

# Lecture 11: Particle Swarm Optimization

**Suggested reading:** Y. Shi, R. Eberhart, “A Modified Particle Swarm Optimizer,”  
Evolutionary Computation Proceedings, 1998, pp. 69-73.



# GAs and PSOs

## ■ Similarities

- Both operate on populations (swarms)
- Neither uses derivatives
- Both biologically motivated

## ■ Differences

- GAs based on genetics and evolution
- PSOs based on social behavior
- In PSOs, same individuals survive throughout study



# Definitions

- Size of search space:  $d = [1 \cdots D]$

- Position of  $i$ 'th particle:  $\mathbf{x}_i = [x_{i1} \quad x_{i2} \quad \cdots \quad x_{iD}]^T$

- Best position  $i$ 'th particle has ever seen:

$$\mathbf{p}_i = [p_{i1} \quad p_{i2} \quad \cdots \quad p_{iD}]^T$$

- Velocity of  $i$ 'th particle:  $\mathbf{v}_i = [v_{i1} \quad v_{i2} \quad \cdots \quad v_{iD}]^T$

- Best position any particle has ever seen:

$$\mathbf{G} = [g_1 \quad g_2 \quad \cdots \quad g_D]^T$$



# Position and Velocity Update

$$v_{id} = wv_{id} + c_1 rand()(p_{id} - x_{id}) + c_2 rand()(g_d - x_{id})$$

$$x_{id} = x_{id} + v_{id}$$

Recommended parameters

w: 0.9-1.2

$c_1$ : 1.4

$c_2$ : 0.1

# GA/PSO Comparison

## Electromagnet Design (12 DOF)

GA:

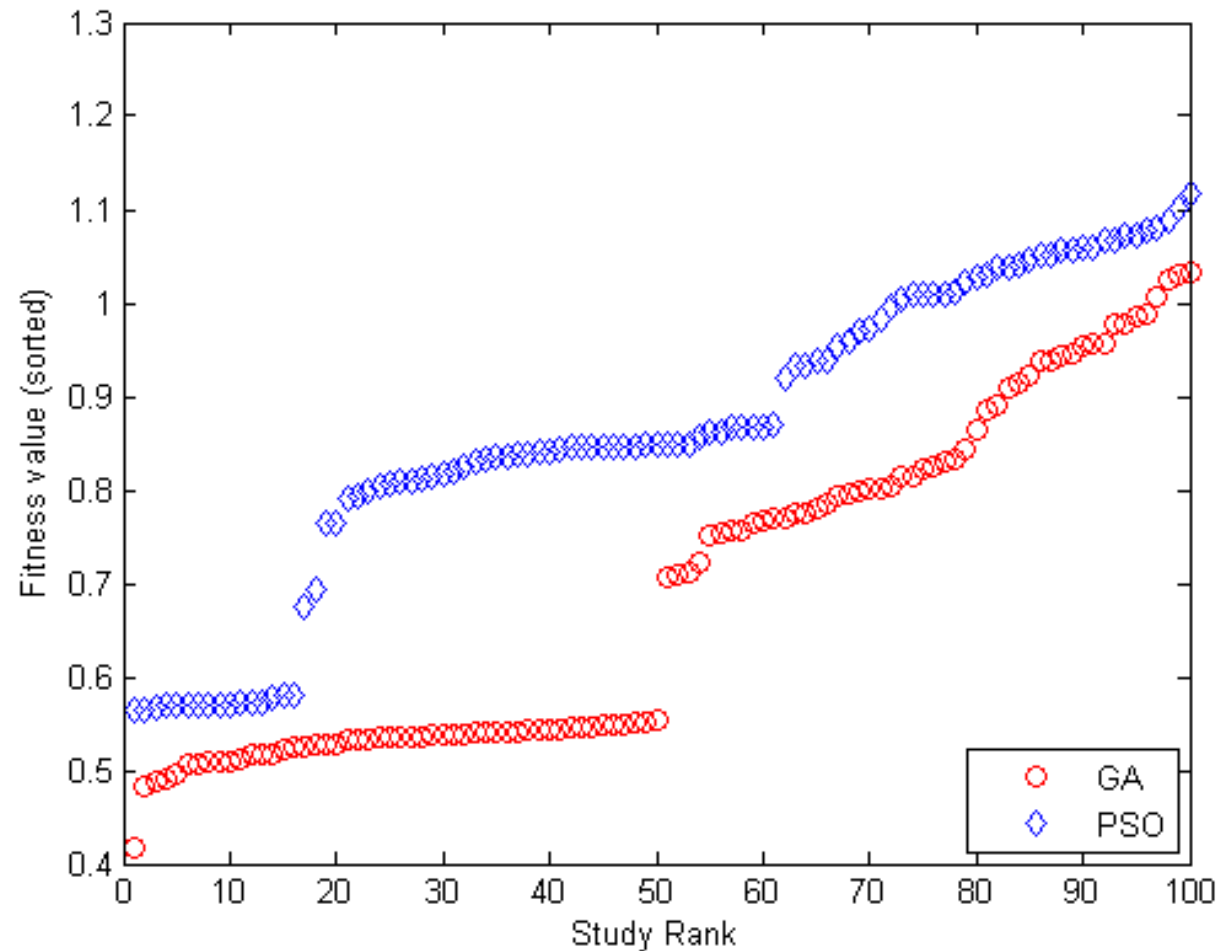
Individuals: 1000

Generations: 5000

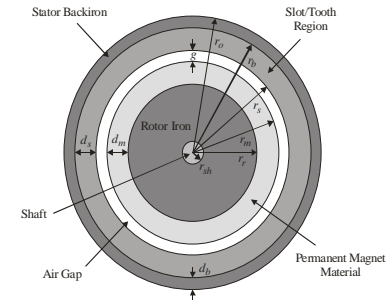
PSO:

Individuals: 400

Iterations: 7025



# GA/PSO Comparison PMSM Design (17 DOF)



GA:  
 Individuals: 500  
 Generations: 500  
 PSO:  
 Individuals: 378  
 Iterations: 378

