## EE301 Midterm \#1

1. Enter your name, student ID number, e-mail address, and signature in the space provided on this page, NOW!
2. This exam has two parts.

Part I consists of three questions, whose answers you need not justify. Enter the answers to Part I on Page 2, which is provided to you separately for your convenience. When you return your exam, simply place Page 2 on top of the rest of the your exam.
Make sure you enter your name, student ID number and e-mail address in the space provided on that page, NOW!
Part II consists of two problems. Unless otherwise instructed, justify your answers to these problems completely. Please note that answers provided without justification to those problems requiring a full justification will be given zero credit.
3. You have one hour.
4. There are 11 pages in the exam booklet (including Page 2). Use the back of each page for rough work, if necessary.
5. You are not allowed the use of crib sheets.
6. You are not allowed the use of calculators.
7. Tip: Make sure you read through the exam once before beginning. Work as quickly and efficiently as you can. If you get stuck on a certain problem, move on to others.

## IMPORTANT!

Enter the answer to the questions in Part I on Page 2.
In Part II, whenever a certain space is provided for the final answer, be sure to enter your answer there.

Name:
Student ID \#:
E-mail address:
Signature:

## Enter your answers to Part I here

## Problem 1: (30 points)

For items (a) and (b), enter the numerical values of $E_{\infty}$ and $P_{\infty}$ respectively. For items (c) through ( j ), enter one of the the letters "A" through "H".

Table I

| $(\mathrm{a})$ | $(\mathrm{b})$ | $(\mathrm{c})$ | $(\mathrm{d})$ | $(\mathrm{e})$ | (f) | (g) | (h) | (i) | (j) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $E_{\infty}$ | $P_{\infty}$ | $x_{\text {even }}(t)$ | $x_{\text {odd }}(t)$ | $x(t+1)$ | $x(t-1)$ | $x(2 t+1)$ | $x(2 t+2)$ | $x(1-2 t)$ | $x(2-2 t)$ |
|  |  |  |  |  |  |  |  |  |  |

## Problem 2: (20 points)

Enter "Y" in the Table if you can conclude that the property listed on the left in each row holds for the system listed at the top of the column. Enter "N" if it can be concluded that the property does not hold. (For each case, there is sufficient data to make this decision.)

Every entry in the table is worth 1.5 points. You will get two additional points if all the entries are correct.

Table II

|  | System I | System II |
| :---: | :--- | :--- |
| Memoryless |  |  |
| Invertible |  |  |
| Causal |  |  |
| Stable |  |  |
| Time-invariant |  |  |
| Linear |  |  |

## Problem 3: (10 points)

In the second row of the following table, enter " Y " if the signal corresponding to the item label listed at the top of the column is periodic; enter " N " otherwise. In the third row, enter the fundamental period, if appropriate.

Table III

| Item label | (a) | (b) | (c) | (d) | (e) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Periodic? |  |  |  |  |  |
| Fundamental period <br> (if periodic) |  |  |  |  |  |

Name:
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Signature:

## Questions for Part I

- Enter your answers on Page 2.
- Do not justify your answers.
- No partial credit will be given for any questions in Part I. Therefore work as carefully as you can.

1. (30 points) A continuous-time signal $x(t)$ is shown below.

(a) (4 points) What is the energy in $x(t)$ over the infinite interval, that is, what is $E_{\infty}$ ?
(b) (2 points) What is the power in $x(t)$ over the infinite interval, that is, what is $P_{\infty}$ ?

Eight signals labeled "Signal A" through "Signal H" are shown on the next page. Match these signals with the following eight signals, and enter your answers in Table I. Each entry must be a letter from "A" through "H". Each answer is worth three points.
(c) The even part of $x(t)$, that is, $x_{\text {even }}(t)$.
(d) The odd part of $x(t)$, that is, $x_{\text {odd }}(t)$.
(e) $x(t+1)$.
(f) $x(t-1)$.
(g) $x(2 t+1)$.
(h) $x(2 t+2)$.
(i) $x(1-2 t)$.
(j) $x(2-2 t)$.

Signal A


Signal C


Signal E


Signal G


Signal B


Signal D


Signal F


Signal H

2. (20 points) Determine if each of the following systems (with input $x$ and output $y$ ) is memoryless or with-memory; invertible or non-invertible; causal or non-causal; stable or unstable; time-invariant or time-varying; linear or nonlinear.

Enter your answers in Table II on Page 2. In each entry in the table, write "Y" if you can conclude that the property listed on the left holds for the system listed at the top of the column. Enter "N" if it can be concluded that the property does not hold. (For each case, there is sufficient data to make this decision.)
Every entry in the table is worth 1.5 points. You will get two additional points if all the entries are correct.

## (a) System I:

$$
y[n]=x[n]+x[-n] .
$$

(b) System II:

$$
y(t)=x(t) x(-t) .
$$

3. (10 points) Classify the following signals as periodic or non-periodic; for periodic signals, calculate the fundamental period. Enter your answers in Table III on Page 2.
(a) (2 points) $x(t)=e^{j 5 t}$.
(b) (2 points) $x(t)=t e^{j 5 t}$.
(c) (2 points) $x[n]=e^{j n}$.
(d) (2 points) $x[n]=e^{j \frac{\pi}{8} n}$.
(e) (2 points) $x[n]=e^{j \frac{\pi}{4} n} e^{j \frac{\pi}{8} n}$.

## Questions for Part II

Justify your answers completely. Answers provided without a complete justification may be given zero credit!
4. (20 points)

The impulse response of a discrete-time linear time-invariant system is given by

$$
h[n]=\left\{\begin{aligned}
1 & \text { if } n=0 \\
-1 & \text { if } n=1 \\
0 & \text { otherwise }
\end{aligned}\right.
$$

A plot of $h[n]$ is shown below.

(a) (5 points)

Let $x[n]$ be an input to this LTI system. Let $y[n]$ be the corresponding output. Find real numbers $\alpha, \beta$ and $\gamma$ such that

$$
y[n]=\alpha x[n+1]+\beta x[n]+\gamma x[n-1] .
$$

(b) (5 points)

Is the system causal? Completely justify your answer.
(c) (10 points) The input to the LTI system is

$$
x[n]= \begin{cases}1 & \text { if } n=-1 \\ 1 & \text { if } n=0 \\ 0 & \text { otherwise }\end{cases}
$$

A plot of $x[n]$ is shown below, for your convenience.


Find the output $y[n]$, and plot it in the space shown below. Show all work.

5. (20 points)

For a discrete-time LTI system, you are given that when the input signal is

$$
x[n]= \begin{cases}1 & \text { if } n=0 \\ 1 & \text { if } n=1 \\ 0 & \text { otherwise }\end{cases}
$$

the output signal is

$$
y[n]=\left\{\begin{array}{cl}
0 & \text { if } n<0 \\
\left(\frac{1}{2}\right)^{n} & \text { if } n \geq 0
\end{array}\right.
$$

(a) (10 points) Find the output $y_{1}[n]$ of the system when the input is

$$
x_{1}[n]=\left\{\begin{aligned}
1 & \text { if } n=0 \\
0 & \text { if } n=1 \\
-1 & \text { if } n=2 \\
0 & \text { otherwise }
\end{aligned}\right.
$$

(b) (10 points) You are given that the impulse response satisfies

$$
h[n]=0, \quad \text { for } \quad n<0 .
$$

Find the numerical values of

$$
h[0], \quad h[1], \quad h[2], \quad h[3], \quad \text { and } \quad h[4] .
$$

