

# A Model-Based 3D Multi-slice Helical CT Reconstruction Algorithm for Transportation Security Application

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**Abstract**—Multi-slice helical CT is widely used for baggage inspection in transportation security due to its fast acquisition speed and large scan coverage. In addition, recent studies indicate that model-based reconstruction has the potential to improve image quality and reduce artifacts relative to traditional filtered backprojection (FBP) method. In this paper, we present the results of a 3D model-based reconstruction algorithm on multi-slice helical scan data taken of actual baggage with high and low density objects. We compared our reconstruction results to conventional FBP reconstructions and illustrated the potential value of our algorithm in terms of image quality and artifact reduction.

## I. INTRODUCTION

Computed tomography (CT) is widely used in transportation security applications [1], [2]. Among various CT scanner geometries, multi-slice helical CT has come into wide use due to its fast acquisition and large scan coverage. In fact, many airports have installed multi-slice helical CT systems as a central component of baggage screening. However, the more complex geometry of multi-slice helical CT also poses challenges in reconstruction. For example, as cone angles become wider, there is an increasing need to use true 3D reconstruction methods in order to avoid the image artifacts introduced by 2D approximations.

Moreover, the task in transportation security is quite different from the medical problem. In the medical application, it is critical to preserve fine details of soft tissue structure; however, in the security application, typically it is more important to obtain precise estimates of object boundary and its average density. Also, in security, the objects of greatest interest typically have densities that are substantially greater than water.

Recently, model-based reconstruction (MBR) algorithms have been shown to be effective in the reconstruction of multislice helical scan CT data [3]. These algorithms have the advantage that they can incorporate more detailed models of both the scanner and the objects being reconstructed. In addition, they offer flexibility in the application of transportation security since they allow for more accurate reconstruction for nontraditional geometries, such as with limited view data [4]. Model-based algorithms have the potential to more accurately

account for a wide array of scanner characteristics including photon counting and electronic noise, beam hardening, metal attenuation and scatter, and the detector point-spread function. More accurate modeling of the scanner can be used to reduce streaking artifacts from high density objects, which can be particularly problematic in the security imaging application. In addition, the MBR method incorporates a prior model that can be tuned to the characteristics of typical objects and the performance metrics of interest.

In this paper, we apply the methods of 3D model-based reconstruction (MBR) to the problem of transportation security imaging. Our approach is based on maximum a posteriori (MAP) reconstruction along with the iterative coordinate descent (ICD) optimization method. We also describe how our algorithm can be parallelized on multicore processing hardware.

In our results, we present 3D MBR cross-sections from real multislice helical scan data of travel bags packed with a variety of high and low density objects. Our results indicate that MBR has the potential to produce reconstructions with fewer artifacts than analytic reconstruction methods.

## II. STATISTICAL MODEL FOR IMAGE RECONSTRUCTION

Let  $x \in \mathbb{R}^M$  be the image vector, and let  $y \in \mathbb{R}^N$  be the vector of projection measurements. We assume  $x$  and  $y$  are related by a linear sparse matrix operator  $A$ ,

$$y = Ax \quad (1)$$

The matrix coefficient  $A_{ij}$  reflects the formation of  $i$ -th projection by  $j$ -th voxel.

In the Bayesian statistical framework, both  $x$  and  $y$  are considered as random, and the reconstruction is most commonly computed as the maximum a posteriori (MAP) estimate given by

$$\hat{x} = \arg \min_{x \geq 0} \{-\log p(y|x) - \log p(x)\} \quad (2)$$

where  $p(y|x)$  is the likelihood term corresponding to the forward projection model and  $p(x)$  is the prior distribution of  $x$ . Also notice that we impose a positivity constraint on the image.

