

# 4D X-Ray CT Reconstruction using Multi-Slice Fusion

Soumendu Majee<sup>1</sup>

Thilo Balke<sup>1</sup>

Craig A. J. Kemp<sup>2</sup>

Gregery T. Buzzard<sup>3</sup>

Charles A. Bouman<sup>1</sup>

<sup>1</sup>*School of ECE, Purdue University, IN, USA*

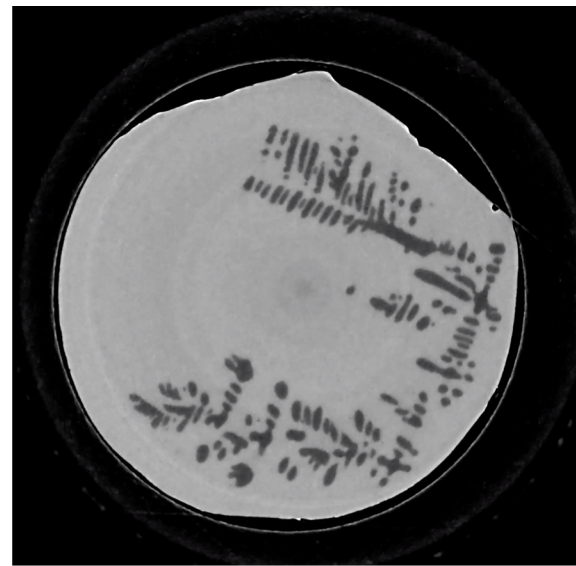
<sup>2</sup>*Eli Lilly and Company, Indianapolis, IN, USA*

<sup>3</sup>*Department of Mathematics, Purdue University, IN, USA*

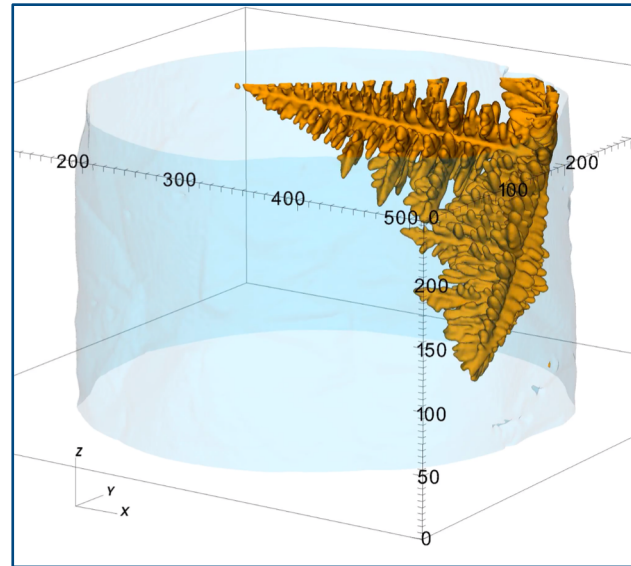


- Eli Lilly and Company research project funding agreement 17099289
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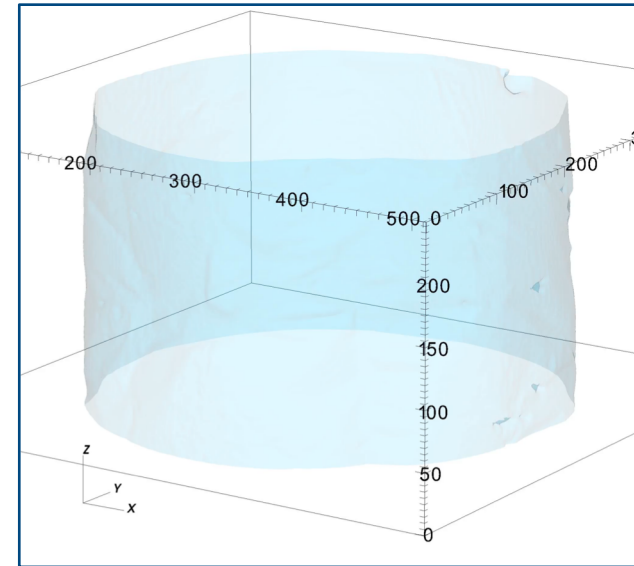
# What is 4D (or High-D) Reconstruction?



2D: Image



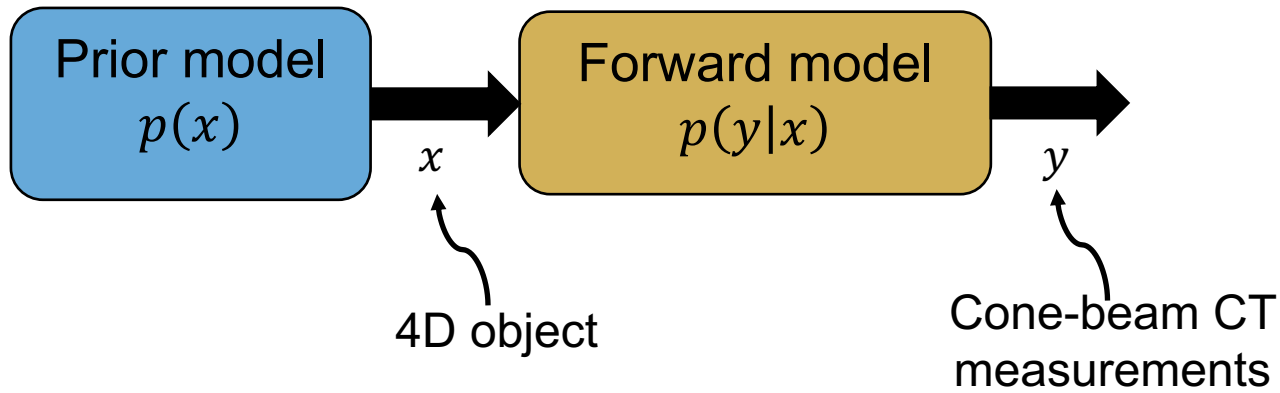
3D: Volume



4D: Volume + time

- Reconstruct objects in many dimensions:
  - 4D: Space + time
  - 5D: Space + time + parameters (e.g., heart + respiration phase)
- Advantages:
  - Reduce data
  - Increase temporal resolution

# MBIR for 4D CT Reconstruction



- Forward model:

$$f(x) = -\log p(y|x)$$

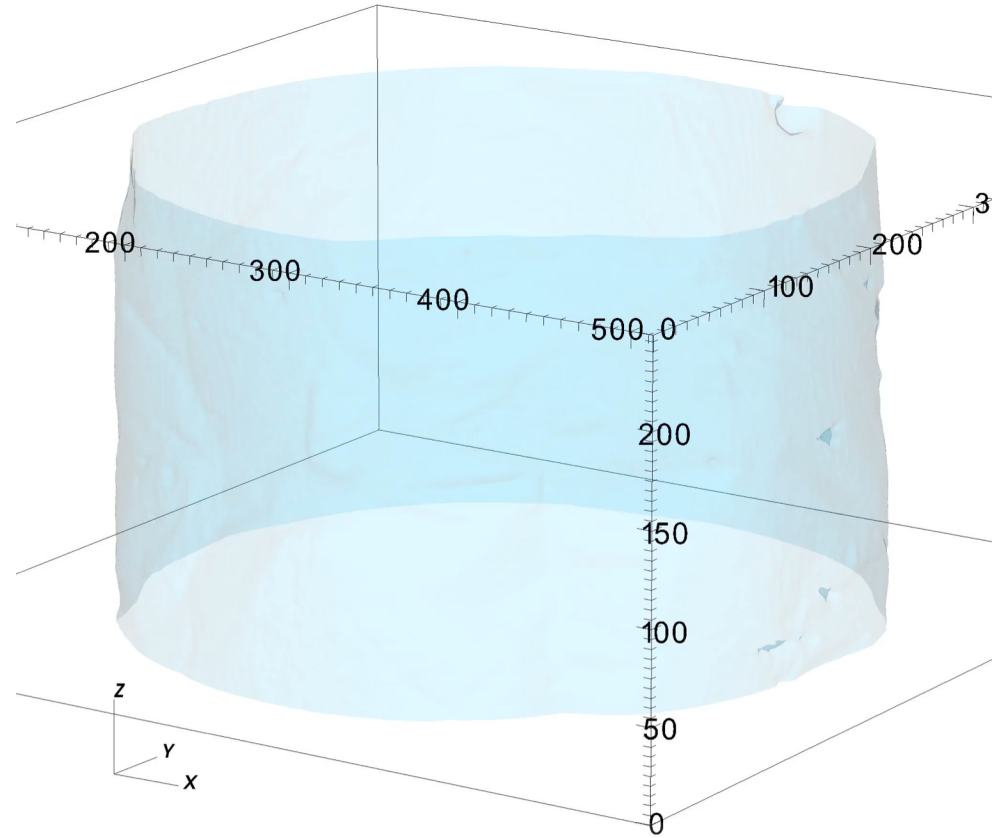
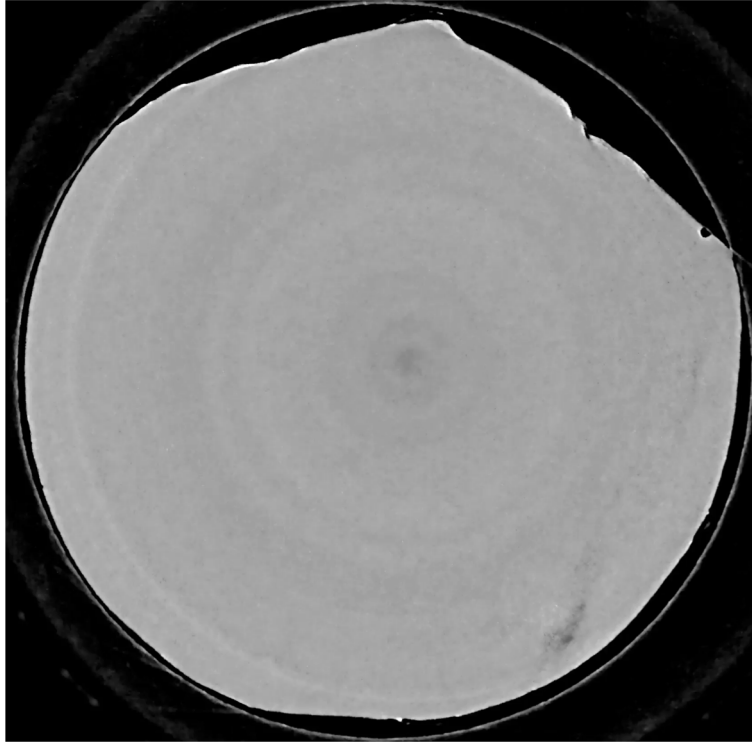
- 4D Prior model:

