# Distributed Resilience for Swarms of Autonomous Agents

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#### Why Multi-Agent Systems (MAS)?

MAS usually offers better **autonomy**, **robustness**, **flexibility...** and are able to achieve sophisticated missions that are well beyond individual systems' capabilities





Each individual:

mobile

low-cost

autonomous

local accessibility



**46** €

• The whole swarm:

large-scale

heterogeneous

communication constraints

no centralized controller

Key enabler:

**local** coordination

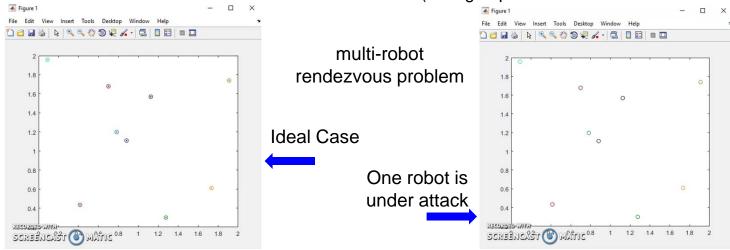
(sensing/communications among nearby neighbors)

**Distributed** algorithms for control/optimization/coordination

**global** objectives

(exploration of the unknown, formation flight, cooperative sensing, search/rescue)

 Advantages: scalability, flexibility, robust under individual node/link failures. Disadvantage: The whole network is vulnerable to sophisticated cyber-attacks. (strong dependence on local coordination)



### Research Challenges towards Resilience for MAS



Agents

- low-cost (limited sensing/processing)
- only local information available

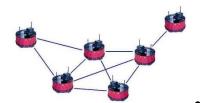
"the ability to prepare and plan for, absorb, recover from, and more successfully adapt to adverse events."



Cyber-Attacks

- highly mobile
- sophisticated (fully control the agent)
- launched massively from multiple locations

Techniques for resilience in MAS must be **automated**, **adaptive** to timevarying networks and mobile malicious agents, works in a **fully distributed** scenario.



Underlying Networks

time-varying

#### Resilience for Consensus-based Distributed Algorithms

All agents reach an agreement on some quantity of interest

- Consensus is the key enabler for swarm of agents to work as a cohesive whole
- o Unconstrained Consensus: All agents reach the same value.
- o Constrained Consensus: All agents reach the same and specific value.
- Optimal Constrained Consensus: All agents reach the same and specific value, which minimizes a global cost function.



$$x_i(t+1) = f_i(v_i)$$
 failure of consensus

$$v_i = \sum_{j \in \mathcal{N}_i(t)} w_{ij} x_j(t)$$
 injects information from malicious agents.

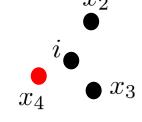
How to exclude malicious information without knowing which one is malicious?

Example:
 An normal agent i receives some states in the plane.

Suppose it is known that at most one of them is malicious.

majority rule? works for unconstrained consensus

is **not applicable** here because of local constraints



Any Ideas?



- Achieve an *resilient average*  $ar{v}_i = \sum_{j \in ar{\mathcal{N}}_i} ar{w}_{ij} x_j$  , which
  - o is **always** a weighted average of normal agents' states
  - could be achieved only by local information plus little knowledge about the malicious agents (an upper bound of how many malicious agents in agents' neighbors)
- Key Idea: Intersection of convex hulls.

$$\mathcal{M}_i = \{x_i, x_1, x_2, x_3, x_4\} \qquad d_i = 5$$

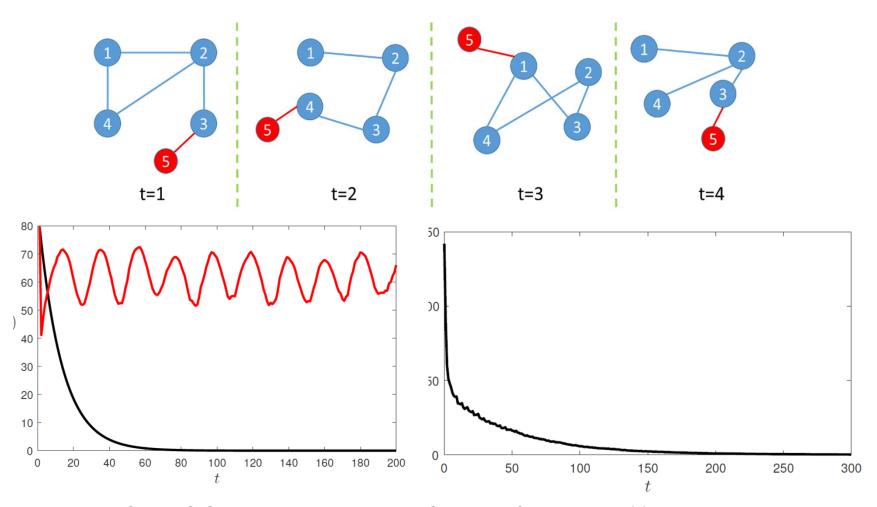
Suppose we know that at most  $r_i = 1$  are malicious.

- (1.) List all subsets of  $\mathcal{M}_i$  with size  $d_i r_i = 4$
- (2.) Choose  $\bar{v}_i \bigcap_{k \in r} \mathcal{H}(\mathcal{M}_{ik})$  is always a resilient average  $\bar{v}_i = \sum_{j \in \bar{\mathcal{N}}_i} \bar{w}_{ij} x_j$

Advantage: Utilizes all received information but eliminate impacts of malicious ones.

• **Simulations on** consensus-based distributed optimizations.

Time-varying networks; Byzantine attack; Time-varying locations; Only local information available.

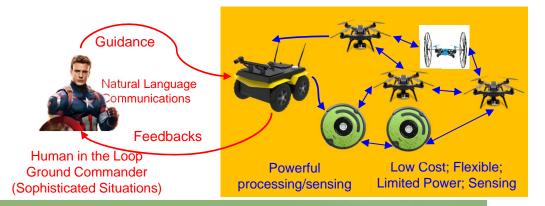


- X. Wang, S. Mou, S. Sundaram. Numerical Algebra, Control and Optimizations, 9(3), 269-281, 2019
- Presentation at the 8<sup>th</sup> Midwest Workshop on Control and Game Theory, April, 2019
- Presentation at the 57th Annual Allerton Conference on Communication, Control and Computing, Oct. 2019

#### Ongoing Project: Al-assisted Multi-Agent Systems with Human-in-the-Loop

• We aim to develop an Al-assisted multiagent platform, which is able to provide distributed environment perception/situation awareness; perform real-time, dynamic and distributed control/management of assets, planning/decision making/task assignment; include human-in-the-loop; improve performance as time evolves.

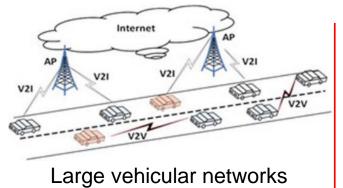
\*This ongoing project relies on collaboration of multiple universities, with funding from **Northrop Grumman** (2019-2021).



Purdue engineers are developing an **autonomous platform** of air and ground robots.





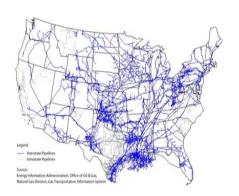


top-down analysis



Resilient,
Distributed algorithms
for control/optimization/coordination





## Thank You!

For our experimental results, please refer to Autonomous & Intelligent Multi-agent Systems (AIMS) Lab

https://engineering.purdue.edu/AIMS







Transportation Networks