Given the image  $x$ , the received photon count  $\lambda_i$  of the  $i$ -th projection follows a Poisson distribution with mean

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$\lambda_{T,i}e^{-A_{i*}x}$  where  $\lambda_{T,i}$  is the photon count of the  $i$ -th projection obtained in an air calibration scan. The line integral of  $i$ -th projection can then be obtained by  $y_i = \log\left(\frac{\lambda_{T,i}}{\lambda_i}\right)$ . Using the second order Taylor expansion, the log likelihood term can be approximated by a quadratic function [5],

$$\log p(y|x) \approx -\frac{1}{2}(y - Ax)^T D(y - Ax) + c(y) \quad (3)$$

where  $D$  is the diagonal matrix with diagonal elements  $D_{i,i}$  which are proportional to the photon counts  $\lambda_i$ , and  $c(y)$  is a term depending only on  $y$ . Notice that in this case, a smaller value of  $\lambda_i$  indicates that the associate projection is less heavily weighted.

The prior distribution  $p(x)$  incorporates knowledge about the object being reconstructed,  $x$ . We will describe the prior model in detail in the next section.

### III. METHOD AND ALGORITHM

#### A. 3D Forward Projection Model

To calculate the projection matrix  $A$ , we use the distance-driven (DD) model [6]. Figure 1 illustrates how the 3D projection geometry is decomposed into the  $z$  axis that falls along the object's translation direction, and the  $xy$ -plane, which is perpendicular to  $z$  [3]. Each voxel is flattened along the dimension most parallel to the detector, and the coefficient  $A_{ij}$  is calculated as the product of  $xy$ -plane projection,  $B_{ij}$ , and  $z$ -direction projection,  $C_{ij}$ .

$$A_{ij} = B_{ij} \times C_{ij} \quad (4)$$

The coefficients  $B_{ij}$  and  $C_{ij}$  are calculated as the convolution of the detector response and the flattened voxel profile to yield

$$B_{ij} = \frac{\Delta_{xy}}{\Delta d_c \cos \theta} \text{clip} \left[ 0, \frac{W_c + \Delta d_c}{2} - |\delta_c|, \min(W_c, \Delta d_c) \right] \quad (5)$$

$$C_{ij} = \frac{1}{\Delta d_r \cos \phi} \text{clip} \left[ 0, \frac{W_r + \Delta d_r}{2} - |\delta_r|, \min(W_r, \Delta d_r) \right] \quad (6)$$

where  $W$  denotes the voxel's width when projected onto the detector,  $\Delta d$  denotes the detector width, subscript  $c$  and  $r$  denote channel and row respectively,  $\theta$  and  $\phi$  are the ray angles in  $xy$ -plane and  $z$ -direction, and  $\tilde{\theta}$  is the adjusted ray angle defined by

$$\tilde{\theta} = \left( \theta + \frac{\pi}{4} \right) \bmod \frac{\pi}{2} - \frac{\pi}{4}. \quad (7)$$

The function  $\text{clip}$  is defined by  $\text{clip}[a, b, c] = \min(\max(a, b), c)$ .

#### B. Prior Model

We model the image  $x$  as a Markov random field, with a 26-point 3D neighborhood and the following distribution

$$p(x) = \frac{1}{z} \exp \left\{ - \sum_{\{s,r\} \in \mathcal{C}} b_{s,r} \rho(x_s - x_r) \right\} \quad (8)$$

where  $\rho$  is the positive and symmetric potential function and  $\mathcal{C}$  is the set of all pairwise cliques.

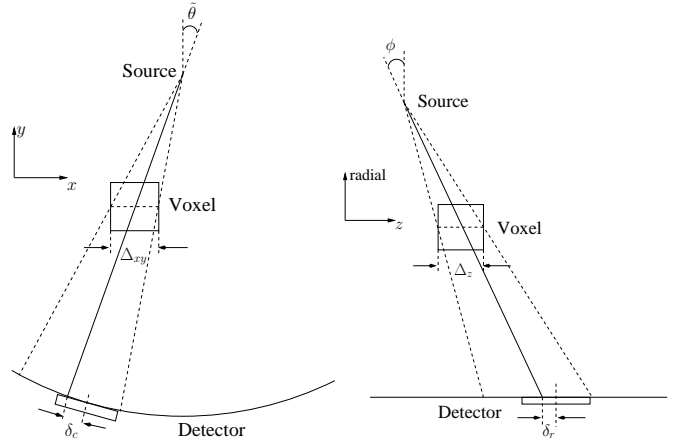


Fig. 1. 3D forward projection geometry used for the distance driven projector.

