



## **Entropy change for an incompressible substance**

(Mythbusters hot water heater “rocket”:

<https://www.youtube.com/watch?v=jbreKn4PoAc>)

**From the  $T$ - $ds$  relations**

$$Tds = du + pdv$$

**For an incompressible substance**

$$dv = 0 \text{ and } du = c(T)dT$$

**For the incompressible substance model**

- Liquids and solids are often approximated as being incompressible.
- $v = \text{constant}$
- $c(T)$ ,  $u = u(T)$ ,  $h = h(T, p)$ ,  $s = s(T)$
- $u(T_2) - u(T_1) = \int_{T_1}^{T_2} c(T)dT$
- $h(T_2, p_2) - h(T_1, p_1) = u(T_2) - u(T_1) + (p_2 - p_1)v$
- $s(T_2) - s(T_1) = \int_{T_1}^{T_2} c(T) \frac{dT}{T}$

If the temperature range isn't too large, then it's reasonable to assume  $c \approx \text{constant}$ ,

- $u(T_2) - u(T_1) \approx c(T_2 - T_1)$
- $h(T_2, p_2) - h(T_1, p_1) \approx c(T_2 - T_1) + (p_2 - p_1)v$
- $s(T_2) - s(T_1) \approx c \ln \left( \frac{T_2}{T_1} \right)$