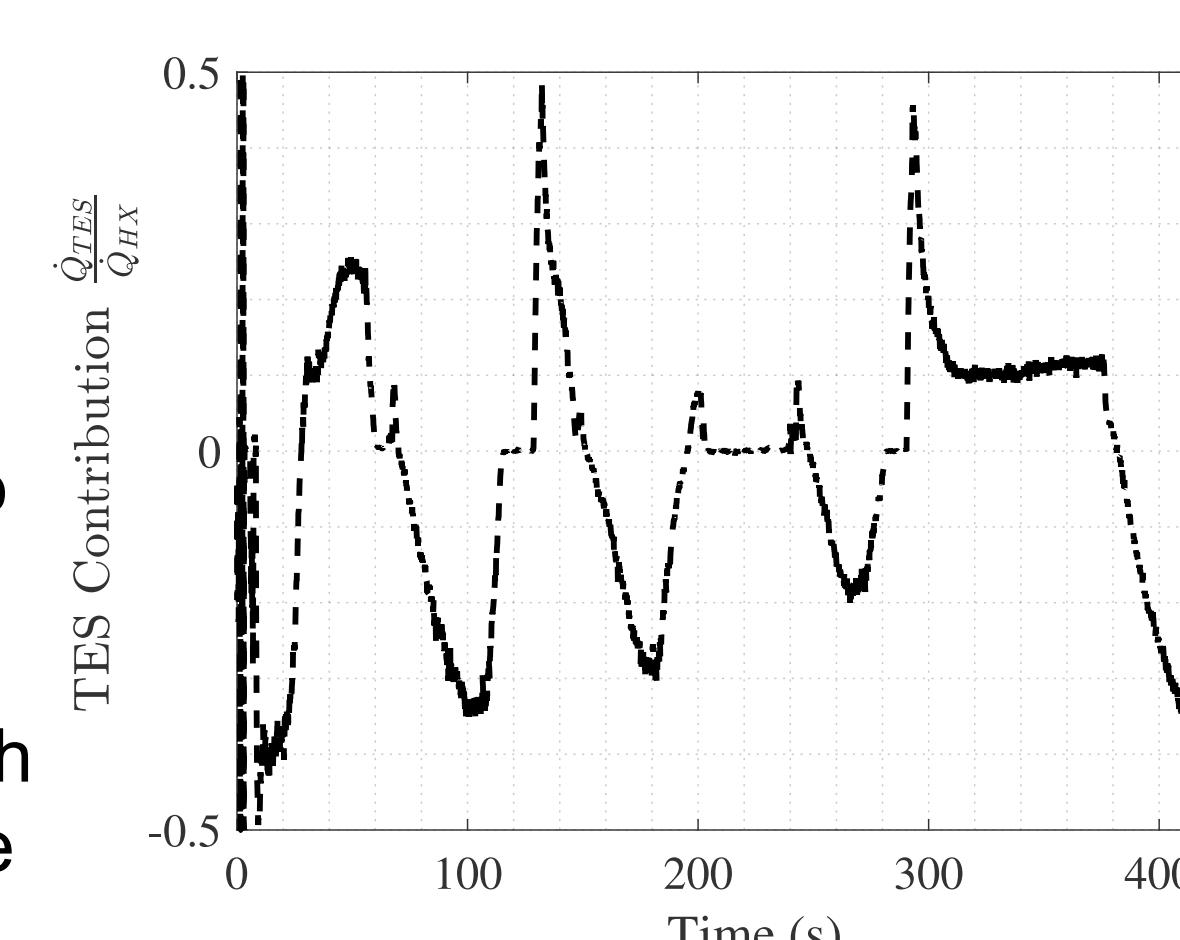
Left: Simulated closed loop response  
Right: Measured closed loop response

Below: Measured TES state of charge



Right: Ratio between heat transfer to TES and heat transfer through HX.

- TES is placed downstream of the HX to maximize heat rejection; This results in relatively less heat transfer through the TES compared to the HX.



- TES can keep the cold plate 7°C cooler during peak loads
- Despite NMPC, the system without the TES is unable to keep the temperature below the barrier temperature.

## Summary & Future Work

### Key Contributions

- Real-time control with a nonlinear model predictive controller of a hybrid TES system.

### Future Work

- Improve low level controllers.
- Utilize a more sophisticated power consumption cost function.
- Use control co-design approaches to fully optimize the system.

## Acknowledgements

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