We studied two different potential functions, given by the  $l_1$  norm prior, which is a special case of generalized Gaussian MRF (GGMRF) [7] when  $p = 1$ ,

$$\rho(\Delta) = |\Delta|, \quad (9)$$

and the  $q$ -generalized Gaussian MRF (q-GGMRF) [3].

$$\rho(\Delta) = \frac{|\Delta|^q}{1 + |\Delta/c|^{q-p}} \quad (10)$$

The q-GGMRF allows more degrees of freedom to control both low-contrast and high-contrast edge characteristics. If  $|\Delta| \ll c$ ,  $\rho(\Delta) \approx |\Delta|^q$  and if  $|\Delta| \gg c$ ,  $\rho(\Delta) \approx |\Delta/c|^p$  where  $c$  is the parameter determining the transition between the two cases. Normally, we will set  $q = 2$  and  $1 < p < q$ . It ensures the overall cost to be convex and, therefore, allows global convergence.

#### C. Optimization

The overall cost function, obtained by combining the approximate log-likelihood and the prior, is

$$\hat{x} = \arg \min_{x \geq 0} \left\{ \frac{1}{2} \|y - Ax\|_D^2 + \sum_{\{s,r\} \in \mathcal{C}} b_{s,r} \rho(x_s - x_r) \right\} \quad (11)$$

We solve this optimization problem using the iterative coordinate descent (ICD) algorithm [5] in which we scan over all voxels and sequentially optimize each voxel while fixing the others. In order to solve the 1D optimization problem resulting from each pixel update, we design a quadratic substitute functional  $q(\Delta; \Delta')$  that upper bounds  $\rho(\Delta)$  and optimize the cost with  $\rho(\Delta)$  replaced by  $q(\Delta; \Delta')$  [8]. In particular,

$$q(\Delta; \Delta') = \frac{\rho'(\Delta')}{2\Delta'} \Delta^2 \quad (12)$$

where  $\Delta'$  denotes the voxel difference before this update. In this way, the original 1D line search is converted into a quadratic optimization and the closed form solution can be derived. Since the substitute cost is always an upper bound of the original cost, minimizing the substitute will also produce a

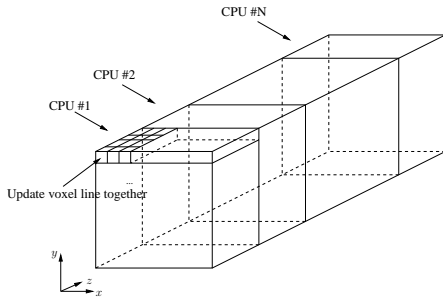


Fig. 2. Parallelized ICD scheme

decreasing sequence of original cost and iterative optimization will lead to the optimal solution of the original problem.

In order to further speed convergence, we also use the non-homogeneous ICD (NHICD) method of [8]. The idea is to focus computation on voxels which tend to generate significant updates. In NHICD, we alternated between a full scan and a partial scan which involves only those voxels which have significant updates at the previous iteration. This scheme provides a further speedup of approximately a factor of three.

#### D. Parallelization

To utilize multi-core processing and speed up the reconstruction for large image volumes, we implemented a parallelized ICD update scheme. In this scheme, the full image volume is cut into  $N$  boxes along the  $z$ -direction as shown in Figure 2 and each processor is responsible for updating voxels in one box. Different processors are synchronized once they finish the work; therefore, one synchronization is made per full scan. This will assign each processor a fairly large amount of work to do in parallel and workload is roughly balanced for different processors in order to reduce processor waiting time. Also, since the image is stored with the index in  $z$ -direction as the fastest-changing variable, the processors update voxels along  $z$ -direction first in order to create better cache efficiency. Moreover, the voxels being updated are selected to be far apart so that they do not share the same sinogram entry, and therefore, can be updated independently.