$$h(x) = -\log p(x)$$

- 4D MBIR reconstruction:

$$\hat{x} \leftarrow \arg \min_x \{f(x) + h(x)\}$$

# Previous Work on 4D MBIR Reconstruction



## TIMBIR:

- Showed 16x increase in temporal resolution
- Based on simple 4D MRF prior

*Can we do better with advanced 4D priors?*

# Designing Advanced 4D Prior Model

## Challenges:

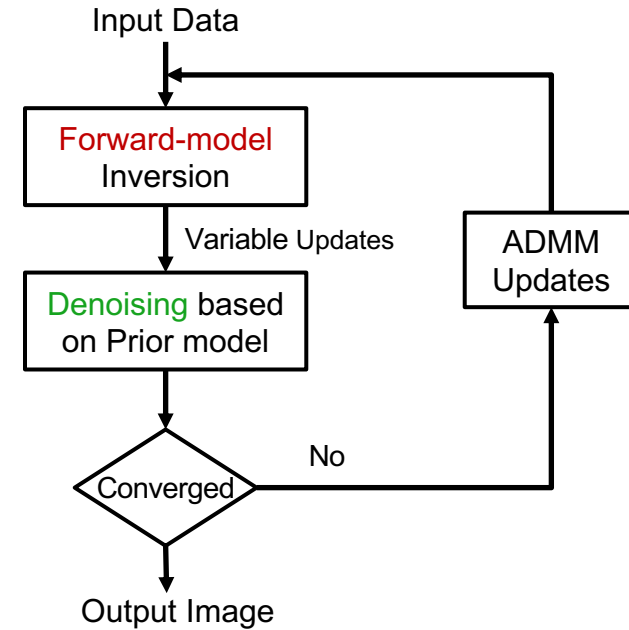
- 4D (or high-D) prior modeling is difficult!
- Curse of dimensionality: In 5D, each voxel has 242 neighbors!
- Prior model is often more computation than forward model!

## Approach:

- Use CNNs to build advanced 4D prior model
- CNNs are fast and very effective at modeling complex data
- Heterogeneous CPU/GPU computing with TensorFlow libraries

# How to Incorporate a CNN Prior?

- Plug & Play Priors:
  - CNN denoiser functions as prior model
  - Variations: P&P-ADMM, RED, P&P-FISTA
  - Alternate reconstruction and denoising

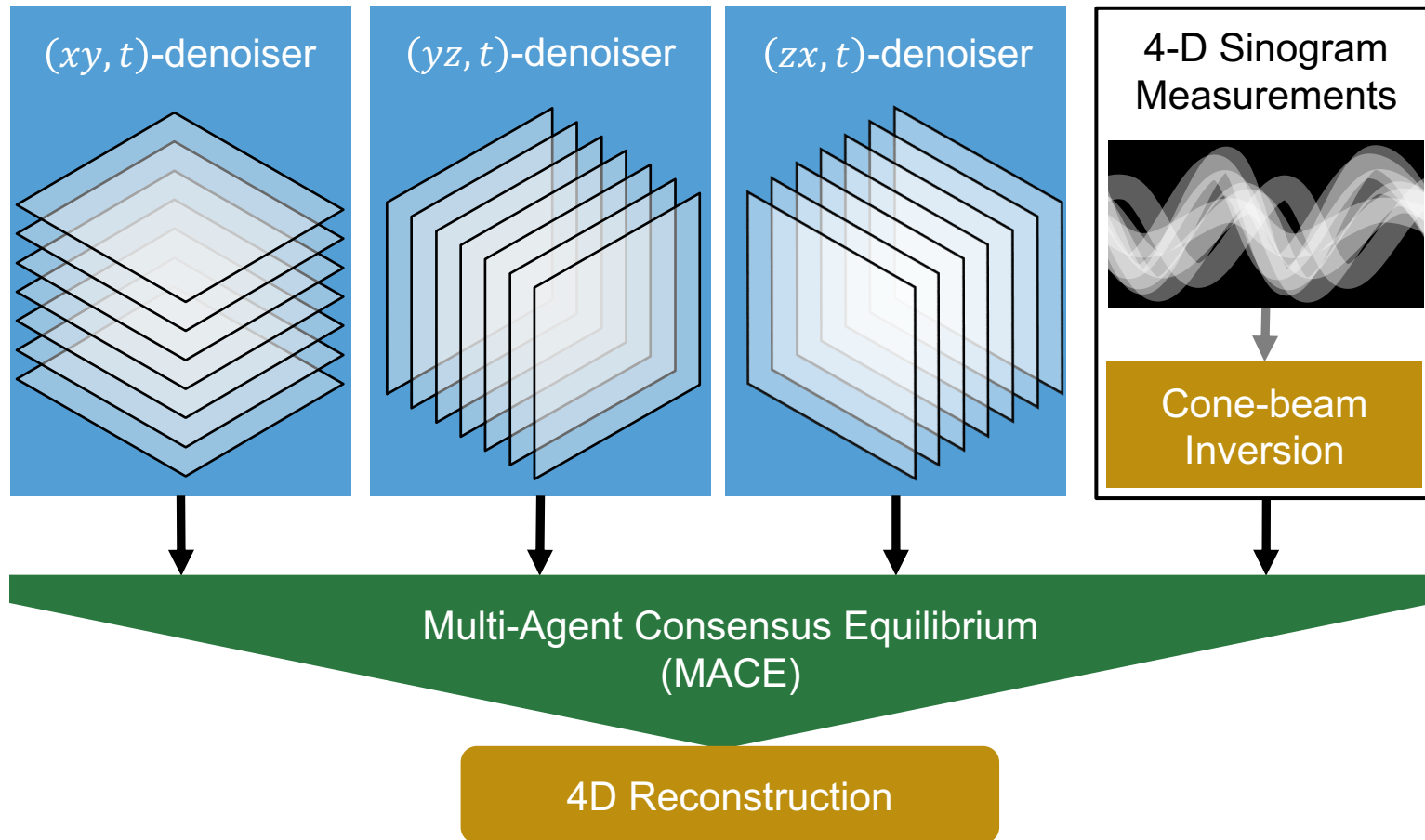


- **Problem:** 4D CNN denoising is difficult
  - 4D convolutions require 6D kernels: computationally expensive
  - No GPU accelerated routines from major Deep Learning vendors
  - 4D training data difficult to obtain

*Can we build 4D prior from 2D convolutions?*

# Multi-Slice Fusion using MACE

## Multi-Slice Fusion

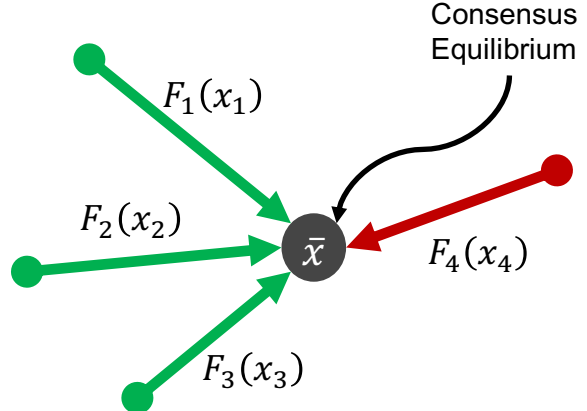


- Fuse multiple low-D CNN denoisers to implement 4D prior
- Use 2D convolutions: fast and implementable
- No 4D training data required

# Intro to MACE Model Fusion

How does MACE work?

