Quantum for AI and AI for Quantum: Exploring the Benefits of Quantum Machine Learning in Representation Learning, Generalization, and Trust



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Quantum meets Al

Al for Quantum

- End-to-end Quantum Neural Networks for <u>representation</u> <u>learning</u>
- <u>Generalization</u> analysis of characterization of variational quantum circuit based functional regression

Quantum for Al

- Noise can be a friend in trustworthy Al
- Use of quantum modules to improve **privacy** in deep learning
- (Free) certified <u>robustness</u> to input perturbations in quantum systems

What are *Foundation Model and GenAI*?



On the Opportunities and Risks of Foundation Models

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Fig. 2. A foundation model can centralize the information from all the data from various modalities. This one model can then be adapted to a wide range of downstream tasks.



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Neural Scaling Laws



Robustness at <u>scale</u>: data and compute bungry

Kaplan et al. Scaling Laws for Neural Language Models. Arxiv 2020

GenAI: the Beauty and the Ugly of AI-generated Content



Press room / MEPs ready to negotiate first-ever rules for safe and transparent AI

MEPs ready to negotiate first-ever rules for safe and transparent AI

Press Releases PLENARY SESSION IMCO LIBE 14-06-2023 - 12:52



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in

- Full ban on Artificial Intelligence (AI) for biometric surveillance, emotion recognition, predictive policing
- Generative AI systems like ChatGPT must disclose that content was AIgenerated
- Al systems used to influence voters in elections considered to be highrisk



JULY 21, 2023

Administration Priorities The Record



BRIEFING ROOM > STATEMENTS AND RELEASES



Artificial Intelligence Office

C D A O Chief Digital and

Responsible Artificial Intelligence Test & Evaluation

Transforming the Department of Defense Through Assured AI

JATIC is developing an interoperable set of state-of-the-art software for rigorous AI model T&E

QTN-VQC

An end-to-end learning framework for quantum neural networks

Jun Qi, Chao-Han Huck Yang, Pin-Yu Chen, and Min-Hsiu Hsieh, "Theoretical Error Performance Analysis for Variational Quantum Circuit Based Functional Regression," npj Quantum Information, 2023

Jun Qi, Chao-Han Huck Yang, and Pin-Yu Chen, "QTN-VQC: An End-to-End Learning framework for Quantum Neural Networks," Physica Scripta, 2023

QTN-VQC Framework

- QTN: Quantum Tensor Network
- VQC: Variational Quantum Circuit



TTN: Tensor-Train Network

• Encoding input N-dim data into tensor product of a unit-norm local feature map $\phi \in R^d$

$$\Phi^{s_1s_2\cdots s_N}(\mathbf{x}) = \phi^{s_1}(x_1) \otimes \phi^{s_2}(x_2) \otimes \cdots \phi^{s_N}(x_N)$$

• Example: x_i is a pixel value ranging from [0,1]

$$\phi^{s_j}(x_j) = \left[\cos\left(\frac{\pi}{2}x_j\right), \, \sin\left(\frac{\pi}{2}x_j\right)\right]$$

-> Normalized wavefunction of a single qubit

• Goal of TTN: Compute $y = W \cdot \Phi(x)$ in a quantum-favored manner

Edwin Stoudenmire and David J. Schwab. "Supervised learning with tensor networks." *Advances in neural information processing systems* 29 (2016).

TTN-VQC: Hybrid Quantum Neural Nets [npj Quantum Information]

 Tensor Product Encoding (TPE): converting a classical data sample x into a quantum state |x>

 The blocks can be repeated to build deeper networks







Fig. 2 An illustration of three components in the VQC model. The TPE employs a series of $R_Y(\frac{\pi}{2}x_i)$ to transform classical data into quantum states. The PQC is composed of CNOT gates and single-qubit rotation gates R_X , R_Y , R_Z with free model parameters a, β , and γ . The CNOT gates impose the operation of quantum entanglement among qubits, and the gates R_X , R_Y , and R_Z can be adjustable during the training stage. The PQC model in the green dash square is repeatably copied to build a deeper model. The measurement converts the quantum states $|z_1\rangle$, $|z_2\rangle$, ..., $|z_U\rangle$ into the corresponding expectation values $\langle \sigma_z^{(1)} \rangle$, $\langle \sigma_z^{(2)} \rangle$, ..., $\langle \sigma_z^{(1)} \rangle$, $\langle \sigma_z^{(2)} \rangle$, ..., $\langle \sigma_z^{(0)} \rangle$ are connected to a loss function and the gradient descent algorithms can be used to update VQC parameters.