## IV. RESULTS

In this study, we used the scan data provided by the ALERT (Awareness and Localization of Explosives-Related Threats) Center, at Northeastern University, to conduct our experiments. The projection geometric parameters are listed in Table I. The reconstructed image is of size  $512 \times 512 \times 840$  and the voxel width is 0.975 mm in cross-section in the  $xy$ -plane and the slice thickness is 1.25 mm in  $z$ -direction. Figure 3 illustrates some of the objects contained in the bag used in our experiment.

Figure 6 demonstrates the quality of different reconstruction algorithms. The FBP reconstruction shows several drawbacks. The reconstruction is blurred, as we can see on the feet of the toy Mr. Potato Head in (a). The shape of some objects are distorted. For example, in the center of (a) and (b),

TABLE I  
CT PROJECTION GEOMETRIC PARAMETERS

no. of rows	16
no. of channels	896
no. of rotations	60
no. of views per rotation	960
no. of views	57600
distance from source to iso	518 mm
distance from source to detector	910 mm
helical pitch (normalized)	1
detector width in channel	1.028 mm
channel offset	0.0031 rad
field of view (diameter)	500 mm

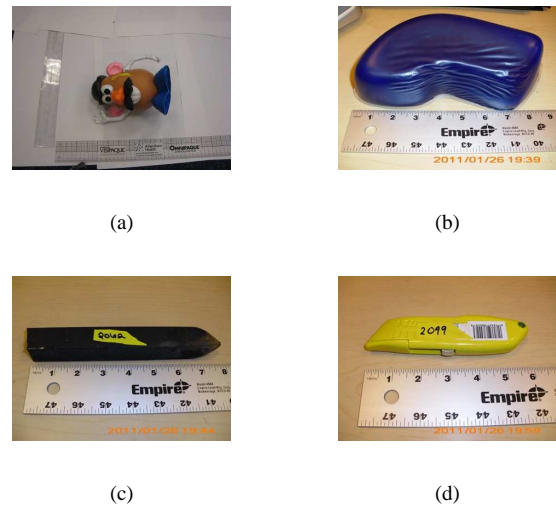


Fig. 3. Objects contained in the baggage (a) toy Mr. Potato Head (b) gel pad (c) steel bar (d) box cutter

the steel bar, which is of high density and supposed to be a rectangular shape, has been distorted. Also, we can see the severe streaking artifacts, such as the region around the high-density objects in (b). The model-based algorithms, on the other hand, provide better reconstructions. The overall image is sharper and shapes of objects are more accurately recovered. Moreover, the model-based algorithm reduces the structured artifacts as compared to the FBP method. These advantages suggest that the model-based algorithm has the ability to provide more detailed and accurate rendering, which could possibly lead to better performance for the security applications.

We further quantify the reconstruction quality by measuring the noise variance on the uniform region. In Figure 4, a target object, which is a plastic bottle of water, is shown. The streaking artifact caused by the nearby high-density metal object can be easily identified in the FBP reconstruction. In Figure 5, we plot the CT voxel values along the line passing through the bottle of water vertically. We observe that the curve of the FBP reconstruction fluctuates more significantly than the

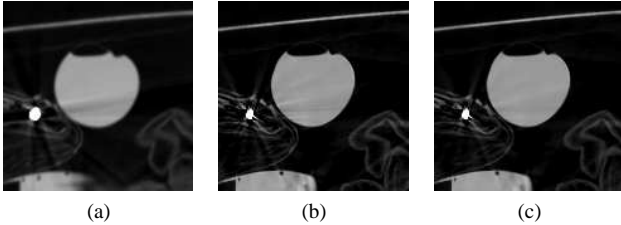


Fig. 4. Reconstructions zoomed to the target area using (a) FBP, (b)  $l_1$  norm prior, and (c) q-GGMRF. The round object is the plastic bottle of water.