- Generalization of Plug & Play
- Can fuse multiple models
- Can be viewed as a force balance equation



MACE equilibrium equations:

$$L(X) = G(X)$$

where

$$L(X) = \begin{bmatrix} F_1(x_1) \\ F_2(x_2) \\ F_3(x_3) \\ F_4(x_4) \end{bmatrix}, \quad X = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix}; \quad G(X) = \begin{bmatrix} \bar{x} \\ \bar{x} \\ \bar{x} \\ \bar{x} \end{bmatrix}, \quad \bar{x} = \frac{1}{2} \left( \frac{1}{3} \sum_{k=1}^3 x_k + x_4 \right)$$

**Forward model agent**

**Prior model agents**



# Definition of Agents

- **Forward model** agent is a proximal map that fits the data:

$$F_4(x) = \operatorname{argmin}_{v \in \mathbb{R}^N} \left\{ -\log p(y|v) + \frac{\beta}{\sigma^2} \|v - x\|_2^2 \right\}$$

- **Prior model** agents are CNN denoising operators:

- $F_1$  denoises in  $(x, y, t)$
  - $F_2$  denoises in  $(x, z, t)$
  - $F_3$  denoises in  $(y, z, t)$
  - $F_1, F_2, F_3$  share same architecture and weights
- 
- CNN denoisers are trained to remove AWGN noise
    - Does not represent measurement noise
    - Artificial noise within MACE framework

# Computing MACE solution

Initial Reconstruction:  $x_1 = x_2 = x_3 = x_4 \in \mathbb{R}^N$

$X \leftarrow W \leftarrow \begin{bmatrix} x_1 \\ \vdots \\ x_4 \end{bmatrix}$

**while** *not converged*

$X \leftarrow \tilde{L}(W; X)$

$Z \leftarrow G(2X - W)$

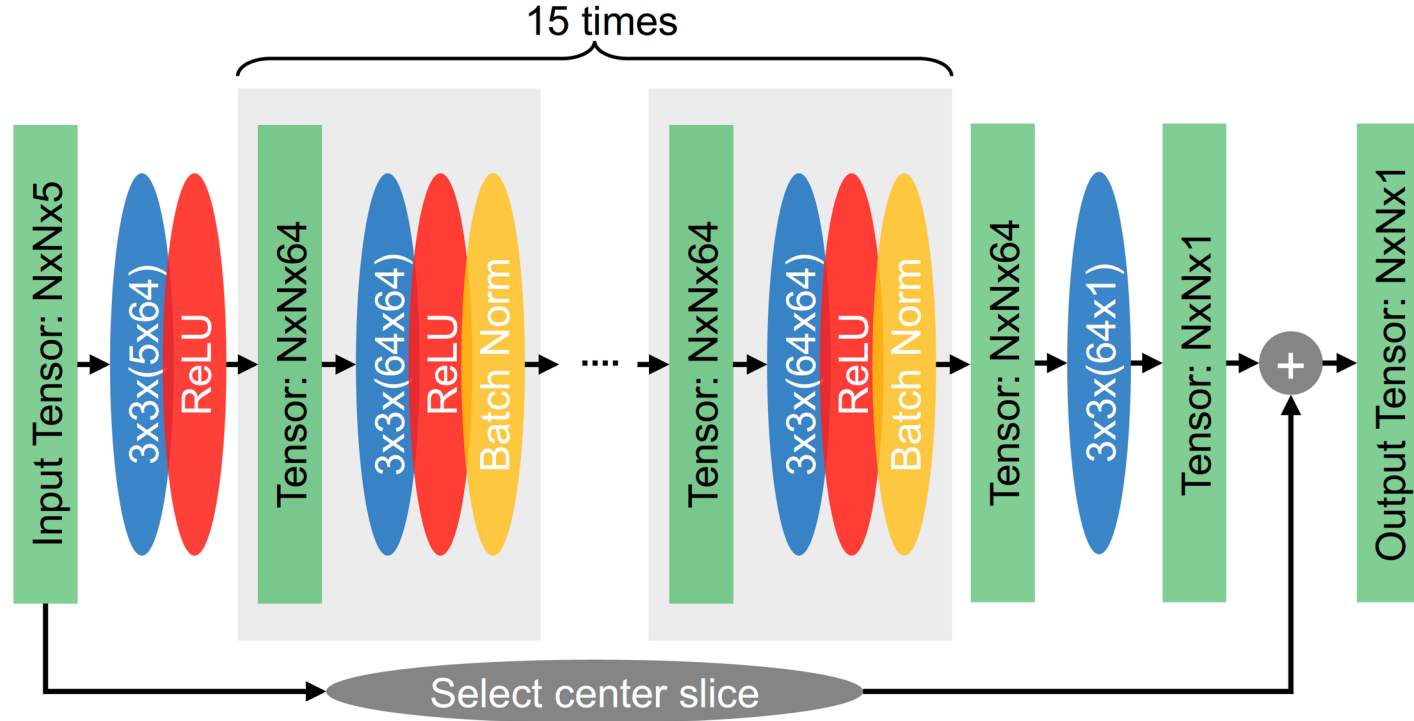
$W \leftarrow W + 2 \rho(Z - X)$

Return( $x_1$ )

Other details:

- Uses partial update of  $L(W) \approx \tilde{L}(W; X)$  to reduce computation
- The parameter  $\rho \in (0,1)$  can be adjusted to speed convergence
- Special case: two agents and  $\rho = 0.5$  equivalent to ADMM
- CNN agents ran on GPUs, and inversion agents ran on CPUs

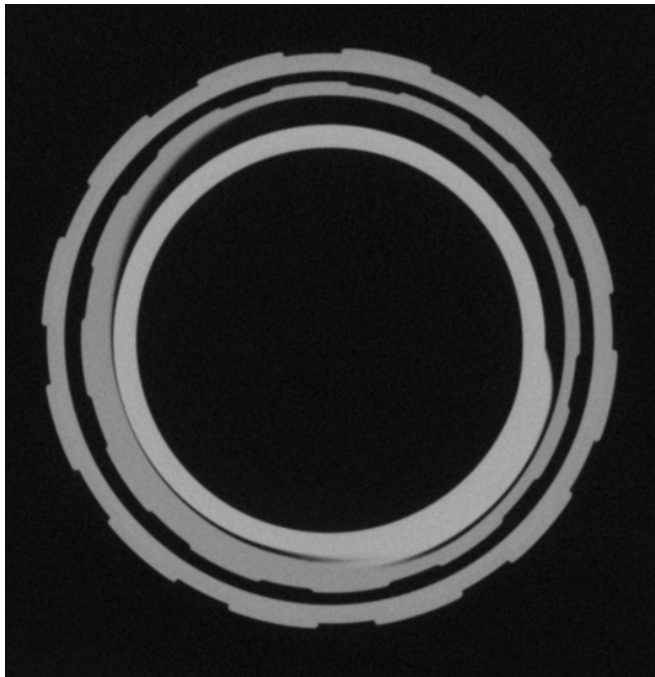
# 2.5D CNN Denoiser Architecture



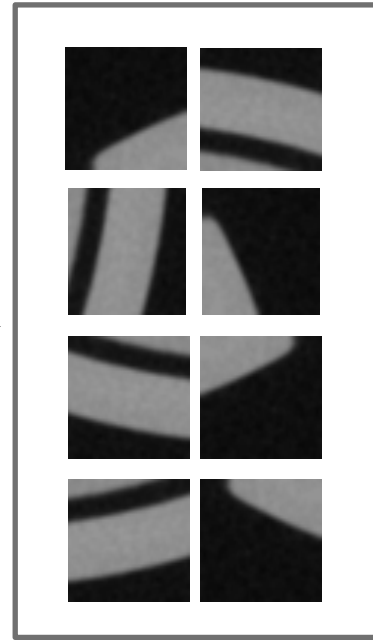
## Network Architecture

- 17 Layer residual network
- 2.5-D: Multiple 2-D slices passed as input channels
- Denoises center slice of 5 adjacent time points
- Denoises full volume with a moving window

