

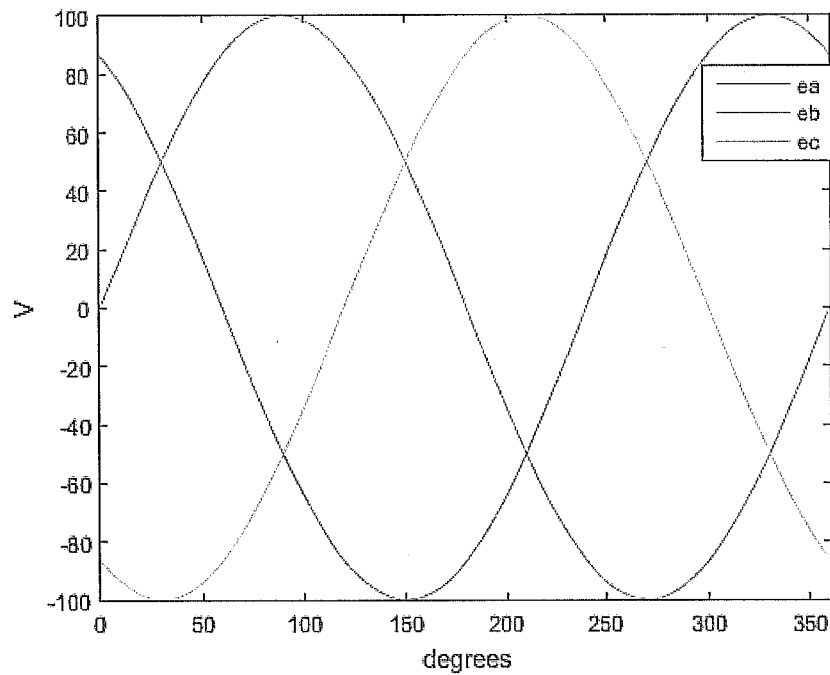
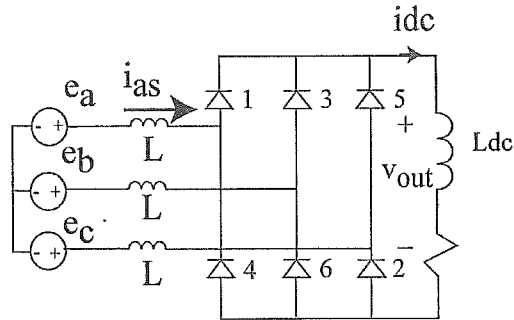
**PE-3**

**August 2017 QE**

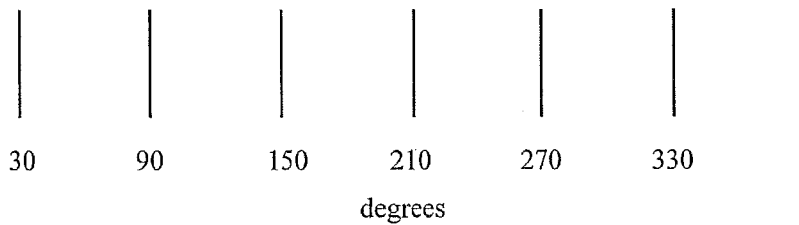
**PE-3 page 1 of 3**

1. Given the following system. (40 pts)

$$e_a = 100 \sin(\theta + 120^\circ), e_b = 100 \sin(\theta), e_c = 100 \sin(\theta - 120^\circ), \omega = 1000 \text{ rad/s.}$$



a. Assuming  $L_{dc}$  is large, label the diodes that conduct on the figure below for the situations in which the inverter is operating in 2-3 mode. Use diode numbering from the figure. You will need to insert subintervals to indicate commutation.

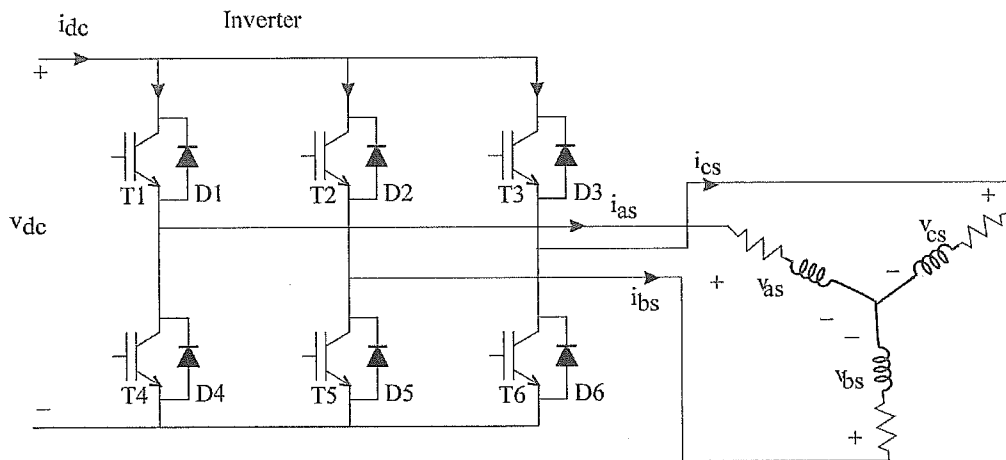


- b. Assume  $L = 1 \text{ mH}$ ,  $L_{dc} = \text{large}$ , 2-3 mode operation, and that the derivative of the short term average of the output current is zero. Derive the expression

$$\hat{v}_{out} = \frac{300\sqrt{3}}{\pi} - \frac{3}{\pi} \hat{i}_{dc}$$

Show all steps and state assumptions made.

2. Given the 3-phase inverter.  $v_{dc} = 100 \text{ v}$ . Each phase of the load has an inductance  $L = 10 \text{ mH}$ , and  $r = 0$  (negligible value). There is no coupling between phases. (35 pts)



- a) Derive the expression  $\hat{v}_{as} = 0.5d_a v_{dc}$ , where  $d_a$  is the phase-a duty cycle. State any assumptions used in the derivation.
- b) Assuming the inverter is operating under sine-triangle modulation (no 3<sup>rd</sup> harmonic injection) and you need phase-currents of the form:  
 $i_{as} = I_p \cos(100t)$ ,  $i_{bs} = I_p \cos(100t - 120^\circ)$ ,  $i_{cs} = I_p \cos(100t + 120^\circ)$ .  
 Determine the maximum value of  $I_p$  that can be obtained if you cannot tolerate harmonics in your current. For this value express  $d_a$ . Then, determine the maximum value of  $I_p$  and a corresponding  $d_a$  for the case in which you can tolerate harmonics in the current. Note that the  $d_a$  for this case is not unique.

Write in Exam Book Only

3. For the given DC chopper circuit system and armature current shown below. Plot the diode currents and source current. Assuming  $k_v \omega_r = 100$  V,  $L_{AA} = 1$  mH,  $T = 1$  ms, determine the duty cycle  $k$ , and the source voltage  $v_s$ . State any assumptions made in your analysis. (25 pts)