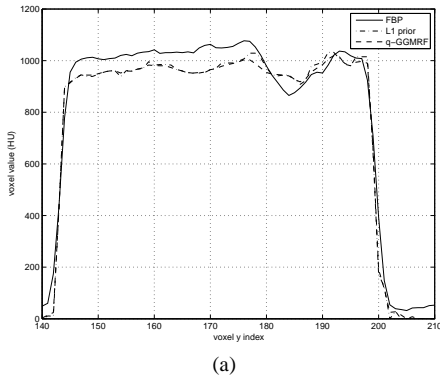


Fig. 5. CT values for voxels along the line through the center of the target region in Figure 4

curve of the other two model-based reconstructions. We further calculate the noise variances with different reconstructions along the line and the result is listed in Table II. The FBP reconstruction leads to the largest noise variance, which is the result of the streaking artifacts. It also shows that q-GGMRF gives the smallest noise variance. This is due to the fact that q-GGMRF has more smoothing effects than the  $l_1$  norm prior.

TABLE II  
NOISE VARIANCE ON UNIFORM REGION

Method	FBP	$l_1$ norm prior	q-GGMRF
Noise variance	3042.8	836.0	496.5

## V. CONCLUSION

In this work, we developed a model-based image reconstruction algorithm and tested it on the data taken from actual baggage. Our algorithm depends on a statistical framework involving a forward model and a prior model. We compared our reconstructions using two different priors,  $l_1$  norm prior and q-GGMRF prior, to the standard FBP algorithm. The model-based algorithms provide better reconstructions and reduce structured artifacts, which suggests potential advantages in application to transportation security.

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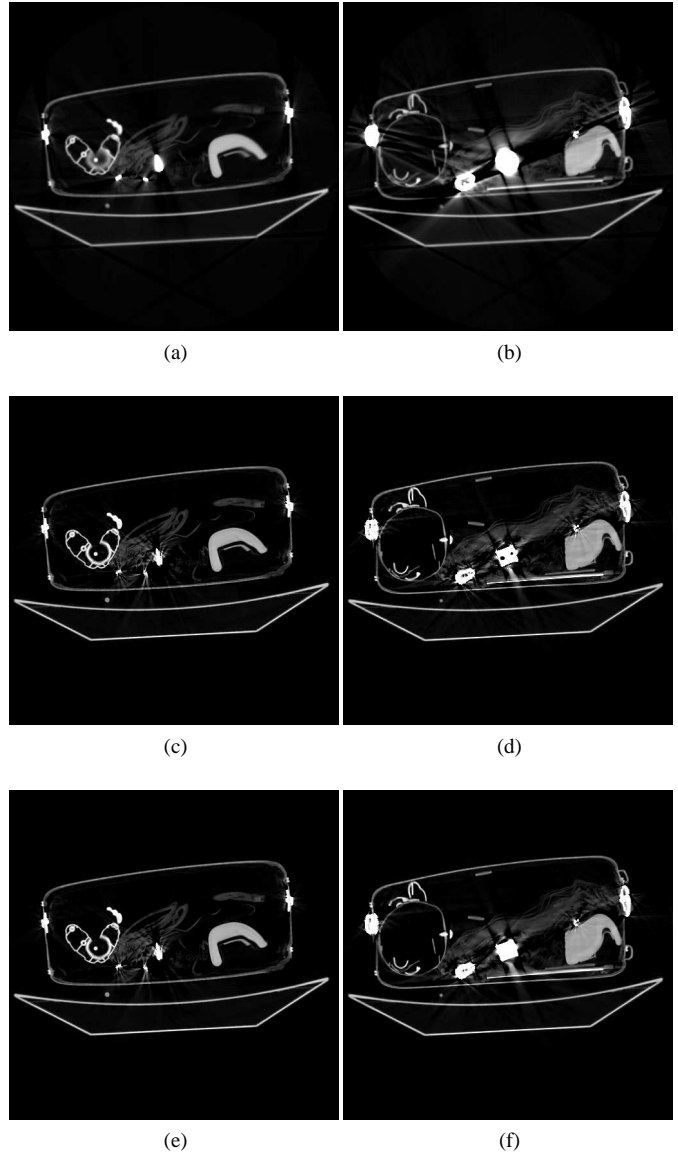


Fig. 6. Reconstruction of the ALERT baggage security data using (a, b) FBP, (c, d)  $l_1$  norm prior, and (e, f) q-GGMRF. The gray scale is in offset Hounsfield Unit (HU), where air = 0 HU and the scale range for all results shown is in  $[0, 1600]$  HU.

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