# Training CNN Denoisers



Typical CT volume

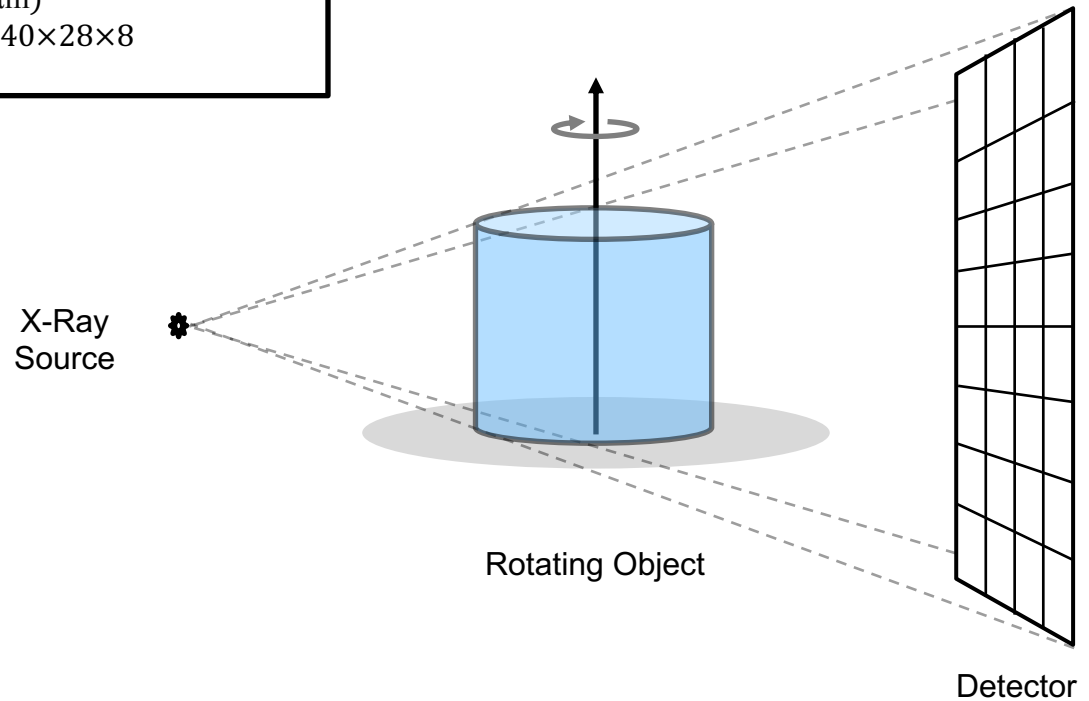


Patches of size  $40 \times 40 \times 5$

1. Extract patches
2. Add synthetic AWGN noise to patches
3. Train CNN to remove noise

# Simulated Experimental Setup

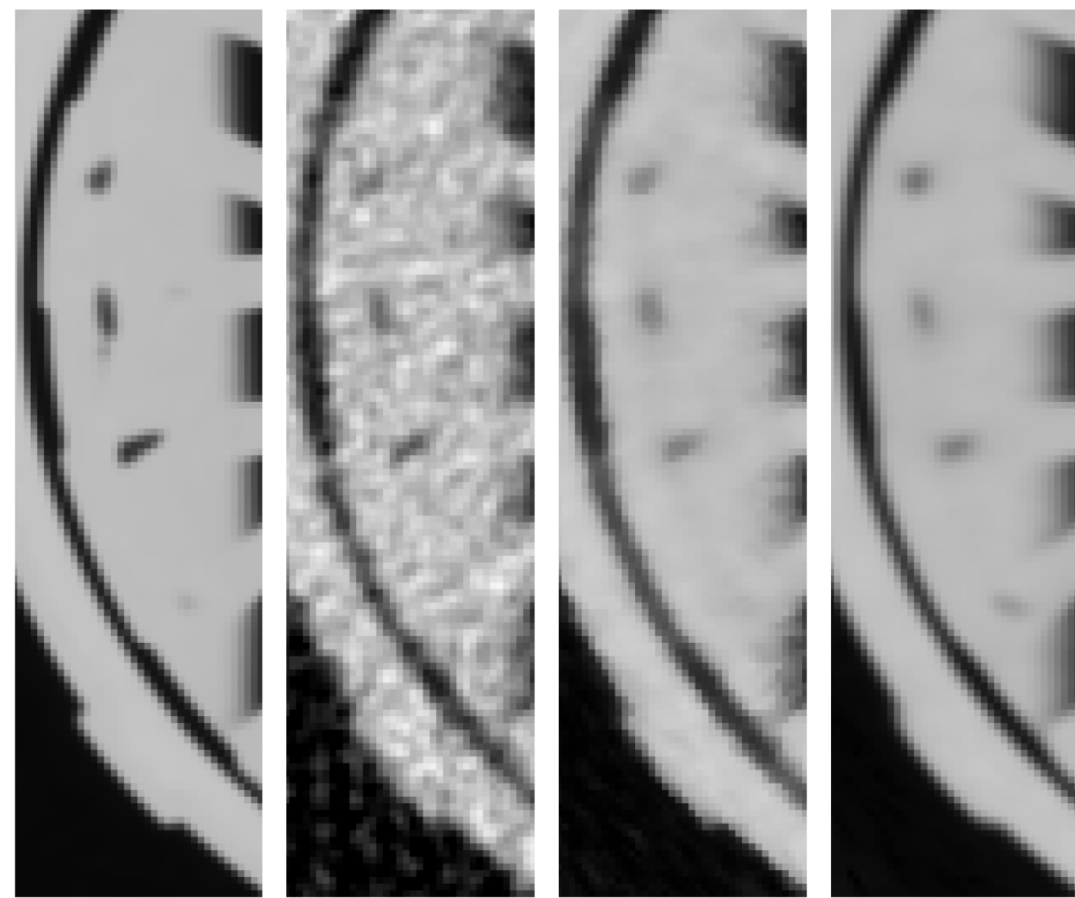
<b>Source-Detector Distance</b>	839 mm
<b>Magnification</b>	5.57
<b>Cropped Detector Array</b>	$240 \times 28, (0.254 \text{ mm})^2$
<b>Detector resolution at ISO</b>	$45.7 \mu\text{m}$
<b>Number of Views per Rotation</b>	75
<b>Voxel Size</b>	$(45.7 \mu\text{m})^3$
<b>Reconstruction Size <math>(x, y, z, t)</math></b>	$240 \times 240 \times 28 \times 8$



## Procedure:

1. Generate 3D phantom
2. Translate 3D phantom to generate 4D phantom
3. Forward project phantom to generate sinograms
4. Reconstruct from sinograms
5. Compare with phantom

# Simulated Results: Qualitative Comparison



Phantom

FBP (3D)

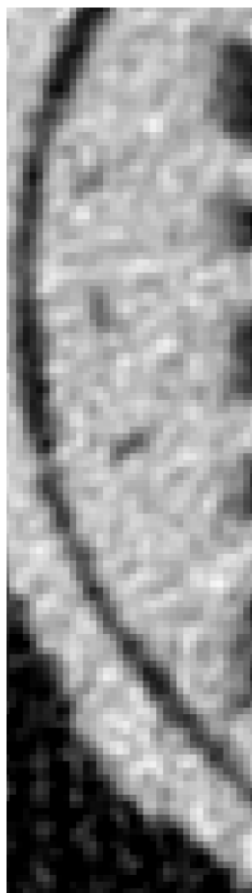
4D MBIR

Multi-Slice  
Fusion

# Simulated Results: Qualitative Comparison



Phantom



FBP (3D)



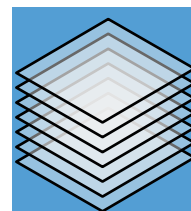
4D MBIR



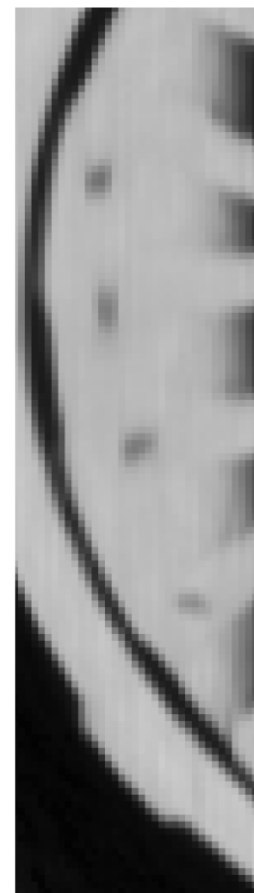
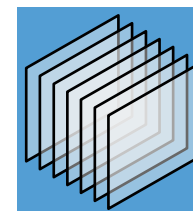
Multi-Slice  
Fusion