QTN-VQC: Fully Quantum Neural Networks [Physica Scripta]

- Two quantum circuit-implemented QTN architectures:
- 1. ConvMPS : convolutional matrix product state
- 2. ConvTTN: convolutional tree tensor network



Figure 3. An demonstration of two QTN architectures for the end-to-end quantum learning paradigm. (a) A convolutional matrix product state architecture. (b) A convolutional tree tensor network architecture. Similar to the VQC model, a TPE model is used to encode non-trainable $R_Y(x_i)$ gates with the classical input x_i , and several trainable $R_X(\theta_i)$ and $R_Y(\theta_i)$ gates in the red dash square is associated with parameters θ_i . The observables of the last quantum channel correspond to the expected values based on Pauli-Z operators and they are taken as QTN features for further processing. If a 2 × 2 convolutional kernel is used, the inputs corresponding to 4 × 4 matrices are associated with the outputs of the 4 × 2 × 2 matrices.

Performance Evaluation

- MNIST: Handwritten digit classification dataset
 - Each sample is a 28 x 28 grayscale image
 - 10000 samples for training and 2000 samples for testing
- Methods
 - PCA-VQC (naïve dimension reduction)
 - TTN-VQC (hybrid; 8 qubits)
 - ConvMPS-VQC (quautum; 4+8 qubits)
 - ConvTTN-VQC (quantum; 4+8 qubits)
- Please refer to papers for detailed implementations

3	4	2	1	9	5	6	2	1	8
8	9	1	2	5	0	Ø	6	4	4
6	7	0	1	6	ξ	6	3	7	0
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3	7	7	0	٩	¢	8	5	4	ŝ
7	2	6	4	Т	0	4	9	2	3

Test Accuracy

Models	CE	Accuracy (%)
PCA-VQC	0.3301	87.7
TTN-VQC	0.0634	98.6
ConvTTN-VQC	0.0805	98.5
ConvMPS-VQC	0.0917	98.3

Binary Classification on MNIST

Training loss

Testing loss



Representation Learning and Generalization of TTN-VQC and QTN-VQC (1)

- Functional Regression: Given a Q-dimensional input vector space R^Q and a measurable U-dimensional output vector space R^U , the TTN-VQC based vector-to-vector regression aims to find a TTN-VQC operator $f: R^Q \rightarrow R^U$ such that the output vectors of f can approximate those of a desirable target function h^* .
- *D*: data distribution; Draw *N* i.i.d. samples from *D*
- F_{TV} : TTN-VQC hy
- Population loss:

$$\mathcal{L}_{\mathcal{D}}(f) := \mathbb{E}_{\mathbf{x} \sim \mathcal{D}} \left[\ell(h_{\mathcal{D}}^*(\mathbf{x}), f(\mathbf{x})) \right]^{\text{of TTN-VQC operators}}$$
$$\mathcal{L}_{S}(f) := \frac{1}{N} \sum_{n=1}^{N} \ell(h_{\mathcal{D}}^*(\mathbf{x}_n), f(\mathbf{x}_n))$$

- Empirical loss:
- f_D^* : best hypothesis in F_{TV}

Representation Learning and Generalization of TTN-VQC and QTN-VQC (2)