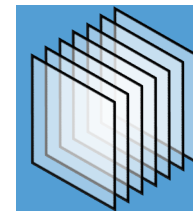
CNN  
 $(xy, t)$



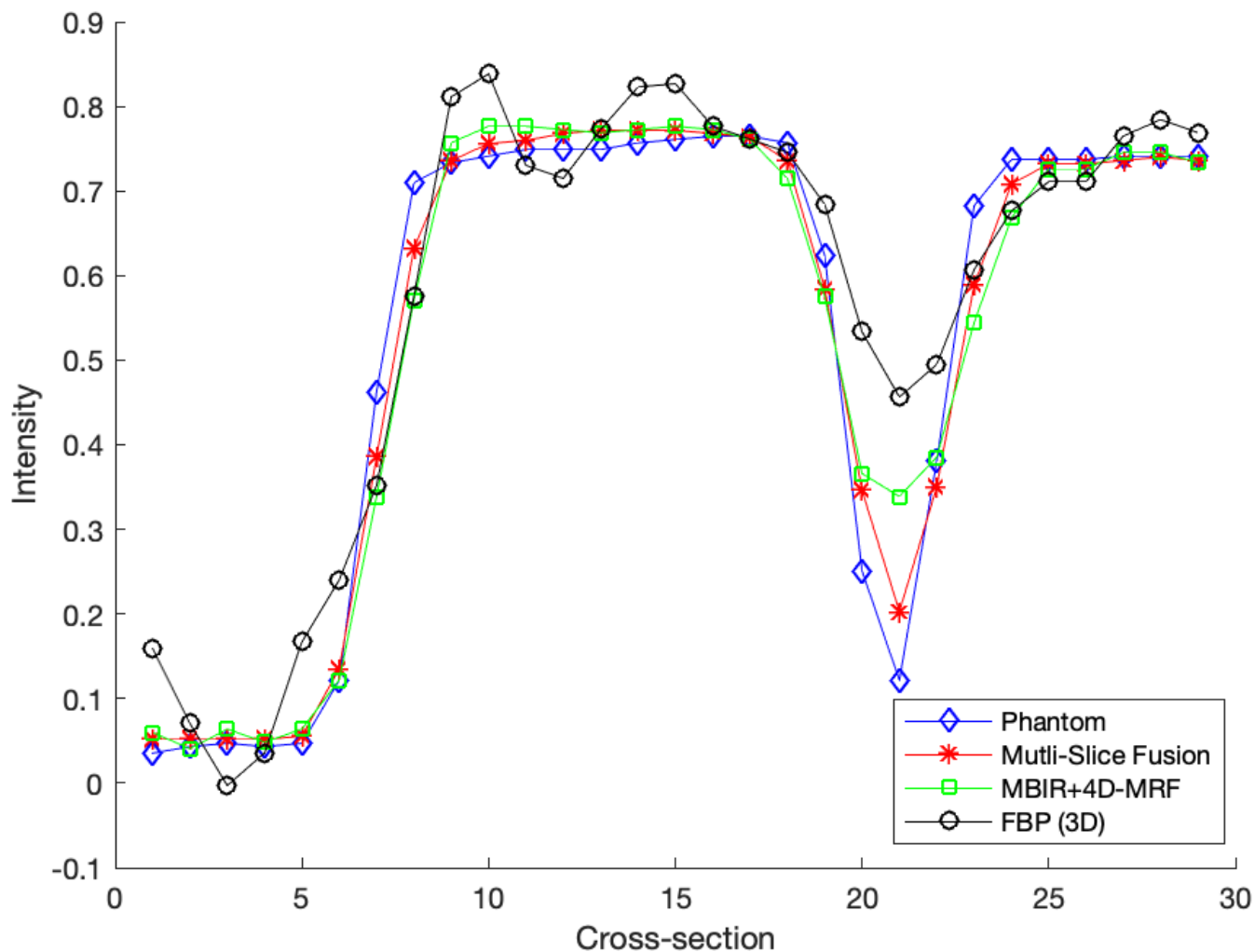
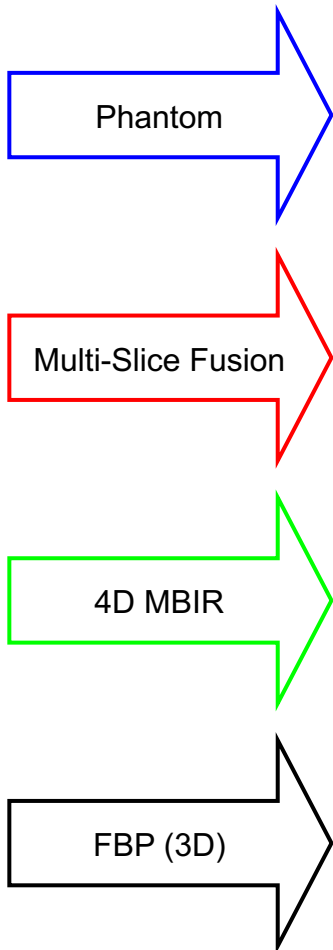
CNN  
 $(yz, t)$



CNN  
 $(zx, t)$



# Simulated Results: Cross-Section



Multi-Slice Fusion: most accurate reconstruction of gap



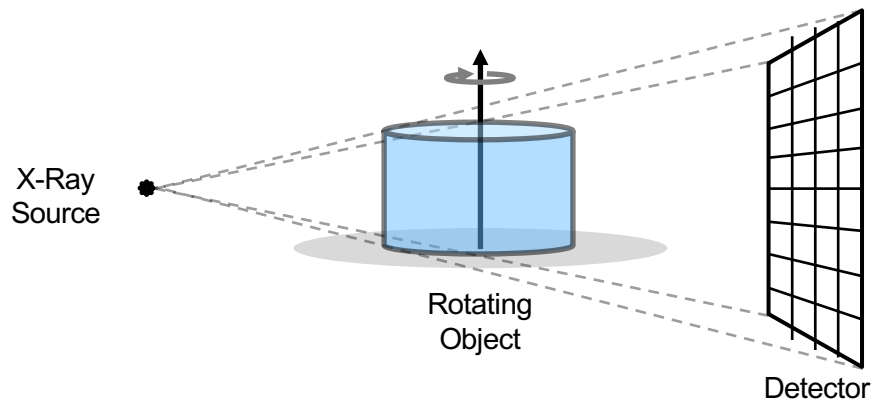
# Simulated Results: Quantitative Metrics

Method	PSNR(dB)	SSIM
FBP	19.690	0.609
MBIR+4D-MRF	25.837	0.787
Multi-Slice Fusion	<b>29.071</b>	<b>0.943</b>
MBIR+ $H_{xy,t}$	29.026	0.922
MBIR+ $H_{yz,t}$	28.040	0.932
MBIR+ $H_{zx,t}$	28.312	0.926

- PSNR and SSIM is computed for each method with respect to the phantom
- Multi-Slice Fusion achieves highest PSNR and SSIM metrics

# Experimental Setup

<b>Scanner Model</b>	North Star Imaging X50
<b>Source-Detector Distance</b>	839 mm
<b>Magnification</b>	5.57
<b>Cropped Detector Array</b>	$731 \times 91, (0.254 \text{ mm})^2$
<b>Detector resolution at ISO</b>	$45.7 \mu\text{m}$
<b>Number of Views per Rotation</b>	150
<b>Voxel Size</b>	$(45.7 \mu\text{m})^3$
<b>Reconstruction Size <math>(x, y, z, t)</math></b>	$731 \times 731 \times 91 \times 16$



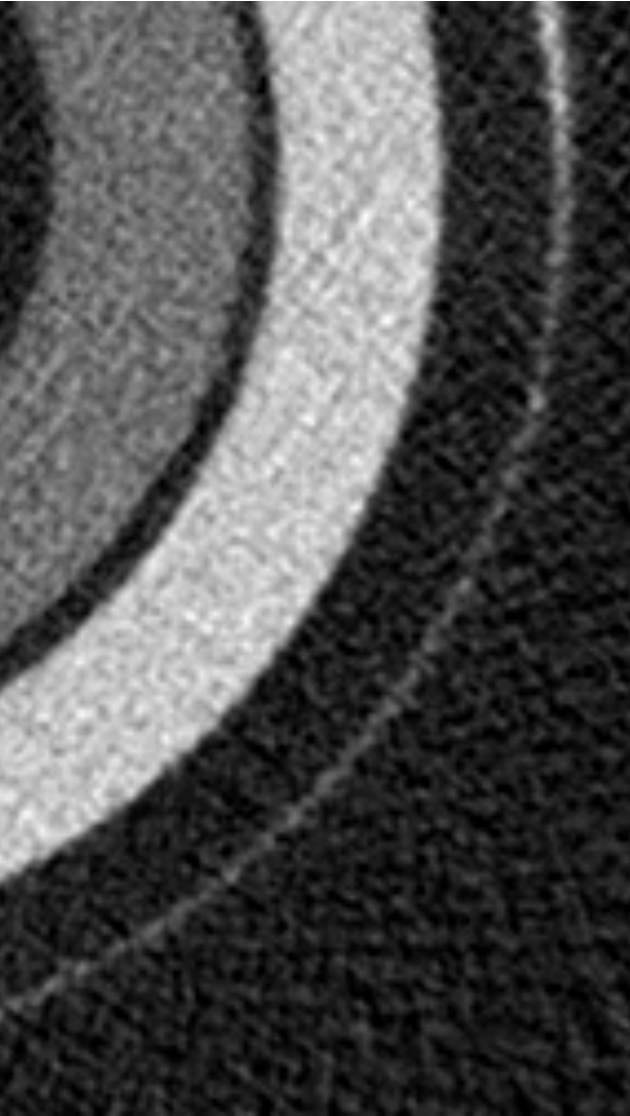
Other details:

- Object held in place by fixtures: artifacts
- All 4D results undergo preprocessing to correct for jig artifacts