- f_S^* : best hypothesis based on empirical loss minimization
- \bar{f}_S : returned hypothesis by gradient-based minimization
- Error decomposition:

$$\mathcal{L}_{\mathcal{D}}(\overline{f}_{S}) = \underbrace{\mathcal{L}_{\mathcal{D}}(f_{\mathcal{D}}^{*})}_{Approximation \ Error} + \underbrace{\mathcal{L}_{\mathcal{D}}(f_{S}^{*}) - \mathcal{L}_{\mathcal{D}}(f_{\mathcal{D}}^{*})}_{Estimation \ Error} + \underbrace{\mathcal{L}_{\mathcal{D}}(\overline{f}_{S}) - \mathcal{L}_{\mathcal{D}}(f_{S}^{*})}_{Training \ Error}$$

- We derive theoretical upper bounds for each error term under proper conditions (e.g., smooth target function h_D^*)

Representation Learning and Generalization of TTN-VQC and QTN-VQC (3)

- <u>Representation Power</u>: upper bound on approximation error
- <u>Generalization power</u>: upper bound on the estimation error concerning the empirical Rademacher complexity
- <u>Optimization bias</u>: training error can be exponentially converged to a small loss value
- Similar analysis holds for QTN-VQC

$\mathcal{L}_{\mathcal{D}}(\overline{f}_{S}) = \underbrace{\mathcal{L}_{\mathcal{D}}(f_{\mathcal{D}}^{*})}_{\mathcal{L}}$	$+ \underbrace{\mathcal{L}_{\mathcal{D}}(f_{S}^{*})}_{\mathcal{D}}$	$-\mathcal{L}_{\mathcal{D}}(f_{\mathcal{D}}^{*}) +$	$-\underbrace{\mathcal{L}_{\mathcal{D}}(\overline{f}_{S})-\mathcal{L}_{\mathcal{D}}(f_{S}^{*})}_{L}$
Approximation Error	r Estima	tion Error	Training Error
Category		This wo	ork
Learning problem		Regress	ion
Dimensionality reduct	ion	TTN	# measurements
Representation power		$\frac{\Theta(1)}{\sqrt{U}} + C$	$P\left(\frac{1}{\sqrt{M}}\right)$
Generalization power	# qubits	$\frac{2P}{\sqrt{N}}\left(\sqrt{2}\right)$	$\overline{\sum_{k=1}^{K}\Lambda_k^2}+\Lambda'\Big)$
Conditions for optimization bias	# training samples	μ -PL + $$	1-Lipschitz

Quantum Foundation Models?

Linear head / PEFT for downstream task

Encoder/Representation

network from pretraining

Foundation Models





QTN-VQC

Exploring "Quantum Foundation Models" and "Quantum Transfer Learning" with TTN-VQC

Pre-training Tensor-Train Networks Facilitates Machine Learning with Variational Quantum Circuits

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Key Results

Category	Pre+TTN-VQC	TTN-VQC	
Representation error # source samples	$\frac{2P}{\sqrt{ S_0 }}\sqrt{\sum_{k=1}^K \Lambda_k^2} + \mathcal{O}(\frac{1}{\sqrt{M}})$	$rac{\Theta(1)}{\sqrt{U}} + \mathcal{O}(rac{1}{\sqrt{M}})$	
Estimation error	# target $2P\Lambda$ samples $\sqrt{ S_T }$	$\frac{2P}{\sqrt{N}}(\sqrt{\sum_{k=1}^{K}\Lambda_k^2} + \Lambda)$	
Conditions for Optimization bias	without PL assumption	PL assumption	
Optimization bias	$\beta R^2 + R \sqrt{\frac{L^2 + \beta^2 R^2}{T_{\rm sgd}}}$	sufficient small	

Binary	MNIST
classifi	cation

Models	Params (Mb)	CE	Accuracy (%)	
PCA-VQC_8Qubit	0.080	0.5744	75.8	
TTN-VQC_8Qubit	0.452	0.0625	98.7	
Pre+TTN-VQC_8Qubit	0.452	0.0390	99.0	

co-TenQu: A quantum-classical collaborative training architecture [IEEE TQE 2024]



- co-TenQu trains the model directly on quantum states aiming at accelerating the training process and improving performance
- co-TenQu with Qiskit and PennyLane:
 - Enhances a classical deep neural network by up to 41.72% in a fair setting.
 - Outperforms other quantum-based methods by up to 1.9X and achieves similar accuracy while utilizing 70.59% fewer qubits.

Data Privacy and Robustness

Data Privacy Breach in AI/ML

Extracting Training Data from Large Language Models								
			USENIX 2021					
Nicholas Carlini ¹	Florian Tramèr ²	Eric Wallace ³	Matthew Jagielski ⁴					
Ariel Herbert-Voss ^{5,6}	Katherine Lee1	Adam Roberts ¹	Tom Brown ⁵					
Dawn Song ³	Úlfar Erlingsson ⁷	Alina Oprea ⁴	Colin Raffel ¹					
¹ Google ² Stanford ³ UC	Berkeley ⁴ Northeast	ern University ⁵ Ope	enAI ⁶ Harvard ⁷ Apple					

Prefix East Stroudsburg Stroudsburg...



Figure 1: **Our extraction attack.** Given query access to a neural network language model, we extract an individual person's name, email address, phone number, fax number, and physical address. The example in this figure shows information that is all accurate so we redact it to protect privacy.



- Clients submit gradients of private data for federated learning
- An honest but curious server (aggregator) in vertical federated learning can recover private client data without violating the protocol (without privacy protection mechanisms)



Quantum Layers for Data Protection

- Vertical federated learning
- Speech input is first processed into Mel spectrogram and then sent into a quantum layer for encoding (on the cloud)
- The encoded features are used to train the acoustic model (on user devices)
- Retain competitive accuracy and reduce model parameter leakage



Chao-Han Huck Yang, Jun Qi, Samuel Yen-Chi Chen, Pin-Yu Chen, Sabato Marco Siniscalchi, Xiaoli Ma, and Chin-Hui Lee. "Decentralizing feature extraction with quantum convolutional neural network for automatic speech recognition." ICASSP 2021

BERT (transformer models) with Quantum Temporal Convolution Layers



Embedding	word2vec				BERT			
(n,k)	(1,4)	(2,2)	(2,3)	(2,4)	(1,4)	(2,2)	(2,3)	(2,4)
TCN	80.09	80.22	80.91	82.34	95.18	95.03	94.95	95.23
QTC	81.42	82.49	83.82	83.95	96.69	96.92	96.32	96.98

- *n*: # of filters
- k: kernel size
- TCN: random temporal convolutional network

Chao-Han Huck Yang, Jun Qi, Samuel Yen-Chi Chen, Yu Tsao, and Pin-Yu Chen. "When BERT meets quantum temporal convolution learning for text classification in heterogeneous computing." ICASSP 2022

Robustness Challenges in AI/ML

 $(x, y) \sim D$

- x: data sample
- y: groundtruth
- D: in-domain data distribution
- (in-distribution)
- θ : model parameters
- $\mathbf{f}_{\mathbf{\theta}}(x)$: model prediction on x

Robustness Categories

- Adversarial robustness (worst-case performance)
- Out-of-distribution (OOD) generalization (domain shifts)
- Out-of-distribution detection (unknowns)

(I) Adversarial robustness: x' similar to x. Ideally, $f_{\theta}(x') = f_{\theta}(x)$



δ: adversarial perturbation



(II) OOD generalization: $x' \sim D'$, a shifted version of D Ideally, $f_{\theta}(x') = f_{\theta}(x)$





(III) OOD detection: x' ~ D', a dissimilar or new domain w.r.t. D Ideally, $f_{\theta}(x') = "Unknown"$

 $f_{\theta}(.) \in \{cat, dog\}$ $f_{\theta}(\mathbf{M}) = "Unknown/OOD"$

Randomized Smoothing for Certified Robustness

- Rough idea: "Majority vote" with Gaussian perturbed input for classification gives guaranteed robustness
- *f* : a base (deterministic) classifier

 $g(x) = \underset{c \in \mathcal{Y}}{\arg \max} \mathbb{P}(f(x + \varepsilon) = c)$ (1) where $\varepsilon \sim \mathcal{N}(0, \sigma^2 I)$