# Results: Dynamic 3D Rendering



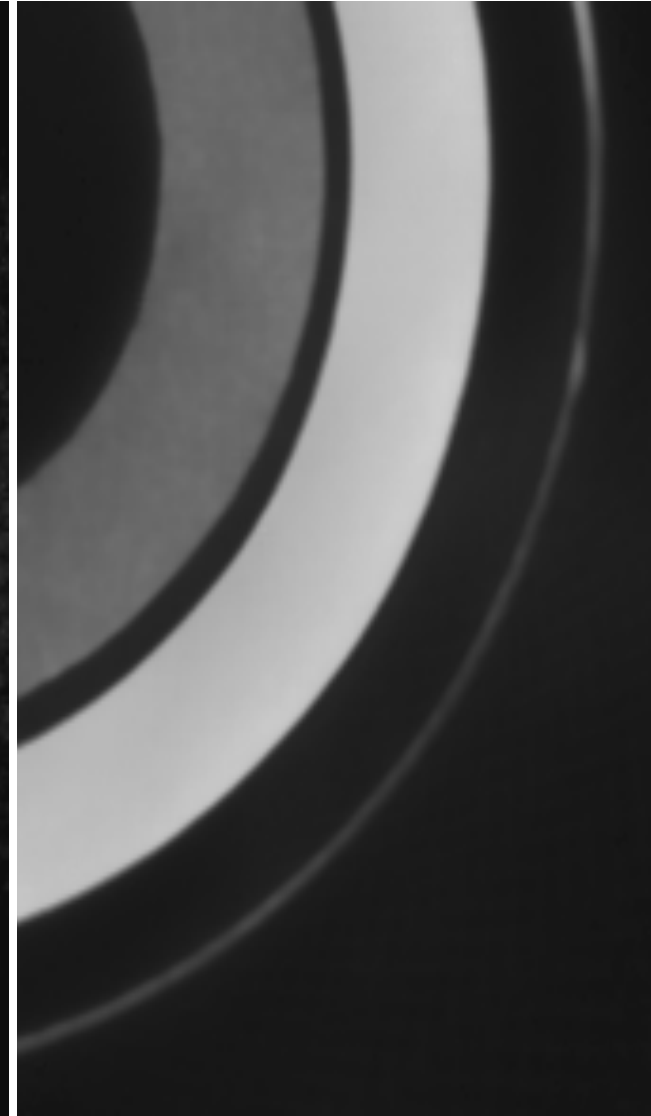
# Results: Qualitative Comparison



FBP (3D)



4D MBIR  
(MBIR with 4D MRF prior model)

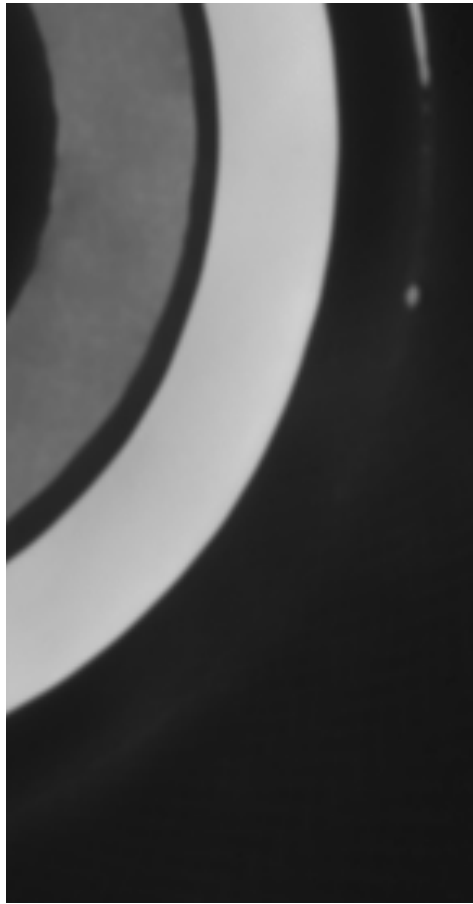


Multi-Slice Fusion

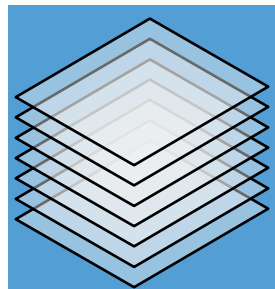
# Results: Effect of Model Fusion



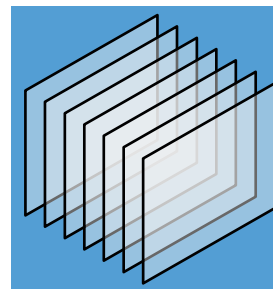
Multi-Slice Fusion



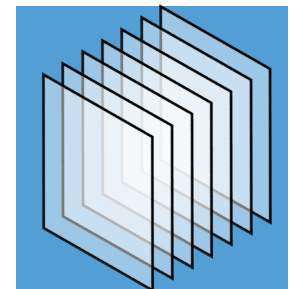
CNN along  $(xy, t)$



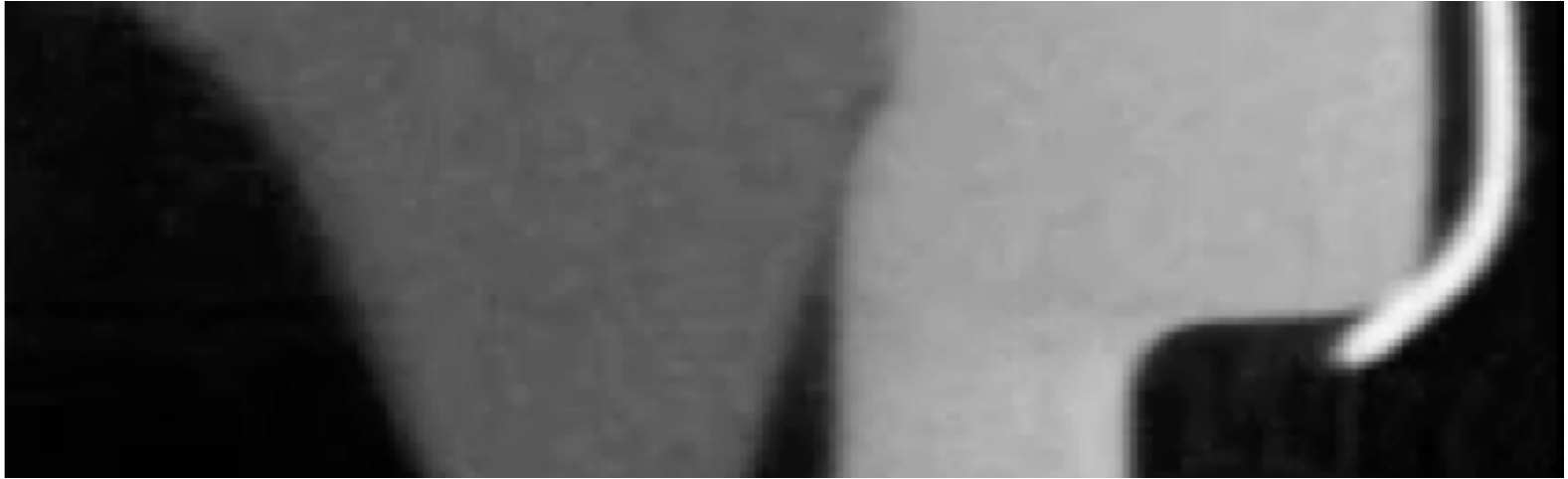
CNN along  $(yz, t)$



CNN along  $(zx, t)$



# Results: Qualitative Comparison (Time-Space)

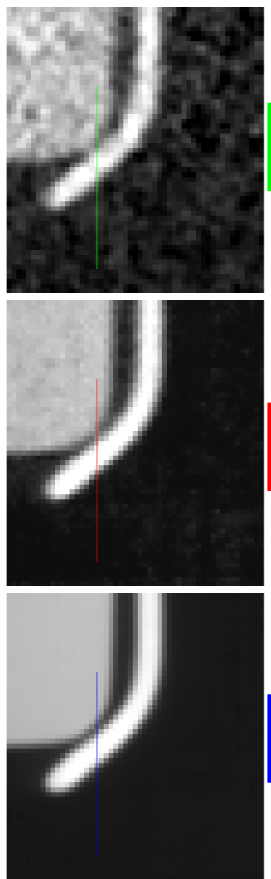


4D MBIR  
(MBIR with 4D MRF prior model)



Multi-Slice Fusion  
(Uses three 2.5D CNN priors with MACE model fusion)

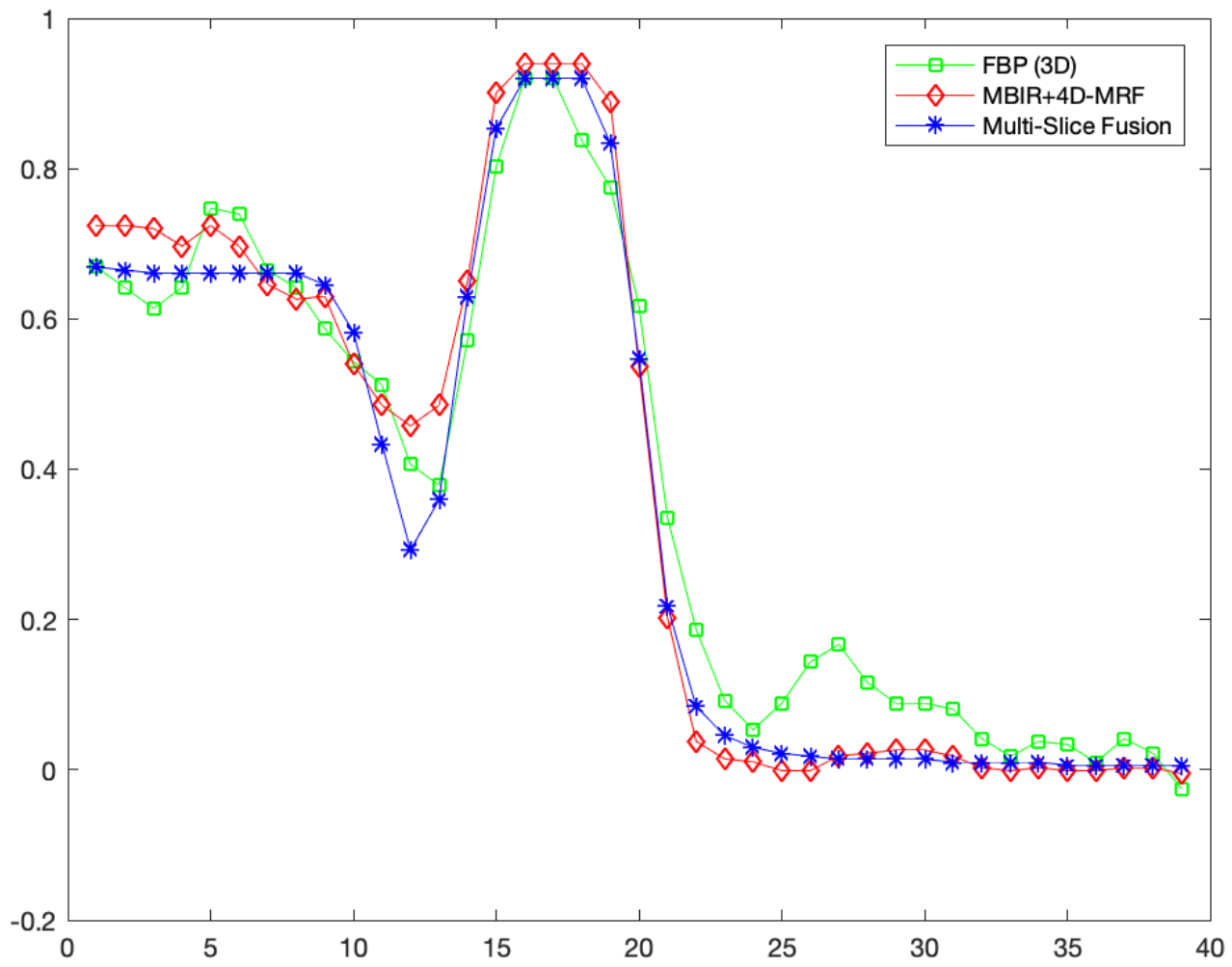
# Results: Cross-Section



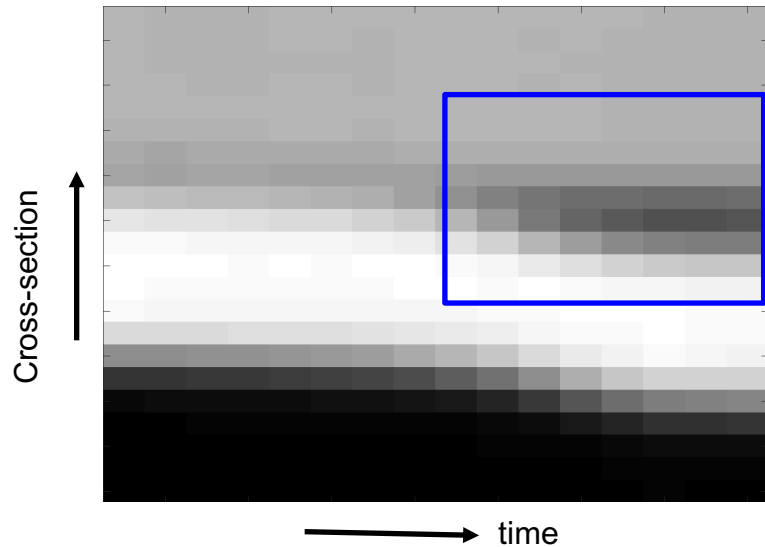
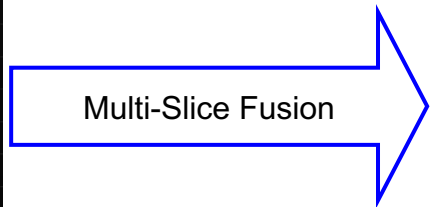
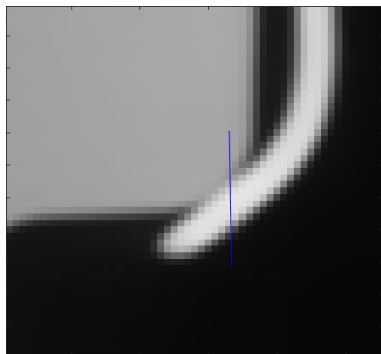
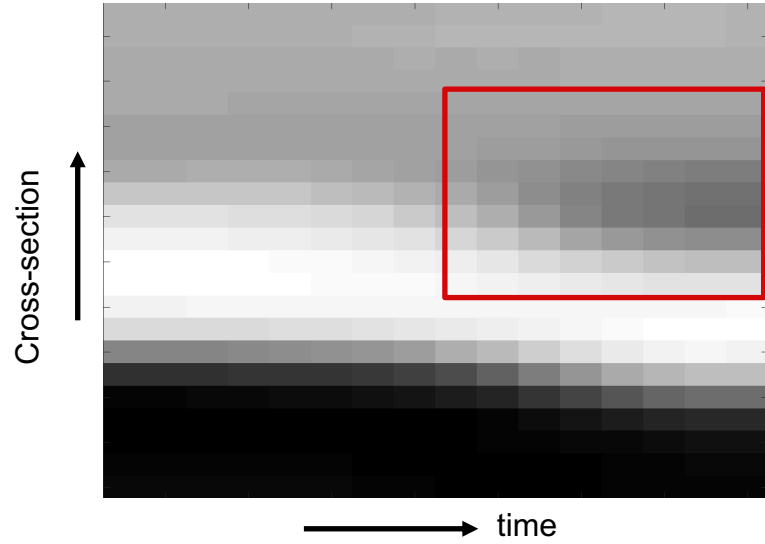
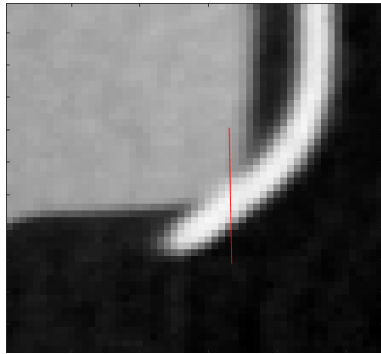
FBP (3D)