Theorem 1. Let $f : \mathbb{R}^d \to \mathcal{Y}$ be any deterministic or random function, and let $\varepsilon \sim \mathcal{N}(0, \sigma^2 I)$. Let g be defined as in (1). Suppose $c_A \in \mathcal{Y}$ and $\underline{p}_A, \overline{p}_B \in [0, 1]$ satisfy:

$$\mathbb{P}(f(x+\varepsilon) = c_A) \ge \underline{p_A} \ge \overline{p_B} \ge \max_{c \neq c_A} \mathbb{P}(f(x+\varepsilon) = c) \quad (2)$$

Then $g(x + \delta) = c_A$ for all $\|\delta\|_2 < R$, where

$$R = \frac{\sigma}{2} \left(\Phi^{-1}(\underline{p_A}) - \Phi^{-1}(\overline{p_B}) \right) \tag{3}$$



Figure 1. Evaluating the smoothed classifier at an input x. Left: the decision regions of the base classifier f are drawn in different colors. The dotted lines are the level sets of the distribution $\mathcal{N}(x, \sigma^2 I)$. **Right**: the distribution $f(\mathcal{N}(x, \sigma^2 I))$. As discussed below, $\underline{p_A}$ is a lower bound on the probability of the top class and $\overline{p_B}$ is an upper bound on the probability of each other class. Here, g(x) is "blue."

Cohen, Jeremy, Elan Rosenfeld, and Zico Kolter. "Certified adversarial robustness via randomized smoothing." ICML 2019

Randomized Smoothing for Quantum Circuits

- Theoretical proof that the addition of quantum random rotation noise can improve the robustness of quantum classifiers against adversarial perturbations
- Noise addition -> Quantum Differential Privacy -> Certified Robustness

Algorithm 1 Quantum model under quantum noise rotation
Input σ: where σ is density matrix of n-dim data.
Output f(θ*, σ)
1. For a chosen quantum classifier, add Pauli-X operators before each input qubit.
2. Generate n random variables θ₁, θ₂, ..., θ_n subject to 0 < h₁ < tan θ_i < h₂ for all i ∈ {1, 2, ..., n}.
3. Set up rotation angles of additional Pauli-X operators with θ₁, θ₂, ..., θ_n
4. Execute the quantum classifier N times to get the score vector f(θ*, σ).

Fruits for thoughts:

- Can Quantum-inspired noise processing improve certified robustness of classical ML classifiers?
- Large Language Models and GenAI technology are stochastic by design -> Quantum modeling?

Jhih-Cing Huang, Yu-Lin Tsai, Chao-Han Huck Yang, Cheng-Fang Su, Chia-Mu Yu, Pin-Yu Chen, and Sy-Yen Kuo. "Certified robustness of quantum classifiers against adversarial examples through quantum noise." ICASSP 2023

Concluding Remarks

- Al for Quantum: Tensor-Train Networks as powerful representation learning tools for quantum neural networks
- Quantum for AI: Quantum circuits and noises as privacy-enhanced and robustness-improved modules for classical and quantum ML
- Post Quantum AI: What can we do with Quantum Foundation Models and Quantum GenAI? (no, they are not buzz words)
 - Quantum-inspired trust and safety for AI
 - Al-inspired risks for Quantum Al

You You

what can quantum computing help with generative AI?

Copilot

Quantum computing has the potential to significantly impact generative AI in several ways:

- 1. Speeding up computations: Quantum computers can perform certain calculations much faster than classical computers, which could accelerate the training of generative models.
- 2. Handling complex problems: Quantum computing can process and analyze large datasets more efficiently, which is beneficial for training generative models on complex tasks.
- Improving optimization: Quantum algorithms can potentially find better solutions to optimization problems, which are central to training generative AI models.
- Enhancing creativity: With its ability to explore a vast search space, quantum computing could help generative AI produce more diverse and innovative outputs.
- 5. Energy efficiency: Quantum computers could use less energy for certain computations, making the process of training generative AI models more sustainable.

While quantum computing is still in its early stages, its integration with generative AI could lead to breakthroughs in the field, enabling the creation of more advanced and efficient AI systems.