4D MBIR

Multi-Slice Fusion



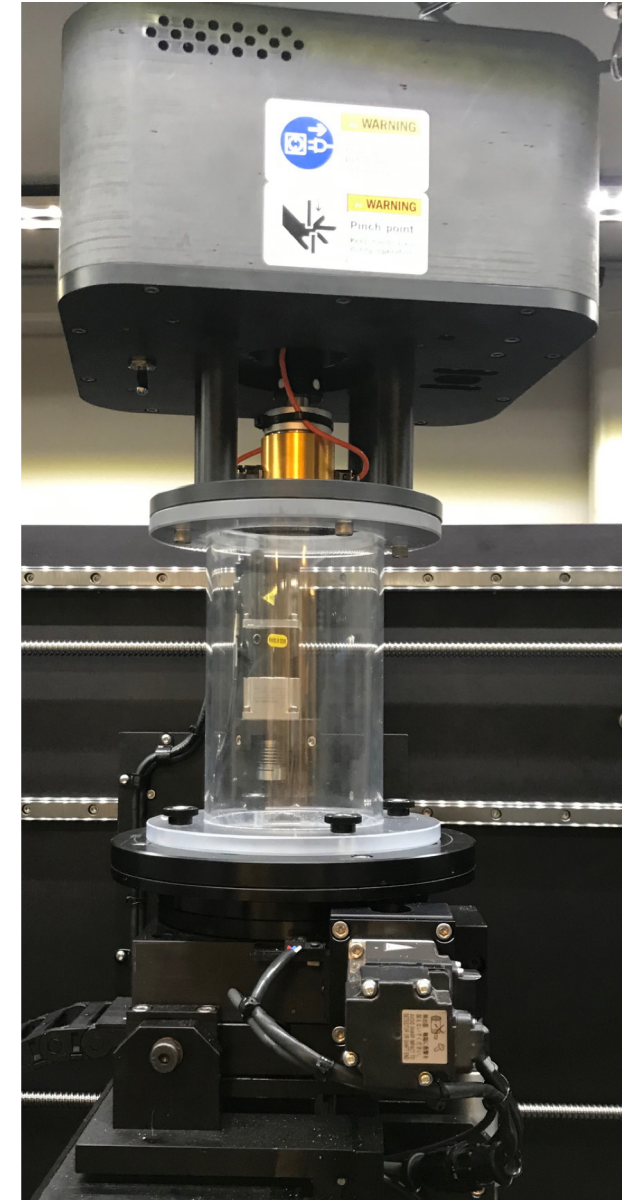
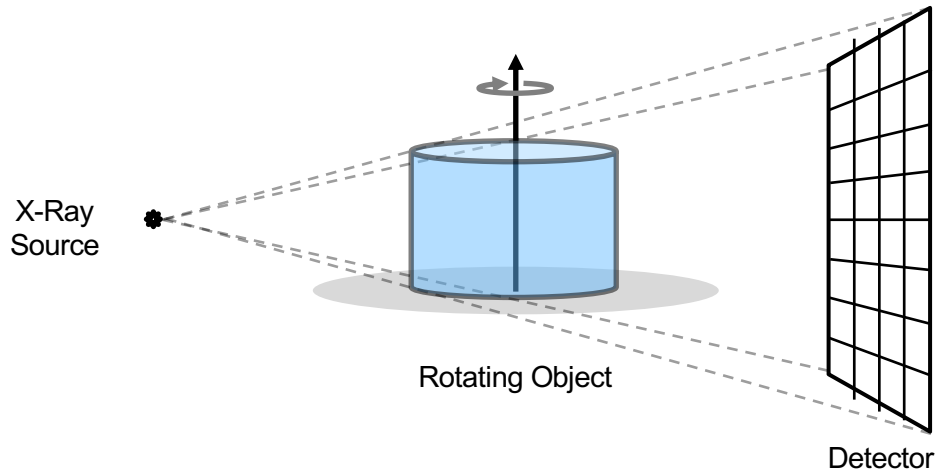
# Results: Temporal Resolution



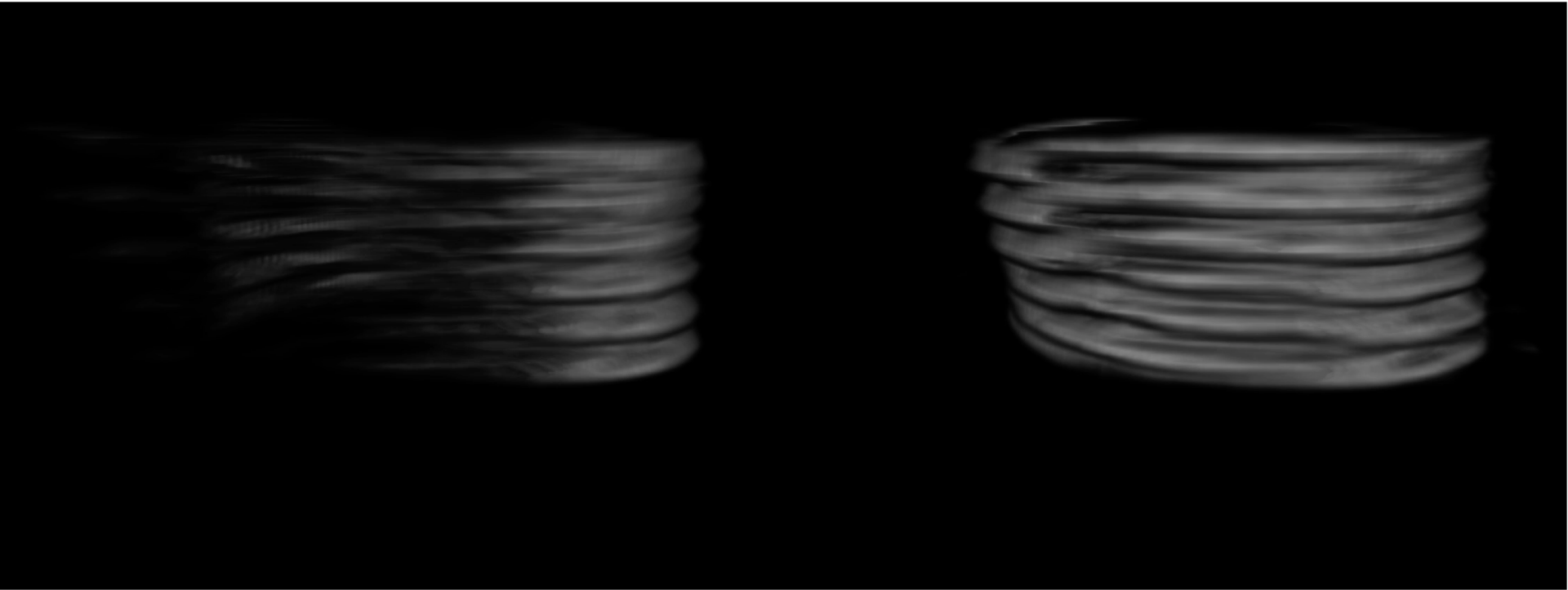


# Experimental Setup: Narrow Angle CT

<b>Scanner Model</b>	North Star Imaging X50
<b>Source-Detector Distance</b>	694 mm
<b>Magnification</b>	2.83
<b>Cropped Detector Array</b>	$300 \times 768, (0.254 \text{ mm})^2$
<b>Detector resolution at ISO</b>	$89 \mu\text{m}$
<b>Number of Views per Rotation</b>	144
<b>Voxel Size</b>	$(89 \mu\text{m})^3$
<b>Reconstruction Size <math>(x, y, z, t)</math></b>	$300 \times 300 \times 768 \times 12$



# Results: Narrow Angle CT



FBP (3D)

Multi-Slice Fusion

Each frame reconstructed from disjoint view-sets of 90-degrees

# Conclusion

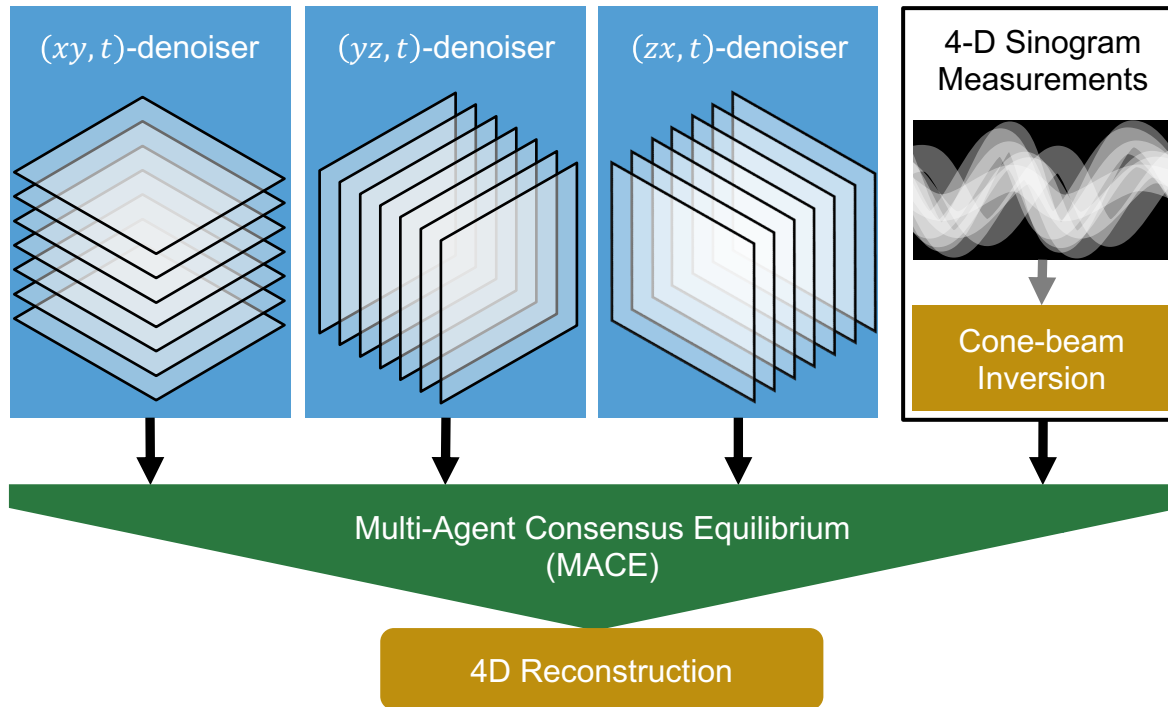


Image Quality can be dramatically improved with:

- 4D reconstruction
- Advanced CNN priors

Multi-slice fusion using MACE:

- Makes high-D priors practical to implement
- Results in smooth reconstruction along all dimensions